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- 2 **Title:** Validation of Extreme Ultraviolet Emission Spectra During Solar Flares
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15 **Abstract**

16 X-rays and extreme ultraviolet (EUV) emissions from solar flares rapidly change the
17 physical composition of the Earth's thermosphere and ionosphere, thereby causing
18 space weather phenomena such as communication failures. To predict the effects of
19 flare emissions on the Earth's upper atmosphere, numerous empirical and physical
20 models have been developed. We verify the extent of reproducing the flare emission
21 spectra using a one-dimensional hydrodynamic calculation and the CHIANTI atomic
22 database. To verify the proposed model, we use the observed EUV spectra obtained by
23 the extreme ultraviolet variability (EVE) on board the Solar Dynamics Observatory
24 (SDO). We examined the "EUV flare time-integrated irradiance" and "EUV flare line
25 rise time" of the EUV emissions for 21 events by comparing the calculation results of
26 the proposed model and observed EUV spectral data. The proposed model succeeded in
27 reproducing the EUV flare time-integrated irradiance of the Fe VIII 131 Å, Fe XVIII 94
28 Å, and Fe XX 133 Å, as well as the 55 to 355 Å and 55 to 135 Å bands. For the EUV
29 flare line rise time, there was acceptable correlation between the proposed model
30 estimations and observations for all Fe flare emission lines. These results demonstrate

that the proposed model can reproduce the EUV flare emission spectra from the emitting plasma with relatively high formation temperature. This indicates that the physics-based model is effective for the accurate reproduction of EUV spectral flux.

Keywords

Solar flare, X-ray emission, EUV emission, Space weather

Main Text

1. Introduction

To freely utilize outer space as a place for deploying advanced space activities, a common fundamental system, called space infrastructure, is required. To build and use a space infrastructure safely, it is important to accurately grasp the current state of the solar-terrestrial environment, which is strongly influenced by solar activities. Among the solar activities, solar flares have the greatest influence on the solar-terrestrial environment. When solar flares occur, powerful electromagnetic radiation and large amounts of high-energy particles are released. Among these, it is well known that the

47 X-ray and extreme ultraviolet (EUV) emissions of the solar flares, in particular,
48 influence the Earth's communication network. When X-ray and EUV emissions from
49 solar flares reach the Earth's upper atmosphere, especially the D layer of the ionosphere,
50 oxygen and nitrogen in the D layer are ionized. Consequently, the electron density in
51 the D layer increases rapidly, and radio waves (especially at high-frequency ranges)
52 propagating through the D layer are absorbed. This phenomenon is called the Dellinger
53 phenomenon (Dellinger 1937), which is widely known as one of the sudden ionospheric
54 disturbances (SIDs). Solar flare emissions reach the Earth in approximately 8 min, and
55 the lead time from solar flare to SIDs is extremely short. Therefore, it is important that
56 the solar irradiance, especially X-ray and EUV emissions, be constantly monitored to
57 minimize the adverse effects of SIDs.

58 In general, it is considered that SIDs are caused by the occurrence of solar flares of the
59 M-class or higher, and can be predicted using the flare class. However, it has been
60 reported that SIDs have occurred from C-class flare, and have not occurred from
61 X-class flares. These observational results suggest that the flare emission contributing to
62 the occurrence of SIDs is not necessarily proportional to the X-ray intensity. To verify

63 what solar flare emission wavelengths influence the occurrence of SIDs, the
64 observational data of the full solar flare emission spectrum is required. However, the
65 spectral observations of EUV and X-ray emissions, which are considered to
66 significantly contribute to SIDs, are limited.

67 X-ray emission has been continuously observed since 1974 by the X-ray Sensors (XRS)
68 on board the Geostationary Operational Environmental Satellite (GOES). GOES/XRS
69 observes two wavelength bands, 0.5 to 4 Å (GOES XRS-A) and 1 to 8 Å (GOES
70 XRS-B) (Bornmann et al. 1996).

