

# Identify Superior Parental Lines for Biparental Crossing via Genomic Prediction: Rice as an Example

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1 **Identify Superior Parental Lines for Biparental Crossing**  
2 **via Genomic Prediction: Rice as an Example**

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6 **ABSTRACT**

7 **Background:** A set of superior parental lines is the key to high-performing recombinant  
8 inbred lines (RILs) for biparental crossing in a rice breeding program. The number of  
9 possible crosses in such a breeding program is often far greater than the number that  
10 breeders can handle in the field. A practical parental selection method via genomic  
11 prediction (GP) is therefore developed to help breeders identify a set of superior  
12 parental lines from a candidate population before field trials.

13 **Results:** The parental selection via GP often involves truncation selection, selecting the  
14 top fraction of accessions based on their genomic estimated breeding values (GEBVs).  
15 However, the truncation selection inevitably causes a loss of genomic diversity in the  
16 breeding population. To preserve genomic variation, the selection of closely related  
17 accessions should be avoided. We first proposed a new index to quantify the genomic  
18 diversity for a set of candidate accessions. Then, we compared the performance of three  
19 classes of strategy for the parental selection, including those consider (a) GEBV only, (b)  
20 genomic diversity only, and (c) both GEBV and genomic diversity. We analyzed two  
21 rice (*Oryza sativa* L.) genome datasets for the comparison. The results show that the  
22 strategies considering both GEBV and genomic diversity have the best or second-best  
23 performance for all the traits analyzed in this study.

24 **Conclusion:** Combining GP with Monte Carlo simulation can be a useful means of  
25 parental selection for rice pre-breeding programs. Different strategies can be  
26 implemented to identify a set of superior parental lines from a candidate population. In  
27 consequence, the strategies considering both GEBV and genomic diversity that can  
28 balance the starting GEBV average with maintenance of genomic diversity should be

29 recommended for practical use.

30 **Keywords:** genomic prediction, genomic selection, mixed effects model, rice breeding.

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## BACKGROUND

33 Biparental crossing is a commonly used scheme in pure-line breeding for self-pollinated  
34 crops such as rice, wheat (*Triticum aestivum* L.), soybean [*Glycine max* (L.) Merr.] and  
35 oat (*Avena sativa* L.). Plant breeders cross two inbred parental lines to produce F<sub>1</sub>  
36 population, then a subset of diverse individuals of the F<sub>2</sub> population is selected to  
37 produce potential RILs after several generations of selfing. Obviously, the parental lines  
38 play a fundamental role in the line development and significantly affect the performance  
39 of the resulting RILs. However, the identification of superior parental lines from  
40 germplasm collections for creating genetic variation to maximize selection response in  
41 subsequent cycles is still a challenge for plant breeders (Bernardo 2003; Witcombe et al.  
42 2013). Another practical concern is that the number of possible crosses in such a  
43 breeding program is often far greater than the number that breeders can handle in the  
44 field. Therefore, it should be of great help to breeders if a limited number of superior  
45 parents can be identified before the field trial.

46 Genomic selection based on the statistical method of GP has been used to improve  
47 breeding efficiency in dairy cattle (Hayes et al. 2009) and a variety of crops (Massman  
48 et al. 2013; Asoro et al. 2011; Heffner et al. 2011; Lorenz et al. 2012; Spindel et al.  
49 2015). The main concept of GP is to capture all the effects of quantitative trait loci  
50 (QTLs) by using dense DNA markers over the whole genome, assuming that the DNA  
51 markers are in strong linkage disequilibrium with one or more QTLs (Meuwissen et al.  
52 2001). The most commonly used DNA markers are single nucleotide polymorphisms  
53 (SNPs). A GP model is first built using the phenotype and genotype data of a training  
54 population. Then, GEBVs for the candidate individuals with known genotype data are  
55 predicted through the resulting GP model. There are two kinds of mixed linear model  
56 methods are widely employed to obtain the GEBVs: (i) best linear unbiased prediction  
57 (BLUP) based on markers and (ii) BLUP based on a genomic relationship matrix. For

58 the BLUP of (i), the marker effects are treated as random effects and the GEBVs of  
59 individuals are calculated by multiplying their marker scores by these BLUP estimates.  
60 Ridge regression BLUP (rr-BLUP) method (Meuwissen et al. 2001; Piepho 2009)  
61 follows this approach. For the BLUP of (ii), the genotypic values of individuals are  
62 treated as random effects and estimated through a genomic relationship matrix. The  
63 genomic BLUP (GBLUP) method (Habier et al. 2007; VanRaden 2008) follows this  
64 approach. For more details regarding the GP models and the estimation methods used  
65 for their model parameters, refer to Xavier et al. (2016).

66 Gaynor et al. (2017) proposed a two-part strategy for implementing genomic  
67 selection for line development, addressing the two components: (i) a product  
68 development component, to identify inbred lines either for hybrid parent development  
69 or cultivar release; (ii) a population improvement, to increase the frequency of favorable  
70 alleles through rapid recurrent genomic selection. Conducting a stochastic simulation,  
71 they showed that programs using the two-part strategy generated up to 2.5 times more  
72 genetic gain than conventional programs, and up to 1.5 times more genetic gain than the  
73 best performing standard genomic selection strategy. Also, Yao et al. (2018) combined  
74 GP with Monte Carlo simulation to select superior parents in wheat breeding before the  
75 field trial. They used the criterion of usefulness function on a selection index,  
76 incorporating yield and two quality traits, to evaluate a cross. Their usefulness function  
77 took into account both the mean genetic value and genetic variance of progeny  
78 populations. Yao et al. (2018) simulated the required progeny populations using the  
79 R/qtl package (Broman et al. 2003), and calculated their usefulness function estimates.  
80 It was concluded that the use of the usefulness function for parental selection resulted in  
81 higher genetic gain than the use of mid-parent GEBV, implying that the strategy for the  
82 parental selection cannot only consider GEBVs of the candidate accessions.

83 Selecting the parental lines with the highest GEBVs (truncation selection),  
84 breeders hope to maximally pass favorable properties of the parental lines on to their  
85 progeny populations. However, several favorable QTLs can risk being eliminated from  
86 the breeding population using the truncation selection (Vanavermaete et al. 2020). We  
87 therefore take both GEBV and genomic diversity into account for identifying superior  
88 parents in a biparental crossing program. For a specific target trait, we construct a

89 GBLUP model to predict the GEBVs for the candidate accessions. Furthermore, we  
90 propose a new index to quantify the genomic diversity for a set of candidate accessions  
91 according to the GBLUP model. We simulate the genotype data for progeny populations  
92 over successive generations derived from a cross between two parental lines. The  
93 GEBVs of the progeny populations are then predicted by the trained GBLUP model. We  
94 further make generation advancement decisions according to the resulting GEBVs.  
95 Finally, we assess a set of parental lines based on their  $F_{10}$  RILs which are assumed to  
96 be a fixed population. Several selection strategies are evaluated within two rice genome  
97 datasets.

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## MATERIALS AND METHODS

### 100 **The Rice Genome Datasets**

101 **Dataset I:** We first used the rice genome dataset presented in Zhao et al. (2011) to  
102 illustrate our proposed procedure. This dataset was originally collected for  
103 genome-wide association study (GWAS). The dataset contains 44,100 SNP variants and  
104 36 traits of 413 *O. sativa* accessions, and has a strong subpopulation structure  
105 containing six different groups. We deleted any SNPs with a missing rate of  $> 0.05$  and  
106 a minor allele frequency of  $< 0.05$ . To reduce redundant collinearity in calculation of the  
107 genomic relationship matrix, we only retained about one-third of the SNPs which are  
108 evenly distributed over each chromosome. We then imputed a missing SNP marker from  
109 its corresponding major homozygous alleles. The final marker matrix consists of 413  
110 accessions and 11,047 SNPs. We here analyzed the six traits: brown rice seed width  
111 (BRSW), florets per panicle (FPP), flowering time at Arkansas (FTAA), flowering time  
112 at Faridpur (FTAF), plant height (PH), and panicle number per plant (PNPP).

113 **Dataset II:** We further analyzed the rice genome dataset presented in Spindle et al.  
114 (2015), which was collected for genomic selection study. The dataset contains 73,147  
115 SNP variants and 363 elite breeding lines belonging to *indica* or *indica-admixed* group.  
116 The phenotype data include the four years (2009-2012), two seasons per year (dry and

117 wet), of grain yield (YLD), flowering time (FT), and plant height (PH). Note that the  
118 PH data in 2009 wet season are not available. The adjusted means for 328 out of the 363  
119 individuals and 10,772 out of the 73,147 SNP markers were used for this study. We here  
120 chose one marker every 0.1cM over each chromosome.

### 121 **Monte Carlo Simulation for the Genotype of Progeny Populations**

122 To simulate the genotype data for progeny populations, we used Gramene Annotated  
123 Nipponbare Sequence (Youens-Clark et al. 2011) to estimate recombination rates  
124 between two adjacent SNPs. The Gramene Annotated Nipponbare Sequence database  
125 contains both the physical and linkage distances between SNPs, which can be  
126 downloaded from <http://archive.gramene.org>. The genetic positions of the SNPs are  
127 estimated via linear interpolation between the two markers flanking each SNP. Once the  
128 genetic positions were obtained, the recombination rates between adjacent SNPs were  
129 estimated via Haldane's mapping function (Haldane 1919):

$$130 \quad r_{AB} = \frac{1}{2}(1 - e^{-2X_{AB}}),$$

131 where  $r_{AB}$  is the recombination rate and  $X_{AB}$  is the linkage distance between SNP  
132 markers A and B. Through a series of Bernoulli distributions and the estimated  
133 recombination rates, the crossover of each chromosome was simulated to yield the  
134 sequence of a gamete, then two gametes were paired to produce the genotype data for  
135 the progeny.

### 136 **GBLUP Model**

137 We considered the following single-trait GBLUP model for GP:

$$138 \quad \mathbf{y} = \mu \mathbf{1}_n + \mathbf{g} + \mathbf{e}, [1]$$

139 where  $\mathbf{y}$  denotes the vector of phenotypic values of a training population with  $n$   
140 individuals;  $\mu$  is a constant term;  $\mathbf{1}_n$  is the vector of order  $n$  with all elements equal to  
141 1;  $\mathbf{g}$  stands for the vector of genotypic values and  $\mathbf{e}$  is the vector of random errors. It  
142 is assumed that  $\mathbf{g}$  follows a multi-variate normal distribution  $MVN(\mathbf{0}, \sigma_g^2 \mathbf{K})$ , where  $\mathbf{0}$

143 is a zero vector;  $\sigma_g^2$  is the genetic variance of additive effects and  $\mathbf{K}$  is a genomic  
 144 relationship matrix among the individuals. Furthermore,  $\mathbf{e}$  follows  $MVN(\mathbf{0}, \sigma_e^2 \mathbf{I}_n)$ ,  
 145 where  $\sigma_e^2$  is the random error variance and  $\mathbf{I}_n$  denotes the identity matrix of order  $n$ .  
 146 Here,  $\mathbf{g}$  and  $\mathbf{e}$  are assumed to be mutually independent. In this study, we considered  
 147 the genomic relationship matrix  $\mathbf{K} = \mathbf{M}\mathbf{M}^T/p$ , where  $\mathbf{M}$  is the marker score matrix  
 148 and  $p$  is the number of SNP markers. The elements of  $\mathbf{M}$  are coded as  $-1$ ,  $0$ , and  $1$  for  
 149 the minor homozygous alleles ( $A_1A_1$ ), the heterozygous alleles ( $A_1A_2$ ), and the major  
 150 homozygous alleles ( $A_2A_2$ ), respectively. The model parameters of the GBLUP model  
 151 can be estimated through Henderson's equations (Henderson 1984), given by:

$$152 \quad \begin{bmatrix} n & \mathbf{1}_n^T \\ \mathbf{1}_n & \mathbf{I}_n + \lambda \mathbf{K}^{-1} \end{bmatrix} \begin{bmatrix} \hat{\mu} \\ \hat{\mathbf{g}} \end{bmatrix} = \begin{bmatrix} \mathbf{1}_n^T \mathbf{y} \\ \mathbf{y} \end{bmatrix}, [2]$$

153 where the regularization parameter  $\lambda$  is given by  $\lambda = \frac{\sigma_e^2}{\sigma_g^2}$ . We used the R function  
 154 `mmer()` in the R package `sommer` (Covarrubias-Pazarán 2016) to obtain the restricted  
 155 maximum likelihood estimates (REMLs) for the two variance components of  $\sigma_g^2$  and  
 156  $\sigma_e^2$ , and then plugged the resulting estimates into Eq. [2] to get  $\hat{\mu}$  and  $\hat{\mathbf{g}}$ .

157 Let  $\hat{\mathbf{g}}_{bp}$  be the vector of estimated genotypic values for a breeding population and  
 158  $\mathbf{K}_{bp}$  be the genomic relationship matrix between the breeding population and the  
 159 training population. In the case, we have:

$$160 \quad \hat{\mathbf{g}}_{bp} = \mathbf{K}_{bp} \mathbf{K}^{-1} \hat{\mathbf{g}}.$$

161 The GEBV for the breeding population is  $\hat{\mathbf{g}}_{bp}$  plus the estimate of the constant term  $\hat{\mu}$ .

## 162 **The Index to Quantify Genomic Diversity**

163 Let  $\mathbf{g}_0$  be the vector of genotypic values and  $\mathbf{K}_0$  be the genomic relationship matrix  
 164 for a particular set of accessions with size  $n_0$ . According to the GBLUP model of Eq.  
 165 [1], the covariance matrix for  $\mathbf{g}_0$  is given by:

$$166 \quad \text{Var}(\mathbf{g}_0) = \sigma_g^2 \mathbf{K}_0.$$

167 The determinant of the covariance matrix represents the overall variability for the

168 genotypic values, which is calculated as:

$$169 \quad |\text{Var}(\mathbf{g}_0)| = (\sigma_g^2)^{n_0} |\mathbf{K}_0|. [3]$$

170 Clearly, the determinant of Eq. [3] is proportional to the  $D$ -score defined below:

$$171 \quad D\text{-score} = |\mathbf{K}_0|. [4]$$

172 The  $D$ -score of Eq. [4] ranges from 0 to 1. For a fixed number of  $n_0$ , a subset of  
173 accessions chosen from a breeding population that achieves the maximal  $D$ -score will  
174 have greater genomic diversity than the competing choices with size  $n_0$ . The concept of  
175 the  $D$ -score is adopted from optimum experimental designs (Atkinson and Donev 1992).  
176 A simple example is given to illustrate the  $D$ -score. Suppose that there are  $n = 3$   
177 accessions in the candidate set with the genomic relationship matrix:

$$178 \quad \mathbf{K} = \begin{bmatrix} 1 & 0.7 & 0.5 \\ 0.7 & 1 & 0.3 \\ 0.5 & 0.3 & 1 \end{bmatrix}.$$

179 For  $n_0 = 2$ , the  $D$ -score for  $g_1$  and  $g_2$  is calculated as  $|\mathbf{K}_0| = \begin{vmatrix} 1 & 0.7 \\ 0.7 & 1 \end{vmatrix} = 0.51$ .

180 Similarly, the  $D$ -scores for  $g_1$  and  $g_3$ , and for  $g_2$  and  $g_3$  are given by 0.75 and 0.91,  
181 respectively. Clearly, the two accessions with  $g_2$  and  $g_3$  have greater genomic  
182 variation (smaller genomic correlation) than the other competing choices. A set of  
183 accessions with the maximal  $D$ -score can avoid the selection of closely related  
184 individuals.

### 185 **An Algorithm to Search for Accessions with the Maximal $D$ -Score**

186 We required a highly efficient algorithm to search for a subset of accessions within a  
187 candidate population so that it can achieve the maximal  $D$ -score. We used a genetic  
188 algorithm to complete this task, which is an exchange algorithm with the three different  
189 operators: roulette wheel selection, crossover, and mutation (Whitley 1994). For a given  
190 candidate set  $S_c$  with  $n_c$  accessions, we searched for an optimal subset  $S_0$  with  $n_0$   
191 individuals from  $S_c$ . Our algorithm began with a set of  $m$  random solutions, each of  
192 which is a vector of 0 or 1 with a length equal to  $n_c$ . The number of values with a score



193 of 1 in the vector is equal to  $n_0$ , corresponding to the chosen accessions at the current  
194 stage. Here, we fixed  $m = n_0$ . We then obtained the elite solutions from the initial  $m$   
195 random solutions after a large number of iterations, where each iteration repeated all the  
196 three operators. We stopped the algorithm when the maximal  $D$ -score among the current  
197 elite solutions converged.

## 198 **The Procedure for Selecting Parental Lines**

199 To evaluate a variety of strategies in determining parental lines, we carried out the  
200 following steps.

201 Step 1: For a specific target trait, we used all of the phenotypic values available from  
202 the rice genome dataset to build the corresponding GBLUP model of Eq. [1].

203 Step 2: We predicted the GEBVs for all of the accessions in the dataset through the  
204 trained GBLUP model developed in Step 1. Seven strategies were used to select a subset  
205 of 10 parental lines according to their GEBVs: (i) the GEBV only (GEBV-O) approach,  
206 which chose the top 10 accessions (either maximal or minimal); the genomic diversity  
207 only (GD-O) approaches: (ii) GD-O-30, (iii) GD-O-50, and (iv) GD-O-100, which  
208 applied the genetic exchange algorithm to search for an optimal subset of 10 accessions  
209 from each of the three candidate sets composed of the top 30, 50, and 100 accessions,  
210 respectively, such that the chosen subset had the maximal  $D$ -score; and the approaches  
211 (GEBV-GD) considering both GEBV and genomic diversity: (v) GEBV-GD-30, (vi)  
212 GEBV-GD-50, and (vii) GEBV-GD-100, which retained the top two accessions, then  
213 applied the genetic exchange algorithm to search for another eight accessions from the  
214 remainder of each candidate set for GD-O-30, GD-O-50, and GD-O-100, respectively,  
215 so that the resulting 10 accessions had the maximal  $D$ -score.

216 Step 3: For each subset of 10 accessions determined by the seven strategies, we crossed  
217 any two parental lines to produce 45  $F_1$  hybrids. Here, we started to simulate the  
218 genotype data for successive generations of progeny populations through the Monte  
219 Carlo simulation. Each of the 45  $F_1$  hybrids produced 60 individuals of the  $F_2$   
220 population by self-pollination, resulting in 2700  $F_2$  individuals. After obtaining the  
221 GEBVs for the 2700  $F_2$  individuals via the trained GBLUP model of Step 1, we then

222 retained the top 45 F<sub>2</sub> individuals. Again, we used these 45 F<sub>2</sub> individuals to produce  
223 2700 F<sub>3</sub> individuals (each F<sub>2</sub> individual produced 60 F<sub>3</sub> individuals) and retained the top  
224 45 F<sub>3</sub> individuals. We then repeated the same procedure to produce 2700 F<sub>10</sub> individuals  
225 which are assumed to be a fixed population.

226 Step 4: For the resulting 2700 F<sub>10</sub> individuals generated according to each strategy, we  
227 found the best F<sub>10</sub> RIL with the top GEBV.

228 A flowchart of the procedure is displayed in Figure 1. We repeated this analysis  
229 procedure 30 times to obtain the best F<sub>10</sub> RILs from each repetition for each strategy.  
230 The average of the GEBVs for the best F<sub>10</sub> RILs was then calculated and used as the  
231 measure of efficiency for the strategy. Note that for the traits of BRSW, FPP, and PNPP  
232 in Dataset I; and YLD in Dataset II, larger GEBVs are preferable (i.e., these traits  
233 follow the rule that the larger, the better). The remaining five traits of FTAA, FTAF, and  
234 PH in Dataset I; and FT, and PH in Dataset II are those for which the rule is “the smaller,  
235 the better”.

### 236 **Calculation of Genetic Gain**

237 To gain an understanding of the genetic improvement on a target trait using  
238 different strategies, we estimated genetic gain as

$$239 \text{ genetic gain} = \overline{GEBV}_{F_{10}} - \overline{GEBV}_P, [5]$$

240 where  $\overline{GEBV}_{F_{10}}$  denotes the GEBV average among the resulting 2700 F<sub>10</sub> RILs and  
241  $\overline{GEBV}_P$  denotes the GEBV average among the 10 selected parental lines for each  
242 strategy (Rutkoski 2019). The larger absolute value of the genetic gain indicates the  
243 more improvement on the target trait.