71 EUV emission has been observed by different instruments because of its importance
72 form space weather forecasting. The Solar and Heliospheric Observatory (SOHO)
73 satellite, which launched in December 1995, has a Solar EUV Monitor (SEM) (Judge et
74 al. 1998). This instrument has been observing EUV emissions with a 15 s time
75 resolution since January 1996. However, SOHO/SEM only has two wavelength bands,
76 260 to 340 Å and 1 to 500 Å, without wavelength resolution. Hence, only the temporal
77 variation of these EUV emissions can be known from the SOHO/SEM data. The
78 Thermosphere Ionosphere Mesosphere Energetics and Dynamics (TIMED) satellite,

79 which launched in December 2001, has an EUV observation instrument called the Solar
80 EUV Experiment (SEE) (Woods et al. 2005). TIMED/SEE has been observing the
81 wavelength range of 1 to 1940 Å with a 4 Å resolution since January 2002 and has
82 superior spectral resolution compared to SOHO/SEM. However, the time resolution of
83 this is approximately one day, and as such, short-term fluctuations such as solar flares
84 cannot be followed. The Solar Dynamics Observatory (SDO) satellite launched on
85 February 2010 includes the Extreme Ultraviolet Variability Experiment (EVE) (Woods
86 et al. 2012). The Multiple EUV Grating Spectrograph (MEGS), a subsystem of the
87 SDO/EVE, has measured full disk solar irradiance in the 1 to 1060 Å range with 1 Å
88 spectral resolution and a 10 s time cadence since May 2010. MEGS-A observes the
89 wavelength range 50 to 370 Å, and MEGS-B observes the wavelength range 350 to
90 1050 Å. MEGS-A was the only instrument that could observe throughout the day with
91 sufficient spectral and temporal resolution to study the EUV flare emission spectra;
92 however, this device was terminated in May 2014 owing to a charge-coupled device
93 (CCD) power anomaly. Although MEGS-B remains in operation today, it is possible
94 that a flare is not observed because MEGS-B can only operate for approximately three

hours a day. Therefore, the observation of high-resolution EUV emission spectra when a solar flare occur is not guaranteed.

To model the emission spectra, we must understand the emission mechanism in solar flares. The basic conceptual model for solar flares is the CSHKP model (Carmichael 1964; Sturrock 1966; Hirayama 1974; Kopp & Pneuman 1976; Yokoyama & Shibata 1998; Shiota et al. 2005). According to this model, solar flares are caused by “magnetic reconnection” generated in the solar corona (Innes et al. 2003; Imada et al. 2013; Warren et al. 2018). The strong magnetic tension generated by the magnetic reconnection heat accelerates the electrons or protons in the solar corona. The accelerated particles travel downward along the magnetic field lines, fall into the chromosphere, and rapidly heat the high-density plasma. The high-temperature and high-density plasmas rise from the chromosphere along the magnetic field lines and form a loop-shaped structure; this phenomenon is called “chromospheric evaporation” (Milligan & Dennis 2009; Imada et al. 2015; Lee et al. 2017). The loop structure observed by soft X-ray and EUV formed from chromospheric evaporation is called the “flare ribbon”. Soft X-ray and EUV emissions are emitted from the flare loop. The time

111 evaporation of the EUV emissions is characterized by the formation temperature of the
112 emitting plasmas. A typical flare light curve of an EUV emission has as impulsive peak
113 at the beginning, followed by a gradual peak, called the impulsive and gradual phases,
114 respectively. In general, the relatively cooler EUV line emissions from the plasma
115 below the transition region are observed in the impulsive phase corresponding to the
116 rapid heating in the early stages of chromospheric evaporation, and hotter EUV line
117 emissions are observed in the gradual phase corresponding to the radiative cooling of
118 the flare loop. Therefore, the emission spectra are evidently different between the
119 impulsive and gradual phases because their origins are different.

120 Different flare EUV emission prediction models have been constructed based on the
121 above flare emission mechanism. The most widely used model is the Flare Irradiance
122 Spectral Model (FISM) (Chamberlin et al. 2006, 2007, 2008). The FISM is an empirical
123 model that derives EUV emission spectra using the GOES soft X-ray flux observation.
124 The FISM estimates the wavelength range of 1 to 1900 Å with 10 Å spectral resolution
125 and 60 s cadence. It has been reported that the FISM can accurately estimate the solar
126 flare emission spectra within 40% for a wavelength in the range 140 to 1900 Å.

127 However, FISM has low accuracy on wavelengths less than 140 \AA ; this is the
128 wavelength range containing the EUV emission lines that are mainly enhanced during
129 the gradual phase of a flare. This is because the FISM considers the time evolution of all
130 EUV line emissions to be the same as the time evolution of the soft X-ray during the
131 flare, and the cooling of the flare loop (time difference of EUV line emissions) is not
132 well represented. Consequently, the FISM underpredicts the flare duration and
133 deposited energy (Thiemann et al. 2017).