244

245

## **RESULTS**

## 246 **Strategies Comparison Based on the best $F_{10}$ RILs**

247 The GEBV averages of the best  $F_{10}$  RILs from the 30 repetitions using each of the  
248 seven strategies are displayed in Tables 1 and 2 for the two datasets. The results in the  
249 tables show that the strategies considering both GEBV and genomic diversity  
250 (GEBV-GD-30, -50, -100) generally have satisfactory efficiency, because they achieve  
251 the best or second-best performance for all the traits. Therefore, this kind of strategies  
252 could be a reliable means of determining the parental lines. On the other hand, the  
253 strategies accounting for genomic diversity only (GD-O-30, -50, -100) don't have  
254 satisfactory efficiency for all the traits, with the exception of GD-O-100 for YLD in  
255 Dataset II. For the strategy based on GEBV only, the GEBV-O has the best or  
256 second-best performance for FPP, and PH in Dataset I; and PH, and FT in Dataset II, but  
257 also has the worst or second-worst performance for the remaining four traits in Dataset I  
258 and YLD in Dataset II. Thus, the GEBV-O could be a high-risk strategy.

259 We also displayed the GEBV averages with the plus and minus one unit of their  
260 corresponding standard deviations for the best individuals from the 30 repetitions over  
261 consecutive generations in Figures 2 and 3. From the figures, the four strategies of  
262 GEBV-O, GEBV-GD-30, -50, -100 selected the same best individual from the 30  
263 repetitions at parental generation, and also at  $F_1$  generation, so there is no standard  
264 deviation shown with the corresponding GEBV averages. The GEBV averages of the  
265 best selected parental lines by the strategies can be ranked as GEBV-O = GEBV-GD-30  
266 = GEBV-GD-50 = GEBV-GD-100 > GD-O-30 > GD-O-50 > GD-O-100 in decreasing  
267 desirability. The desirability at parental generation decreases as the degree of diversity  
268 increases for the three strategies considering the genomic diversity only. Also, the  
269 desirability declines from parental generation to  $F_1$  generation for every strategy, due to  
270 the heterogenous alleles in  $F_1$  hybrids.

271 To explore the extent to which the top two accessions contribute to the subset of  
272 ten parental lines determined by the four strategies of GEBV-O, GEBV-GD-30, -50,  
273 -100, we compared each subset with a reduced group consisting of  $F_1$  hybrids whose  
274 parental lines contain at least one of the top two accessions for each subset. Every  
275 reduced group consists of 17  $F_1$  hybrids. Similarly, we followed the analysis procedure

276 to obtain the GEBV averages for the best  $F_{10}$  RILs from 30 repetitions based on the  
277 reduced group. The results are displayed in Table 3 with the corresponding GEBV  
278 averages based on the group of the original 45  $F_1$  hybrids. From the table, there is no  
279 practical significant difference between these two groups for all the traits using the four  
280 strategies.

## 281 Genetic Gains for the Strategies

282 The average among the genetic gains on a target trait for each strategy calculated  
283 by Eq. [5] from the 30 repetitions is displayed in Tables 4 and 5 for Datasets I and II,  
284 respectively. It is reasonable to compare the performance of the strategies according to  
285 the endpoint of  $\overline{GEBV}_{F_{10}}$ . From the tables, we found that the comparison results based  
286 on  $\overline{GEBV}_{F_{10}}$  are consistent with the above results based on the best  $F_{10}$  RILs. Also, the  
287 strategies considering genomic diversity (GD-O-30, -50, -100; GEBV-GD-30, -50, -100)  
288 have greater genetic gain than the GEBV-O for all the traits except PH in Dataset I  
289 (Table 4). As expected, the genetic gain usually increases with the increase of the  
290 genomic diversity (GD-O-100 outperforms both GD-O-50 and GD-O-30 for all the  
291 traits except BRSW, and FTAF in Dataset I; GEBV-GD-100 outperforms both  
292 GEBV-GD-50 and GEBV-GD-30 for all the traits). In addition, GEBV-O has the best  
293  $\overline{GEBV}_p$ ; GEBV-GD-30 has better  $\overline{GEBV}_p$  than GD-O-30; GEBV-GD-50 has better  
294  $\overline{GEBV}_p$  than GD-O-50 and GEBV-GD-100 has better  $\overline{GEBV}_p$  than GD-O-100 for all  
295 the traits. Namely, a strategy has a relatively good starting point as it considers more  
296 degree of GEBV.

297

298

## DISCUSSION

299 From the results for comparing the proposed strategies, those considering both GEBV  
300 and genomic diversity or considering GEBV only can be recommended for practical use.  
301 Furthermore, from the results for exploring the extent to which the top two accessions  
302 contribute to the parental lines determined by the four strategies of GEBV-O,  
303 GEBV-GD-30, -50, -100, we have the conclusion: the economical strategies with 17  $F_1$

304 hybrids whose parental lines contain at least one of the top two accessions for each  
305 selected subset can be a practical alternative to those with 45 F<sub>1</sub> hybrids composed of all  
306 of the possible crosses.

307 From Tables 4 and 5, the strategies considering genomic diversity only (GD-O-30,  
308 -50, -100) generally have greater genetic gain, mainly due to their more genomic  
309 variation but less favorable  $\overline{GEBV}_p$ , so they have more room to improve. Also, the  
310 GEBV-O has the best starting  $\overline{GEBV}_p$  but the least genomic diversity in the base  
311 population, so it has less potential to improve. The strategies considering both GEBV  
312 and genomic diversity (GEBV-GD-30, -50, -100) could balance the tradeoff between  
313 starting  $\overline{GEBV}_p$  and genomic variation of the base population.

314 Dataset II was specifically collected for genomic selection. All of the available  
315 accessions in the dataset belong to *indica* or *indica-admixed* group. From the results of  
316 the performance based on the best F<sub>10</sub> RILs in Table 2, all the seven strategies seem to  
317 have close performance for the three target traits. The resulting GEBV averages of the  
318 best F<sub>10</sub> RILs range from 6472 to 6546 kg/ha for YLD, from 85.889 to 91.852 cm for  
319 PH, and from 77.725 to 78.410 days for FT. This could be due to the fact that the  
320 candidate accessions in Dataset II are elite breeding lines which have limited genomic  
321 diversity and similar phenotypic values for the target traits. However, the two strategies  
322 with greater genomic diversity, GD-O-100 and GEBV-GD-100 for YLD (their  
323 corresponding GEBV averages are 6546 and 6539 kg/ha), led to larger YLD than the  
324 other five strategies (their corresponding GEBV averages range from 6472 to 6506  
325 kg/ha). The four strategies of GEBV-O, GEBV-GD-30, -50, -100 performed equally  
326 well for PH (their corresponding GEBV averages range between 85.817 and 86.062 cm),  
327 but slightly better than GD-O-30, -50, -100 (their corresponding GEBV averages are  
328 87.517, 89.920, and 91.799 cm). The consistent results based on the  $\overline{GEBV}_{F_{10}}$  can be  
329 found in Table 5.

330 It is known that Dataset I contains more genomic diversity than Dataset II, since it  
331 consists of five subpopulations and one admixed group. The more genomic diversity of  
332 Dataset I could lead to a bigger difference between the strategies considering both  
333 GEBV and genomic diversity, and the strategy considering GEBV only for some traits.

334 For example, the difference of the GEBV averages among the best F<sub>10</sub> RILs between  
335 GEBV-GD-50 and GEBV-O is about -9.06 days for FTAA, and -2.55 days for FTAF in  
336 Dataset I (Table 1), but the corresponding difference is just -0.09 days for FT in Dataset  
337 II (Table 2). However, the flowering time is very sensitive to environments, so the  
338 genomic diversity cannot solely amount to the different results between these two  
339 datasets. More interestingly, the more genomic diversity of Dataset I could lead to a  
340 larger genetic gain for a specific trait. From Table 4, the mean of the genetic gains using  
341 the seven strategies for PH in Dataset I is given by -42.15 cm. But, from Table 5, the  
342 corresponding mean in Dataset II is just -13.79 cm.

343 Daetwyler et al. (2015) and Goiffon et al. (2017) highlighted that an increase in  
344 rare favorable alleles in a population can help improve selection responses. Selecting  
345 only parental lines with the highest GEBVs can result in a loss of rare favorable alleles  
346 for some target traits, thus missing potential RILs over future generations. From the  
347 results of BRSW, FTAA, FTAF, and PNPP in Figure 2; and YLD in Figure 3, the  
348 performance of GEBV-O appears to be inferior to GEBV-GD-30, -50, -100. This  
349 indicates that an increase in genomic diversity in parental lines could compensate for  
350 this possible deficiency, and then improve the long-term response to the target traits.  
351 The greater genomic diversity could increase the possibility of containing favorable  
352 alleles in parental lines, and we therefore expect that the chance of harboring the  
353 favorable alleles would increase in RIL populations.

354 Apparently, the numbers of accessions fixed in the proposed strategies seem to be a  
355 little arbitrary, such as those of selecting 10 parental lines, retaining the top 2 accessions,  
356 and searching 10 or another 8 accessions from the three candidate sets composed of the  
357 top 30, 50 and 100 accessions, respectively. A user certainly can adjust these numbers in  
358 the strategies for her/his own study. Also, it was required to have historical phenotypic  
359 data used to build the GP model. If the historical phenotypic data are not available, then  
360 a pilot experiment is needed to phenotype a set of accessions, which can be determined  
361 using an optimization algorithm (Ou and Liao 2019). An R function for performing the  
362 proposed procedure of selecting parental lines is available from the authors upon  
363 request.

364 As mentioned earlier, Yao et al. (2018) evaluated genetic gain using the usefulness  
365 function in parental selection, and showed that their selection strategy outperformed the  
366 strategy using the mid-parent GEBV. In this study, we emphasized both GEBV and  
367 genomic diversity in parental selection, and we made generation advancement decisions  
368 for each selection strategy according to the GEBVs of the top individuals. Finally, we  
369 compared different strategies based on the performance of the best F<sub>10</sub> RILs, and  
370 discussed genetic gain for target traits using the strategies. Moreover, Yao et al. (2018)  
371 showed that applying a selection index incorporating multiple traits can simultaneously  
372 improve both yield and quality in wheat than the individual trait selection. Also, Jia and  
373 Jannink (2012), Hayashi and Iwata (2013), and Guo et al. (2014) highlighted that  
374 multiple-trait GP models can provide better prediction accuracy than single-trait GP  
375 models for those traits with low heritability. We will consider the selection index and the  
376 multiple-trait GP models into the framework of the current study, so as to investigate the  
377 multiple-trait situations in a future study.

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## CONCLUSIONS

380 Combining GP with Monte Carlo simulation can be a useful means of detecting superior  
381 parents for rice pre-breeding programs. Different strategies can be implemented to  
382 identify a set of superior parental lines from a candidate population. The strategy  
383 considering GEBV only can have a better starting GEBV average but less genomic  
384 diversity in the base population. On the other hand, the strategies considering genomic  
385 diversity only can have greater genomic diversity but a less favorable starting GEBV  
386 average in the base population. The strategies considering both GEBV and genomic  
387 diversity that can balance the starting GEBV average with maintenance of genomic  
388 diversity should be recommended for practical use.

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390 **Abbreviations:** BLUP, best linear unbiased predictor; BRSW, brown rice seed width;  
391 GBLUP, genomic best linear unbiased predictor; GEBV, genomic estimated breeding

392 value; GEBV-GD, algorithms considering both GEBV and genomic diversity; GEBV-O,  
393 algorithms considering GEBV only; FPP, florets per panicle; FT, flowering time; FTAA,  
394 flowering time at Arkansas; FTAF, flowering time at Faridpur; GD-O, algorithms  
395 considering genomic diversity only; PH, plant height; PNPP, panicle number per plant;  
396 RIL, recombinant inbred line; SNP, single nucleotide polymorphism; YLD, grain yield.

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## DECLARATIONS

401 **Ethical Approval and Consent to participate:** Not applicable.

402 **Consent for publication:** Not applicable.

403 **Availability of supporting data:** Not applicable.

404 **Competing interests:** The authors declare that there is no conflict of interest.

405 **Funding:** Not applicable.

406 **Authors' contributions:** PY analyzed the datasets, wrote the R functions, prepared the  
407 tables and figures, and drafted the manuscript. CT supervised the research, derived the  
408 analysis approach, and drafted the manuscript.

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## REFERENCES

413

414 Asoro, F.G., M.A. Newell, W.D. Beavis, M.P. Scott, and J.L. Jannink. 2011. Accuracy  
415 and training population design for genomic selection on quantitative traits in  
416 elite north American oats. *Plant Genome* 4: 132–144.

417 Atkison, A.C., and A.N. Donev. 1992. *Optimum experimental designs*. New York:



- 418 Oxford University Press.
- 419 Bernardo, R. 2003. Parental selection, number of breeding populations, and size of each  
420 population in inbred development. *Theor. Appl. Genet.* 107: 1252-1256.
- 421 Broman, K.W., H. Wu, S. Sen, and G.A. Churchill. 2003. R/qtl: QTL mapping in  
422 experimental crosses. *Bioinformatics* 19: 889-890.
- 423 Covarrubias-Pazarán, G. 2016. Genome-assisted prediction of quantitative traits using  
424 the R package sommer. *PLOS One* 11: e0156744.
- 425 Daetwyler, H.D., M.J. Hayden, G.C. Spangenberg, and B.J. Hayes. 2015. Selection on  
426 optimal haploid value increases genetic gain and preserves more genetic  
427 diversity relative to genomic selection. *Genetics* 200: 1341–1348.
- 428 Gaynor, R.C., G. Gorjanc, A.R. Bentley, E.S. Ober, P. Howell, R. Jackson, et al. 2017. A  
429 two-part strategy for using genomic selection to develop inbred lines. *Crop Sci.*  
430 57: 2372–2386.
- 431 Goiffon, M., A. Kusmec, L. Wang, G. Hu, and P.S. Schnable. 2017. Improving response  
432 in genomic selection with a population-based selection strategy: Optimal  
433 population value selection. *Genetics* 206: 1675–1682.
- 434 Guo, G., F. Zhao, Y. Wang, Y. Zhang, L. Du, and G. Su. 2014. Comparison of  
435 single-trait and multiple-trait genomic prediction models. *BMC Genetics* 15: 30.
- 436 Habier, D., R.L. Fernando, and J.C.M. Dekkers. 2007. The impact of genetic  
437 relationship information on genome-assisted breeding values. *Genetics* 177:  
438 2389–2397.
- 439 Haldane, J.B.S. 1919. The combination of linkage values and the calculation of distance  
440 between the loci for linked factors. *Genetics* 8: 299–309.
- 441 Hayashi, T., and H. Iwata. 2013. A Bayesian method and its variational approximation

442 for prediction of genomic breeding values in multiple traits. BMC  
443 bioinformatics 14: 1–14.

444 Hayes, B.J., P.J. Bowman, A.J. Chamberlain, and M.E. Goddard. 2009. Genomic  
445 selection in dairy cattle: Progress and challenges. J. Dairy Sci. 92: 433–443.

446 Heffner, E.L., J.L. Jannink, and M.E. Sorrells. 2011. Genomic selection accuracy using  
447 multifamily prediction models in wheat breeding program. Plant Genome 4: 65–  
448 75.

449 Henderson, C.R. 1984. Applications of linear models in animal breeding. Univ. of  
450 Guelph, Guelph, Ontario.

451 Jia, Y., and J.L. Jannink. 2012. Multiple-trait genomic selection methods increase  
452 genetic value prediction accuracy. Genetics 192: 1513-1522.

453 Lorenz, A.J., K.P. Smith, and J.L. Jannink. 2012. Potential and optimization of genomic  
454 selection for *Fusarium* head blight resistance in six-row barley. Crop Sci. 52:  
455 1609–1621.

456 Massman, J.M., H.J.G. Jung, and R. Bernardo. 2013. Genomewide selection versus  
457 marker-assisted recurrent selection to improve grain yield and stover-quality  
458 traits for cellulosic ethanol in maize. Crop Sci. 53: 58–66.

459 Meuwissen, T.H.E., B.J. Hayes, and M.E. Goddard. 2001. Prediction of total genetic  
460 value using genome-wide dense marker maps. Genetics 157: 1819–1829.

461 Ou, J.H., and C.T. Liao. 2019. Training set determination for genomic selection. Theor.  
462 Appl. Genet. 132: 2781–2792.

463 Piepho, H.P. 2009. Ridge regression and extensions for genome-wide selection in maize.  
464 Crop Sci. 49: 1165–1176.

465 Rutkoski, J.E. 2019. A practical guide to genetic gain. Adv. Agron. 157: 217-249.

- 466 Spindel, J., H. Begum, D. Akdemir, P. Virk, B. Collard, E. Redona, et al. 2015. Genomic  
467 selection and association mapping in rice (*Oryza sativa*): Effect of trait genetic  
468 architecture, training population composition, marker number and statistical  
469 model on accuracy of rice genomic selection in elite, tropical rice breeding lines.  
470 PLOS Genetics 11: e1005350.
- 471 VanRaden, P.M. 2008. Efficient methods to compute genomic predictions. J. Dairy Sci.  
472 91: 4414–4423.
- 473 Vanavermaete, D., J. Fostier, S. Maenhout, and B. De Baets. 2020. Preservation of  
474 genetic variation in a breeding population for long-term genetic gain. G3:  
475 Genes|Genomes|Genetics doi:10.1534/g3.120.401354.
- 476 Whitley, D. 1994. A genetic algorithm tutorial. Stat. Comput. 4: 65–85.
- 477 Witcombe, J.R., S. Gyawali, M. Subedi, D.S. Virk, and K.D. Joshi. 2013. Plant breeding  
478 can be made more efficient by having fewer, better crosses. BMC Plant Biol. 13:  
479 22.
- 480 Xavier, A., W.M. Muir, B. Craig, and K.M. Rainey. 2016. Walking through the  
481 statistical black boxes of plant breeding. Theor. Appl. Genet. 129: 1933–1949.
- 482 Yao, J., D. Zhao, X. Chen, Y. Zhang, and J. Wang. 2018. Use of genomic selection and  
483 breeding simulation in cross prediction for improvement of yield and quality in  
484 wheat (*Triticum aestivum* L.). Crop J. 6: 353-365.
- 485 Youens-Clark, K., E. Buckler, T. Casstevens, C. Chen, G. DeClerck, P. Derwent, et al.  
486 2011. Gramene database in 2010: updates and extensions. Nucleic Acids Res. 39:  
487 D1085–D1094.
- 488 Zhao, K., C.W. Tung, G.C. Eizenga, M.H. Wright, M.L. Ali, A.H. Price, et al. 2011.  
489 Genome-wide association mapping reveals a rich genetic architecture of  
490 complex traits in *Oryza sativa*. Nature Communications 2: 467.

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496 Table 1: The ranking and the GEBV average (in parentheses) for the best  $F_{10}$  RILs from  
 497 the 30 repetitions using the seven proposed strategies in Dataset I.

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	BRSW	FPP	FTAA	FTAF	PH	PNPP
GEBV-O	<u>6 (3.418)</u>	<b>2 (5.961)</b>	<u>6 (56.521)</u>	<u>6 (61.856)</u>	<b>1 (42.185)</b>	<u>6 (4.125)</u>
GD-O-30	<u>7 (3.408)</u>	5 (5.951)	3 (51.564)	3 (59.353)	5 (49.337)	3 (4.188)
GD-O-50	3 (3.576)	<u>6 (5.916)</u>	5 (53.348)	5 (60.126)	<u>6 (49.801)</u>	5 (4.138)
GD-O-100	4 (3.496)	<u>7 (5.882)</u>	<u>7 (56.835)</u>	<u>7 (61.967)</u>	<u>7 (51.788)</u>	<u>7 (4.086)</u>
GEBV-GD-30	5 (3.419)	3 (5.954)	<b>1 (47.136)</b>	<b>1 (59.216)</b>	<b>2 (42.699)</b>	<b>1 (4.225)</b>
GEBV-GD-50	<b>1 (3.656)</b>	<b>1 (5.964)</b>	<b>2 (47.457)</b>	<b>2 (59.304)</b>	3 (43.232)	<b>2 (4.214)</b>
GEBV-GD-100	<b>2 (3.634)</b>	4 (5.953)	4 (51.382)	4 (59.634)	4 (43.498)	4 (4.171)

499

500 (i) The best and second-best strategies are indicated in bold text, and the worst and  
 501 second-worst strategies are indicated by underlining.