134 The Q_{EUV} , for which the 0 to 450 \AA EUV band is an important indicator for the EUV
135 irradiance input to the Earth's upper atmosphere (Strickland 1995), and the EUV
136 irradiance in the 0 to 70 \AA and 70 to 170 \AA bands have the greatest contribution to the
137 Q_{EUV} (Woods et al. 2011). Therefore, EUV irradiance from wavelengths less than 140
138 \AA is important. To solve this discrepancy, it is necessary to estimate the time evolution
139 of the EUV emissions accurately.

140 Other physics-based models have been constructed for this purpose; however, the EUV
141 emission was only partially reproduced (Li et al. 2014; Zeng et al. 2014). Thiemann et
142 al. (2017) partially succeeded in modeling the timing to coronal loop cooling with an

143 empirical rule. These studies used a zero-dimensional hydrodynamic model to simulate
144 the thermal evolution of the coronal loops, called the enthalpy-based thermal evolution
145 of loops (EBTEL) model, that could calculate the temperature and density in the flare
146 loop without calculating the spatial loop evolution (Klimchuk et al. 2008; Cargill et al.
147 2012). The EBTEL model did not calculate the spatial distribution of the emitting
148 plasma in the flare loop; hence, it is possible that the emission from the transition region
149 plasma would not be reproduced accurately (Kawai et al. 2020). Kawai et al. (2020)
150 introduced a new method for reproducing EUV flare emission spectra considering the
151 time evolution of the plasma distribution in the flare loop. This method was constructed
152 using a one-dimensional hydrodynamic calculation and an atomic database. The details
153 of the method are described in detail in Section 2.

154 In this paper, we present the statistical results of the EUV emission spectra observed by
155 SDO/EVE for 21 flare events and compare these with the spectra reproduced by Kawai
156 et al. (2020)'s method. The purpose of this study is to investigate the accuracy in
157 reproducing solar flare emission spectra using a simple method based on the physics of
158 flare loops and to examine the important parameters for reproducing the solar flare

159 emissions.

160 The remainder of the paper consists of following sections. Section 2 presents the
161 extraction of the comparative parameters using GOES and SDO/EVE. Section 3
162 introduces the models used in this study. Section 4 presents an example of the
163 derivation of the solar flare emission spectra using the proposed model. Section 5
164 presents the statistical results of the comparison between the proposed model
165 simulations and observations and verifies the solar flare emission spectra. Section 6
166 discusses and summarizes the presented comparison results.

167

168 **2. Data**

169 **2.1 Soft X-ray observation**

170 we used the soft X-ray data observed by the GOES/XRS. Flare class and duration are
171 typically determined with GOES XRS-B light curve observations. In this study, the
172 flare start, peak, and end times were defined using the time derivative data of the GOES
173 XRS-B light curve observations to not lose the impulsive and gradual phases.
174 Furthermore, we divided the flare duration into the rise time and decay time to

175 investigate the flare evolution in detail. Figure 1 displays an example of determining the
176 rise time and decay time for the M9.9-class flare on January 1, 2014. The rise time is
177 determined by when the positive derivative value is observed continuously from the
178 GOES XRS-B start time to the peak time. The decay time is determined by when the
179 negative derivative value is observed continuously from the GOES XRS-B peak time to
180 the end time.

181 **2.2 EUV flare emission spectra observation**

182 we examined the EUV emission spectra obtained from the SDO/EVE MEGS-A
183 observations. For this study, we selected flare events greater than M3-class flare that
184 occurred between November 2010 and May 2014 from the Hinode flare catalogue
185 (Watanabe et al. 2012). We used 21 events observed by the SDO/EVE MEGS-A during
186 this period.

187 Figure 2 displays the EUV spectrum at flare peak time (18:52 UT) for the M9.9-class
188 flare on January 1, 2014 observed by the SDO/EVE MEGS-A. This EUV spectrum was
189 subtracted from the spectral value of each wavelength before the flare as the
190 background. We focused on the six EUV flare lines of Fe VIII 131 Å, Fe XV 284 Å, Fe

191 XVI 335 Å, Fe XVIII 94 Å, Fe XX 133 Å, and He II 304 Å, which were strongly
192 enhanced during the flare. The formation temperature of the Fe XX 133 Å is ~ 9 to 13
193 MK, Fe XVIII 94 Å is ~ 6 MK, Fe XVI 335 Å is ~ 3 MK, Fe XV 284 Å is ~ 2 MK, Fe
194 VIII 131 Å is ~ 0.4 MK, and He II 304 Å is ~ 0.05 MK. Figure 3 displays the EUV light
195 curves of these six flare lines during M9.9-class flare on January 1, 2014. We subtracted
196 3 min, the average value, from before the flare of each line flux as the background, and
197 used 110 s as the running average to remove the noise due to short term fluctuations
198 (dashed line in Figure 3).