502 (ii) GEBV-O: the subset of the top 10 accessions with the minimal or maximal GEBVs;

503 GD-O-30, -50, -100: the subsets of 10 accessions with the maximal D-scores chosen  
 504 from the candidate sets composed of the top 30, 50, and 100 accessions, respectively;

505 GEBV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen  
 506 from the remainder of the candidate sets composed of the top 30, 50, and 100 accessions,

507 respectively, which have the maximal D-scores.

508 (iii) BRSW: brown rice seed width; FPP: florets per panicle; FTAA: flowering time at  
 509 Arkansas; FTAF: flowering time at Faridpur; PH: plant height; PNPP: panicle number  
 510 per plant.

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516 Table 2: The ranking and the GEBV average (in parentheses) for the best  $F_{10}$  RILs from  
 517 the 30 repetitions using the seven proposed strategies in Dataset II.

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	YLD	PH	FT
GEBV-O	<u>7 (6472)</u>	<b>1 (85.817)</b>	<b>2 (77.818)</b>
GD-O-30	4 (6491)	5 (87.517)	<u>7 (78.410)</u>
GD-O-50	5 (6489)	<u>6 (89.920)</u>	5 (78.164)
GD-O-100	<b>1 (6546)</b>	<u>7 (91.799)</u>	<u>6 (78.359)</u>
GEBV-GD-30	3 (6506)	<b>2 (85.976)</b>	4 (77.883)
GEBV-GD-50	<u>6 (6485)</u>	3 (85.917)	<b>1 (77.725)</b>
GEBV-GD-100	<b>2 (6539)</b>	4 (86.062)	3 (77.873)

519

520 (i) The best and second-best strategies are indicated in bold text, and the worst and  
 521 second-worst strategies are indicated by underlining.

522 (ii) GEBV-O: the subset of the top 10 accessions with the minimal or maximal GEBVs;

523 GD-O-30, -50, -100: the subsets of 10 accessions with the maximal D-scores chosen

524 from the candidate sets composed of the top 30, 50, and 100 accessions, respectively;

525 GEBV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen

526 from the remainder of the candidate sets composed of the top 30, 50, and 100 accessions,

527 respectively, which have the maximal D-scores.

528 (iii) YLD: yield; PH: plant height; FT: flowering time.

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534 Table 3: The GEBV averages for the best  $F_{10}$  RILs from the 30 repetitions based on the  
535 group of the original 45  $F_1$  hybrids and the reduced group of 17  $F_1$  hybrids using the  
536 four strategies of GEBV-O, GEBV-GD-30, GEBV-GD-50, and GEBV-GD-100.

537

	GEBV-O		GEBV-GD-30		GEBV-GD-50		GEBV-GD-100	
Dataset I	45 $F_1$	17 $F_1$	45 $F_1$	17 $F_1$	45 $F_1$	17 $F_1$	45 $F_1$	17 $F_1$
BRSW	3.418	3.423	3.419	3.418	3.656	3.652	3.634	3.650
FPP	5.961	5.965	5.954	5.957	5.964	5.958	5.953	5.943
FTAA	56.521	57.513	47.136	46.961	47.457	47.421	51.382	51.734
FTAF	61.856	61.850	59.216	59.123	59.304	59.232	59.634	59.713
PH	42.185	43.409	42.699	43.271	43.232	43.791	43.498	43.854
PNPP	4.125	4.129	4.225	4.226	4.214	4.204	4.171	4.161
Dataset II	45 $F_1$	17 $F_1$	45 $F_1$	17 $F_1$	45 $F_1$	17 $F_1$	45 $F_1$	17 $F_1$
YLD	6472	6476	6506	6499	6485	6484	6539	6534
PH	85.817	85.991	85.976	85.844	85.917	86.092	86.062	86.060
FT	78.818	77.834	77.883	77.750	77.725	77.778	77.873	77.690

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539 (i) GEBV-O: the subset of the top 10 accessions with the minimal or maximal GEBVs;

540 GEBV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen

541 from the remainder of the candidate sets composed of the top 30, 50, and 100 accessions,

542 respectively, which have the maximal D-scores.

543 (ii) BRSW: brown rice seed width; FPP: florets per panicle; FTAA: flowering time at  
 544 Arkansas; FTAF: flowering time at Faridpur; PH: plant height; PNPP: panicle number  
 545 per plant.

546 (iii) YLD: yield; PH: plant height; FT: flowering time.

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550 Table 4: The average of genetic gains from the 30 repetitions for Dataset I.

551

	BRSW			FPP		
	$\overline{\text{GEBV}}_P$	$\overline{\text{GEBV}}_{F_{10}}$	genetic gain	$\overline{\text{GEBV}}_P$	$\overline{\text{GEBV}}_{F_{10}}$	genetic gain
GEBV-O	3.17	3.42	0.25	5.51	5.96	0.45
GD-O-30	3.10	3.41	0.31	5.48	5.95	0.47
GD-O-50	3.00	3.57	0.57	5.41	5.91	0.50
GD-O-100	2.94	3.49	0.55	5.31	5.88	0.57
GEBV-GD-30	3.12	3.42	0.30	5.48	5.95	0.47
GEBV-GD-50	3.04	3.65	0.61	5.43	5.96	0.53
GEBV-GD-100	3.00	3.63	0.63	5.34	5.95	0.61
	FTAA			FTAF		
	$\overline{\text{GEBV}}_P$	$\overline{\text{GEBV}}_{F_{10}}$	genetic gain	$\overline{\text{GEBV}}_P$	$\overline{\text{GEBV}}_{F_{10}}$	genetic gain
GEBV-O	64.30	56.57	-7.73	63.45	61.87	-1.58
GD-O-30	72.25	49.26	-22.99	64.93	59.40	-5.53
GD-O-50	75.41	53.54	-21.87	65.82	60.16	-5.66
GD-O-100	80.01	57.00	-23.01	67.34	62.01	-5.33
GEBV-GD-30	71.09	47.31	-23.78	64.68	59.25	-5.43
GEBV-GD-50	72.86	47.64	-25.22	65.40	59.35	-6.05
GEBV-GD-100	77.16	51.53	-25.63	66.46	59.68	-6.78
	PH			PNPP		
	$\overline{\text{GEBV}}_P$	$\overline{\text{GEBV}}_{F_{10}}$	genetic gain	$\overline{\text{GEBV}}_P$	$\overline{\text{GEBV}}_{F_{10}}$	genetic gain
GEBV-O	83.77	42.52	-41.25	3.93	4.12	0.19
GD-O-30	89.50	49.69	-39.81	3.86	4.19	0.33
GD-O-50	90.11	50.13	-39.98	3.80	4.14	0.34
GD-O-100	92.10	52.10	-40.00	3.64	4.08	0.44
GEBV-GD-30	87.26	42.99	-44.27	3.90	4.22	0.32
GEBV-GD-50	87.95	43.50	-44.45	3.84	4.21	0.37
GEBV-GD-100	89.27	43.95	-45.32	3.70	4.17	0.47

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554 (i)  $\overline{GEBV}_p$ : the GEBV average among the 10 selected parental lines.  $\overline{GEBV}_{F_{10}}$  : the  
555 GEBV average among the resulting 2700 F<sub>10</sub> RILs.  
556 (ii) GEBV-O: the subset of the top 10 accessions with the minimal or maximal GEBVs;  
557 GD-O-30, -50, -100: the subsets of 10 accessions with the maximal D-scores chosen  
558 from the candidate sets composed of the top 30, 50, and 100 accessions, respectively;  
559 GEBV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen  
560 from the remainder of the candidate sets composed of the top 30, 50, and 100 accessions,  
561 respectively, which have the maximal D-scores.  
562 (iii) BRSW: brown rice seed width; FPP: florets per panicle; FTAA: flowering time at  
563 Arkansas; FTAF: flowering time at Faridpur; PH: plant height; PNPP: panicle number  
564 per plant.

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Table 5: The average of genetic gains from the 30 repetitions for Dataset II.