199 To investigate the flare deposited energy and duration, which have a significant
200 influence on the Earth's thermosphere and ionosphere response (Qian et al. 2011), we
201 extracted the "EUV flare time-integrated irradiance" and the "EUV flare line rise time"
202 as comparison parameters.

203 The EUV flare time-integrated irradiance is the time-integrated value of the irradiance
204 from the flare start to end time. We examined for EUV flare lines 55 to 355 Å and 55 to
205 135 Å band. The wavelength band of 55 to 135 Å, where the uncertainty of the FISM
206 calculation is considerable and significantly influences the Earth's ionosphere (Woods

et al. 2011; Thiemann et al. 2017). This relatively short wavelength band consists of the hot EUV lines and dominates the EUV emissions in the gradual phase (Woods et al. 2011). The EUV flare rise time is the duration from the flare start to EUV line peak time as with the above mentioned soft X-ray observation.

3. Models

3.1 Coordinated Astronomical Numerical Software (CANS) 1D package

We used the one-dimensional hydrodynamic model called CANS 1D package (<http://www-space.eps.s.u-tokyo.ac.jp/~yokoyama/etc/cans/index-e.html>) to solve the physical process of the plasma in the flare loop. This package can calculate the energy redistribution process in the flare loop that occurs after the energy input. CANS 1D simulates one-dimensional fluid motion and energy transfer along an invariant magnetic loop. It assumes that the cross section of the magnetic loop does not change in time. The fluid was considered as non-viscous and compressible and included heat conduction and radiative cooling. Gravity was also considered. The fundamental equations of CANS 1D are as follows:

$$\frac{\partial}{\partial t}(\rho S) + \frac{\partial}{\partial x}(\rho V_x S) = 0 \quad (1)$$

$$\frac{\partial}{\partial t}(\rho V_x S) + \frac{\partial}{\partial x}[(\rho V_x^2 + p)S] = \rho g S \quad (2)$$

$$\frac{\partial}{\partial t} \left[\left(\frac{p}{\gamma - 1} + \frac{1}{2} \rho V_x^2 \right) S \right] + \frac{\partial}{\partial x} \left[\left(\frac{\gamma}{\gamma - 1} p + \frac{1}{2} \rho V_x^2 \right) V_x S - \kappa \frac{\partial T}{\partial x} S \right] = (\rho g V_x + H - R + H_f) S \quad (3)$$

$$p = \frac{k_B}{m} \rho T \quad (4)$$

223 where ρ is the plasma density, S is the cross section, V_x is the plasma velocity,

224 g is the gravitational acceleration, $\gamma = 5/3$ is the specific heat ratio, κ is the

225 thermal conductivity coefficient, H is the static heating, R is the radiative

226 cooling, H_f is the flare heating term, k_B is the Boltzmann constant, and m is

227 the mean particle mass. The Spitzer model was used as the thermal conductivity

228 coefficient (Spitzer 1962). The calculation region is from the foot point of the

229 flare loop, which means the photosphere ($x = 0$) to the flare loop top ($x = L$),

230 where L is the half-loop length.

231 Flare heating is given as a function of time and space, as follows:

$$H_f = H_{f0} \cdot q(t) \cdot f(x) \quad (5)$$

$$q(t) = \frac{1}{4} \left\{ 1 + \tanh \frac{t}{0.1\tau_0} \right\} \left\{ 1 - \tanh \frac{t - \tau_f}{0.1\tau_0} \right\} \quad (6)$$

$$f(x) = \frac{1}{\sqrt{2\pi}} \exp \left[-\frac{(x - L)^2}{2w_f^2} \right] \cdot \frac{1}{2} \left\{ 1 + \tanh \left(\frac{x - 20\mathcal{H}_0}{3\mathcal{H}_0} \right) \right\} \quad (7)$$

232 where H_{f0} is the input energy, τ_f is the heating duration, and w_f is the
233 heating width. \mathcal{H}_0 is the scale height at the photosphere ($x = 0$).
234 **3.2 CHIANTI atomic database**
235 We used the CHIANTI atomic database to reproduce the X-ray and EUV
236 emissions originating from the flare loop. The CHIANTI database contains a
237 large amount of atomic data for the analysis of astrophysical spectra including
238 atomic energy levels, wavelengths, radiative transition probabilities, rate
239 coefficients for ionization, and data to calculate different emissions (Dere et al.
240 1997).