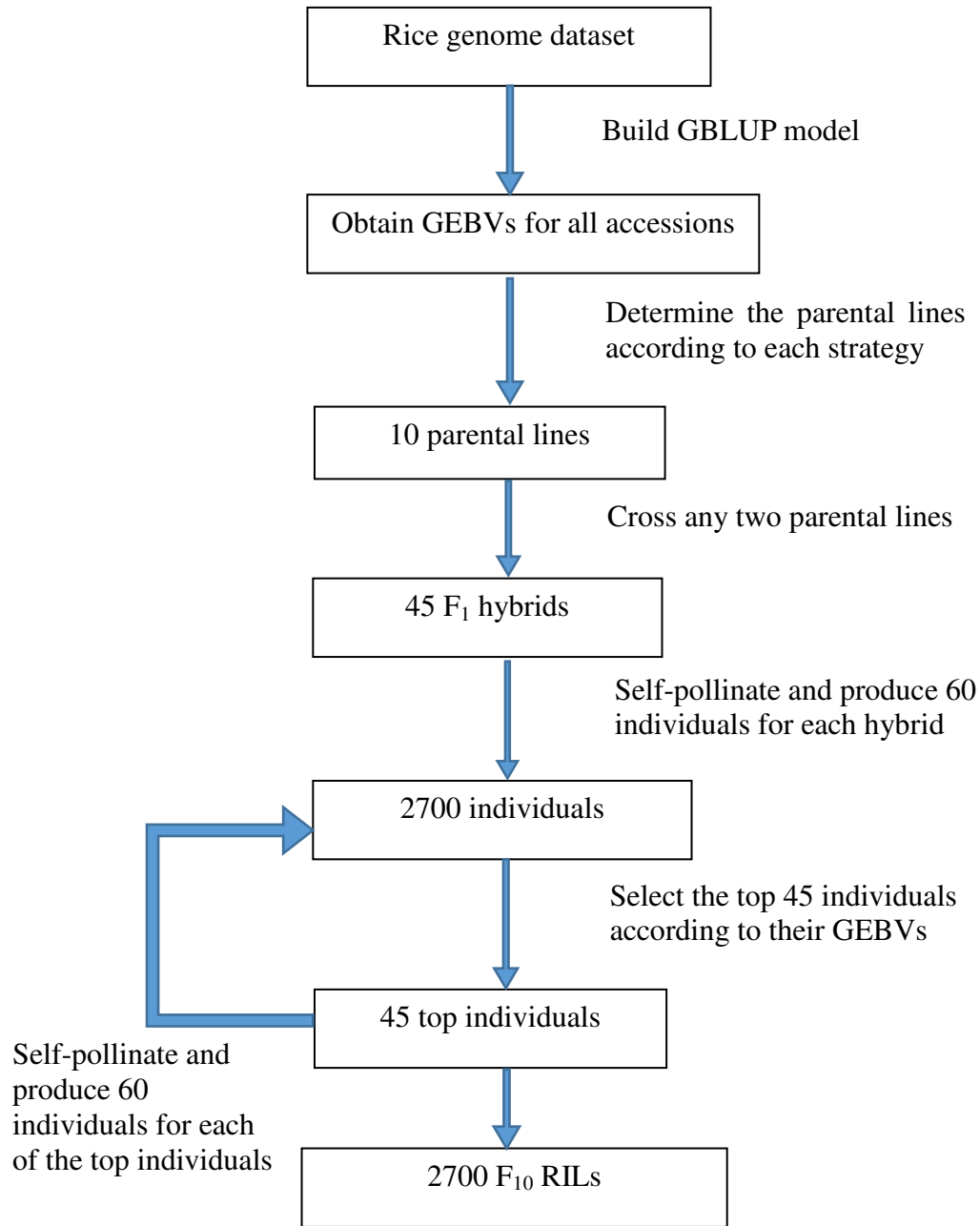
YLD			
	$\overline{GEBV}_P$	$\overline{GEBV}_{F_{10}}$	genetic gain
GEBV-O	5571.61	6468.60	896.99
GD-O-30	5452.39	6488.02	1035.63
GD-O-50	5436.58	6484.58	1048.00
GD-O-100	5289.74	6540.72	1250.98
GEBV-GD-30	5538.44	6501.23	962.79
GEBV-GD-50	5522.45	6482.13	959.68
GEBV-GD-100	5454.37	6535.79	1081.42
PH			
	$\overline{GEBV}_P$	$\overline{GEBV}_{F_{10}}$	genetic gain
GEBV-O	97.75	85.89	-11.86
GD-O-30	102.20	87.59	-14.61
GD-O-50	103.66	89.99	-13.67
GD-O-100	106.83	91.85	-14.98
GEBV-GD-30	99.00	86.01	-12.99
GEBV-GD-50	99.39	85.99	-13.40
GEBV-GD-100	101.15	86.13	-15.02
FT			
	$\overline{GEBV}_P$	$\overline{GEBV}_{F_{10}}$	genetic gain
GEBV-O	83.14	77.84	-5.30
GD-O-30	83.98	78.73	-5.25
GD-O-50	84.57	78.19	-6.38
GD-O-100	85.62	78.39	-7.23
GEBV-GD-30	83.44	77.90	-5.54
GEBV-GD-50	83.69	77.76	-5.93
GEBV-GD-100	84.16	77.89	-6.27

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601 (i)  $\overline{GEBV}_P$ : the GEBV average among the 10 selected parental lines.  $\overline{GEBV}_{F_{10}}$  : the

602 GEBV average among the resulting 2700 F<sub>10</sub> RILs.  
603 (ii) GEBV-O: the subset of the top 10 accessions with the minimal or maximal GEBVs;  
604 GD-O-30, -50, -100: the subsets of 10 accessions with the maximal D-scores chosen  
605 from the candidate sets composed of the top 30, 50, and 100 accessions, respectively;  
606 GEBV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen  
607 from the remainder of the candidate sets composed of the top 30, 50, and 100 accessions,  
608 respectively, which have the maximal D-scores.  
609 (iii) YLD: yield; PH: plant height; FT: flowering time.

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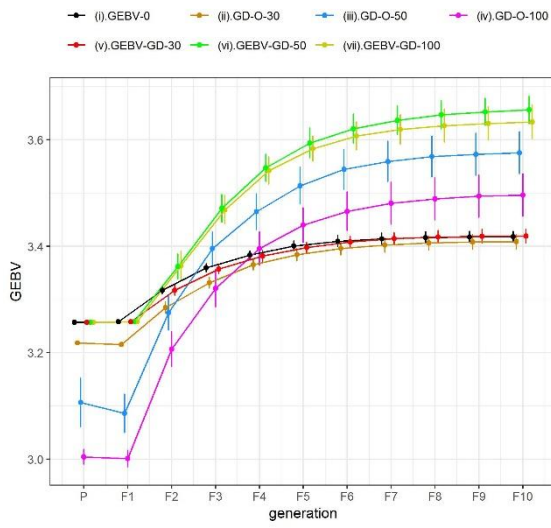
622 Figure 1: The working flow for the Monte Carlo simulation.

623 GEBV: genomic estimated breeding value; GBLUP: genomic best linear unbiased

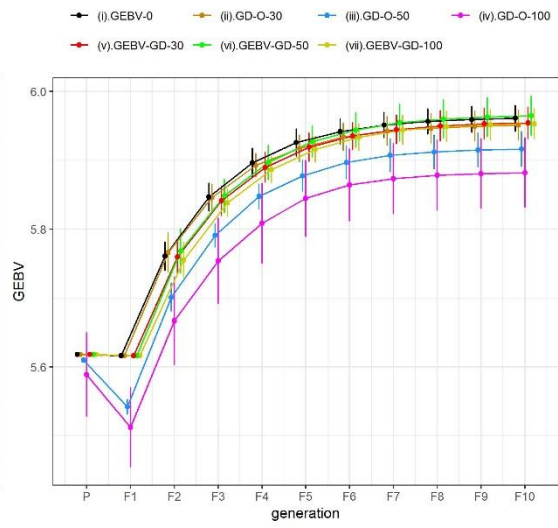
624 predictor; RIL: recombinant inbred line.

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BRSW (the larger the better)

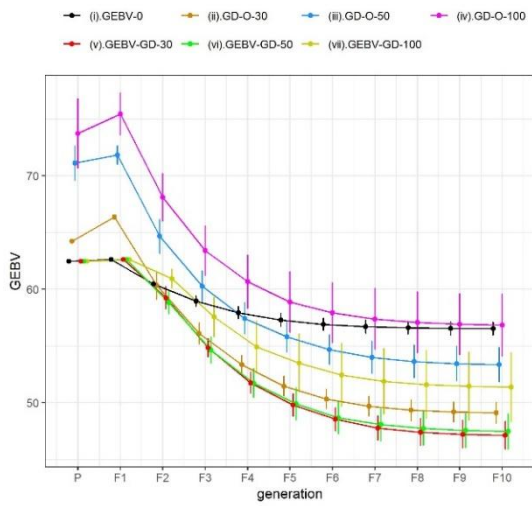


FPP (the larger the better)

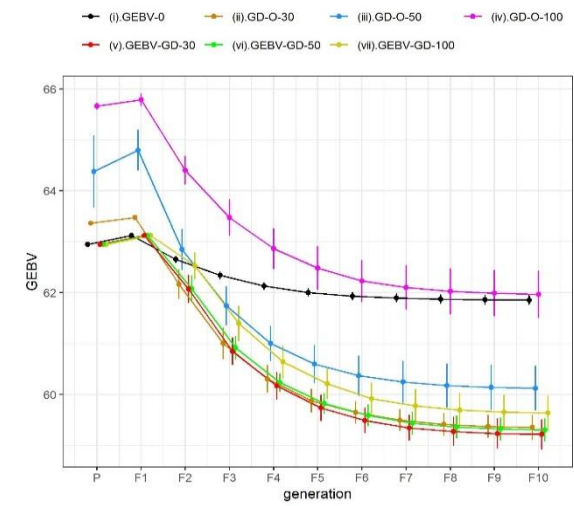


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FTAA (the smaller the better)

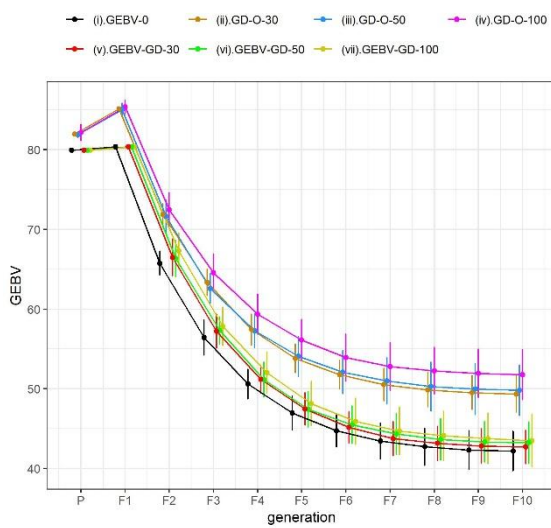


FTAF (the smaller the better)

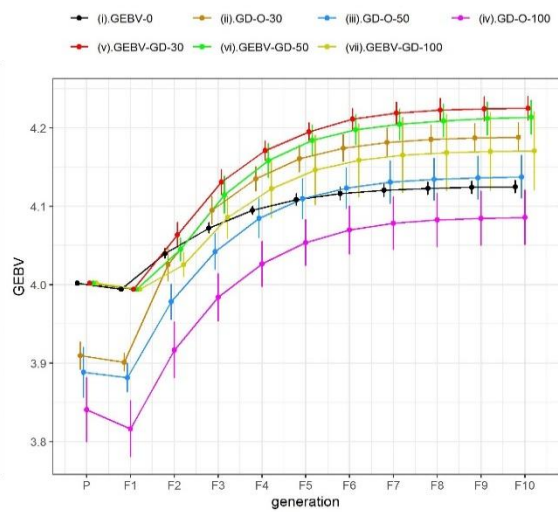


627

PH (the smaller the better)



PNPP (the larger the better)



628

629 Figure 2: The GEBV averages for the best individuals from the 30 repetitions at  
630 consecutive generations for the six chosen traits in Dataset I.

631 (i) GEBV-O: the subset of the top 10 accessions with the minimal or maximal GEBVs;  
632 GD-O-30, -50, -100: the subsets of 10 accessions with the maximal D-scores chosen  
633 from the candidate sets composed of the top 30, 50, and 100 accessions, respectively;  
634 GEBV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen  
635 from the remainder of the candidate sets composed of the top 30, 50, and 100 accessions,  
636 respectively, which have the maximal D-scores.

637 (ii) BRSW: brown rice seed width; FPP: florets per panicle; FTAA: flowering time at  
638 Arkansas; FTAF: flowering time at Faridpur; PH: plant height; PNPP: panicle number  
639 per plant.

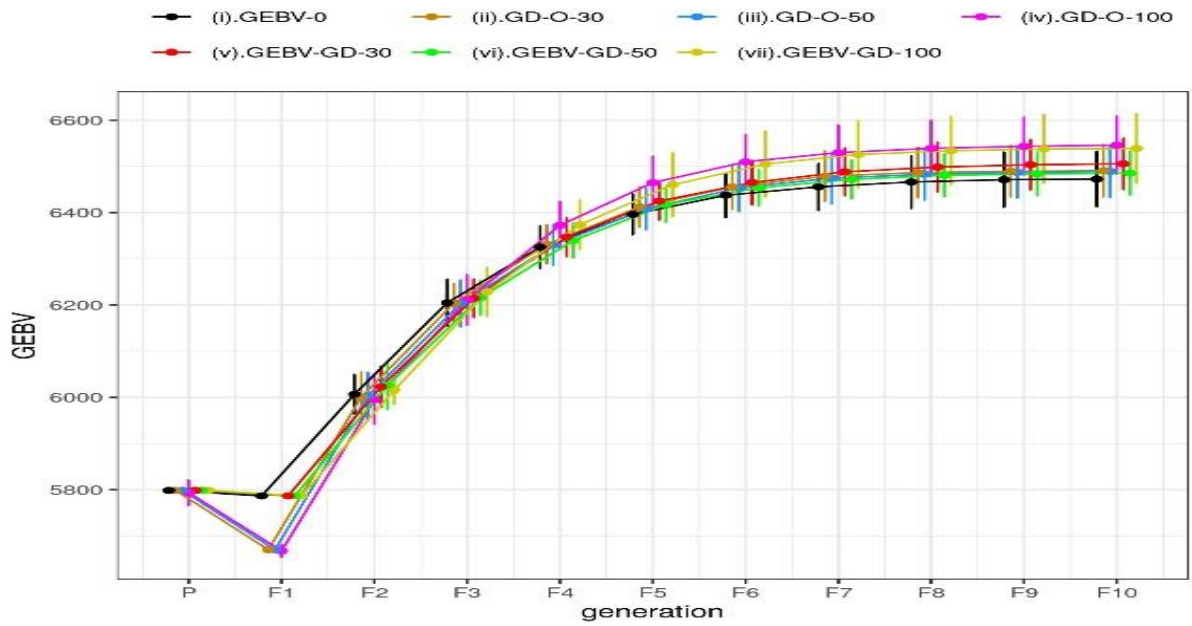
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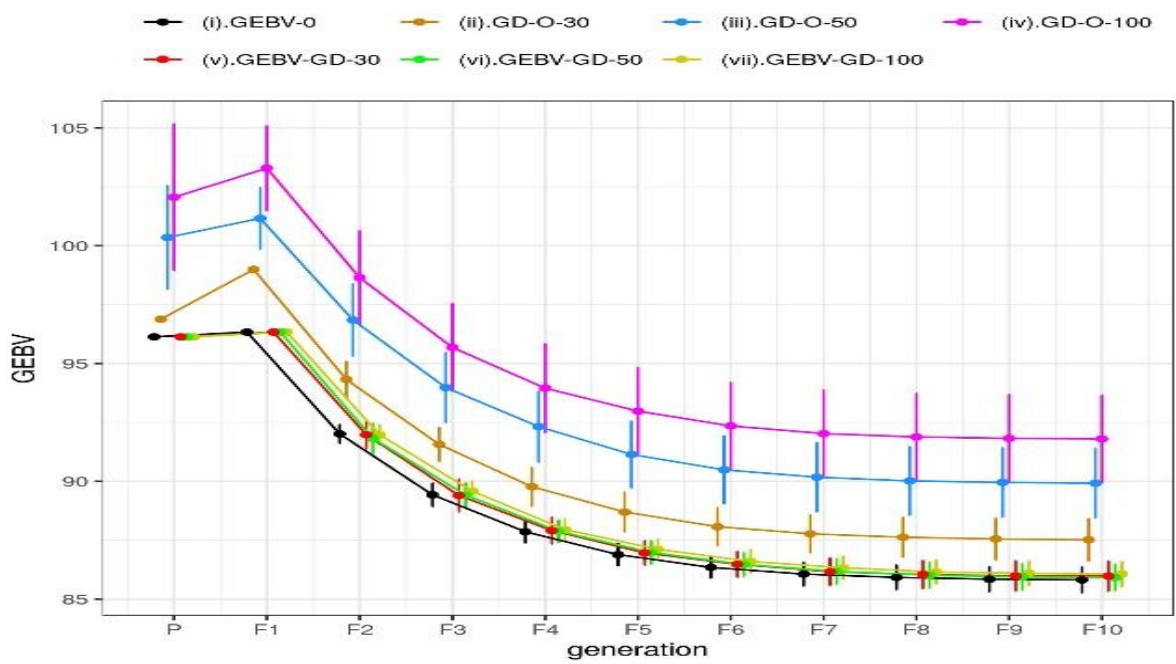
YLD. (the larger the better)



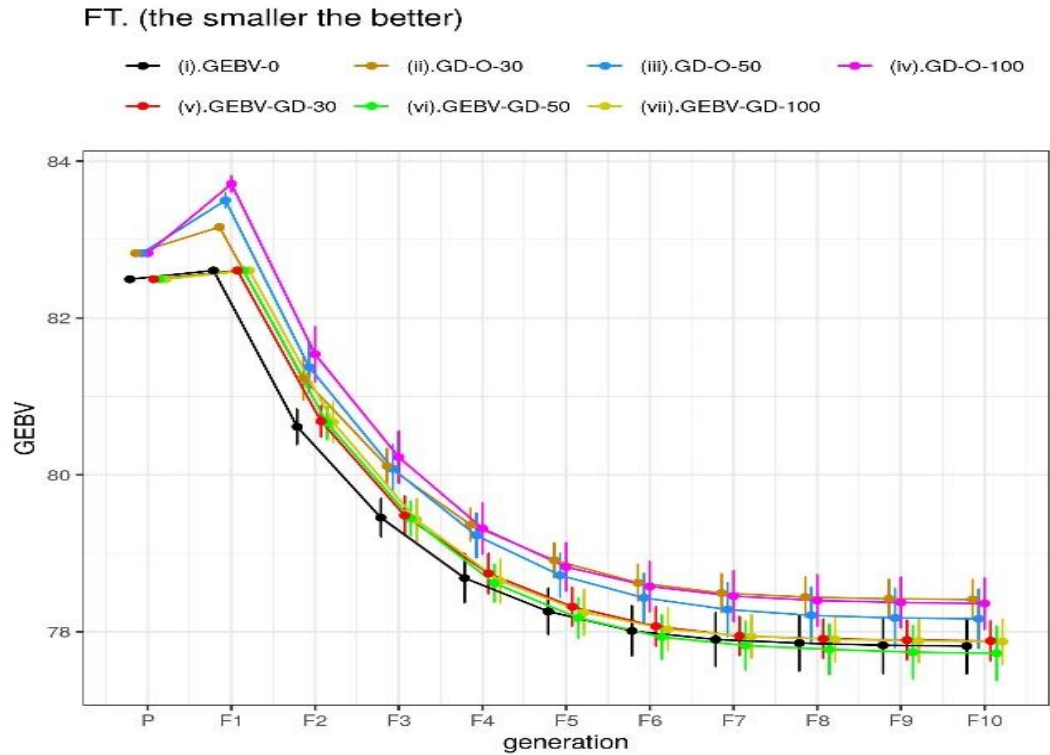
644

645

PH. (the smaller the better)



646



647

648 Figure 3: The GEBV averages for the best individuals from the 30 repetitions at  
 649 consecutive generations for the three target traits in Dataset II.

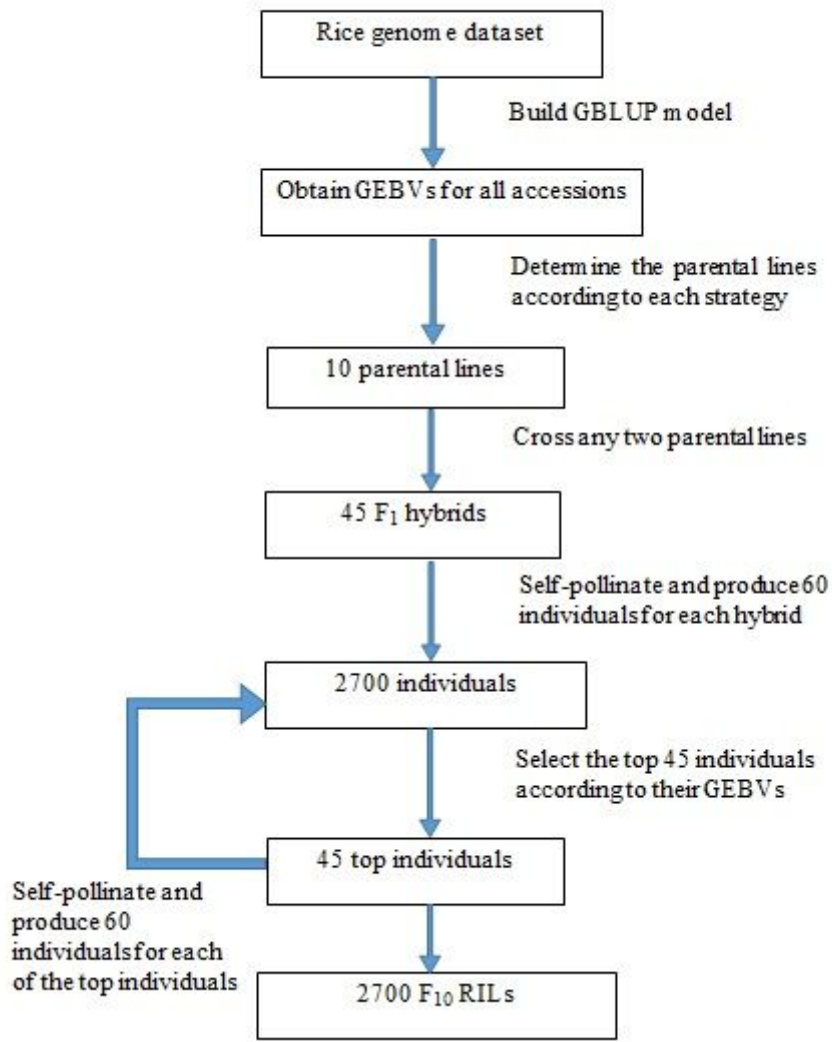
650 (i) GEBV-O: the subset of the top 10 accessions with the minimal or maximal GEBVs;  
 651 GD-O-30, -50, -100: the subsets of 10 accessions with the maximal D-scores chosen  
 652 from the candidate sets composed of the top 30, 50, and 100 accessions, respectively;  
 653 GEBV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen  
 654 from the remainder of the candidate sets composed of the top 30, 50, and 100 accessions,  
 655 respectively, which have the maximal D-scores.

656 (ii) YLD, yield; PH, plant height; FT, flowering time.

657

658

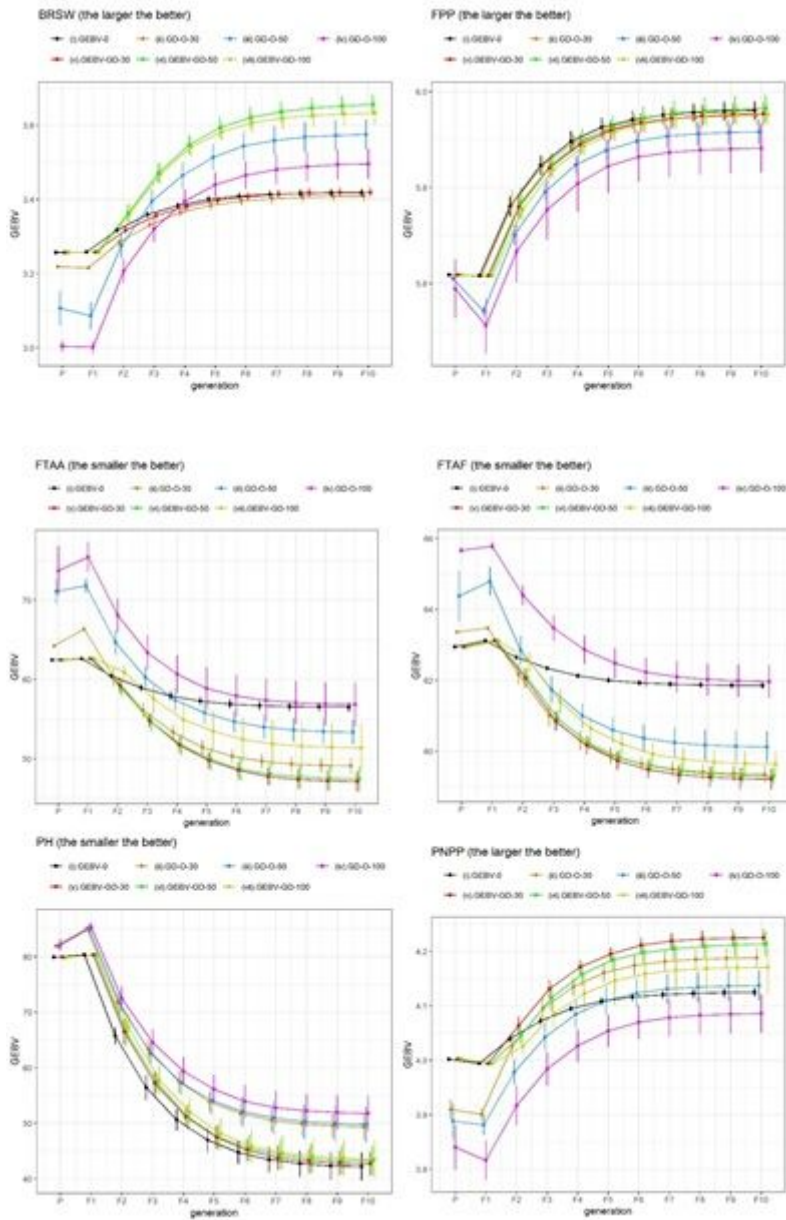
# Figures



**Figure 1**

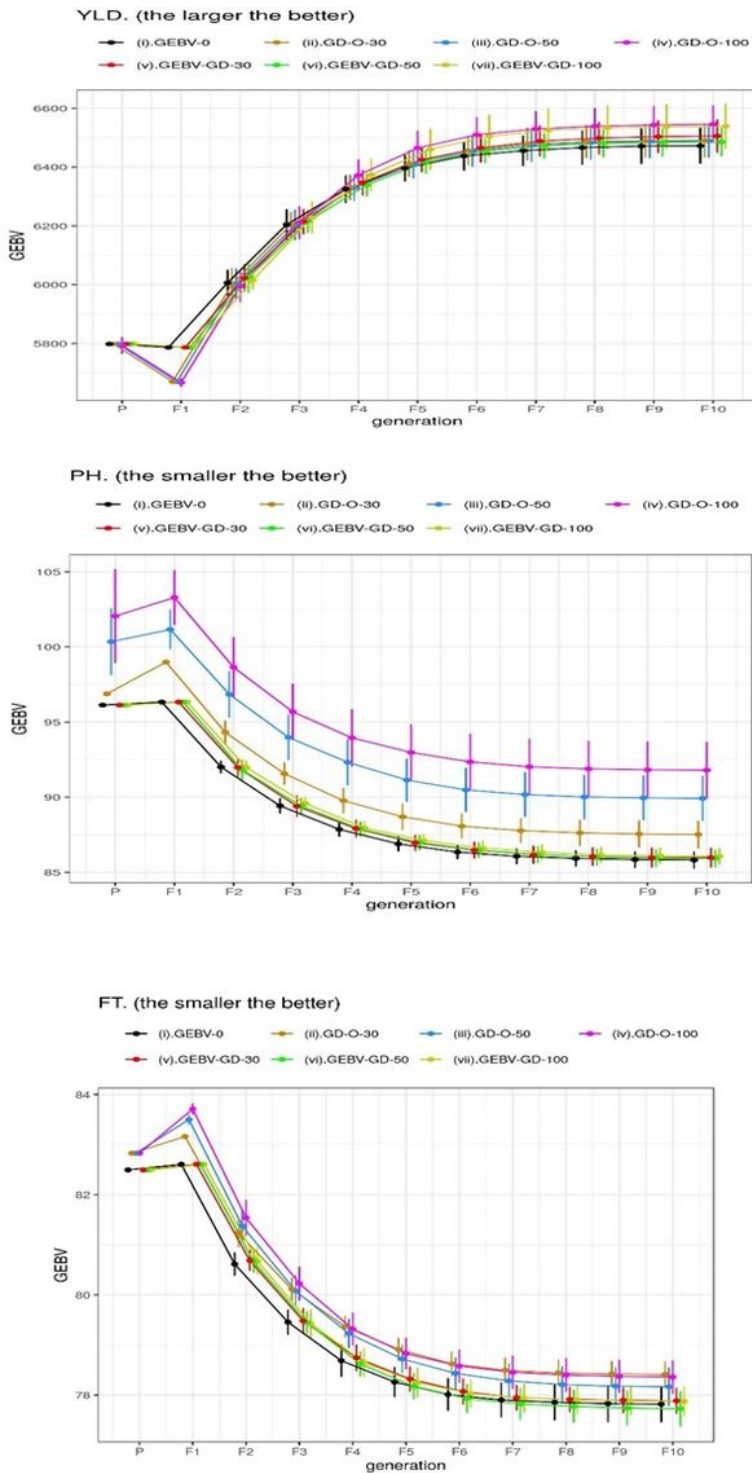
The working flow for the Monte Carlo simulation. GEBV: genomic estimated breeding value; GBLUP: genomic best linear unbiased predictor; RIL: recombinant inbred line.





**Figure 2**

The GEV averages for the best individuals from the 30 repetitions at consecutive generations for the six chosen traits in Dataset I. (i) GEV-O: the subset of the top 10 accessions with the minimal or maximal GEVs; GD-O-30, -50, -100: the subsets of 10 accessions with the maximal D-scores chosen from the candidate sets composed of the top 30, 50, and 100 accessions, respectively; GEV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen from the remainder of the candidate sets composed of the top 30, 50, and 100 accessions, respectively, which have the maximal D-scores. (ii) BRSW: brown rice seed width; FPP: florets per panicle; FTAA: flowering time at Arkansas; FTAF: flowering time at Faridpur; PH: plant height; PNPP: panicle number per plant.



**Figure 3**

The GEBV averages for the best individuals from the 30 repetitions at consecutive generations for the three target traits in Dataset II. (i) GEBV-0: the subset of the top 10 accessions with the minimal or maximal GEBVs; GD-O-30, -50, -100: the subsets of 10 accessions with the maximal D-scores chosen from the candidate sets composed of the top 30, 50, and 100 accessions, respectively; GEBV-GD-30, -50, -100: the subsets of the top 2 accessions plus 8 accessions chosen from the remainder of the candidate

sets composed of the top 30, 50, and 100 accessions, respectively, which have the maximal D-scores. (ii)  
YLD, yield; PH, plant height; FT, flowering time.