241

242 **4. Validation of M9.9-class flare on January 1, 2014**

243 We compared the EUV flare time-integrated irradiance and EUV flare line rise
244 time obtained from the proposed model and SDO/EVE MEGS-A observations.
245 The model simulations were in accordance with Kawai et al. (2020).

246 **4.1 Preprocessing**

247 As a preparation to simplify the derivation of the EUV emission spectrum, the

248 rise and decay time were fit to exponential curves using the Gauss-Newton
249 method. Figure 4 displays an example of the fit GOES XRS-B light curve for the
250 M9.9-class flare on January 1, 2014.

251 **4.2 Coronal loop length measurement**

252 The flare loop length for the parameter used in CANS 1D was estimated by the
253 observation of the separation distance of the ribbons, called ribbon distance, with
254 the SDO/Atmospheric Imaging Assembly (AIA) (Lemen et al. 2012). We used
255 1600 Å images to obtain the ribbon distance immediately before the flare start.
256 Before deriving the ribbon distance, we corrected the projection effect by
257 rotating the flaring region to the solar center using the solar software
258 drot_map.pro. First, we defined the flare ribbon as a region with intensities of 40
259 times greater than the standard deviation of the quiet region. Ribbon distance is
260 derived as the distance between the two brightest points in the flare ribbons and
261 is known as the $H\alpha$ (UV) kernel (Asai et al. 2003; Temmer et al. 2007). For the
262 M9.9-class flare on January 1, 2014, as indicated in Figure 5, the ribbon distance
263 was derived as 23.3 arcsec. Therefore, the ribbon distance of this event was

estimated to be 16.9 Mm. Subsequently, the loop length was estimated to be 26.5

Mm by assuming a semicircle whose diameter was this ribbon distance.

4.3 Numerical simulation

We reproduced the time evolution of the plasma in the flare loop with CANS 1D

as described in Section 3.1. Figure 6 displays an example of the calculated results

of CANS 1D. In this case, we set L to 26.5 Mm, H_{f0} was $6.0 \text{ erg cm}^{-3} \text{ s}^{-1}$,

w_f was 600 km, and τ_f was 240 s (Equations (5) - (7)). From the result, we

identified the transition region to be near 0.3 Mm. In the figure, the temperature

and density in the flare loop rise sharply in a couple of hundred seconds and at a

height of 0.3 Mm, and the edge moves temporally. This represents the evolution

of chromospheric evaporation. When flare occurs, accelerated particles fall on

the chromosphere along the magnetic field lines. Consequently, the low

temperature plasma in the chromosphere is rapidly heated and transported

upward owing to the pressure gradient. Hence, this calculation can reproduce the

time evolution of the plasma in the flare loop.

4.4 Conversion from GOES X-ray to EUV spectrum

280 We combined the CANS 1D result with the CHIANTI atomic database version
281 9.0 (Dere et al. 2019) to derive the synthetic flare emissions. Finally, we
282 converted the synthetic flare emissions into a light curve that was comparable to
283 the observation. Figure 7 displays the reproduced GOES XRS-B light curve by
284 the proposed model. We performed the conversion as follows using the fit GOES
285 XRS-B light curve as described above. First, we calculated the ratio between the
286 GOES XRS-B observation and simulated GOES XRS-B light curve (integrated
287 calculated value of 1 to 8 Å) for each observation time. Afterwards, we
288 performed convolution on the simulated GOES XRS-B light curve with the
289 observation. Subsequently, we calculated the ratio between the maximum value
290 of the GOES XRS-B observation and maximum value of the convoluted GOES
291 XRS-B light curve. We applied these two ratios to all simulated light curves.
292 Finally, we derived the EUV emission spectra in all wavelengths that was
293 comparable to the observation (see the Fig. 1 in Kawai et al. (2020)).
294 Figure 8 displays an example of the EUV flare time-integrated spectra during the
295 M9.9-class flare on January 1, 2014. The dashed red, blue, and solid green lines

296 indicate the values obtained from the proposed model, FISM, and SDO/MEGS-A
297 observations, respectively. As indicated in Figure 8, both the proposed model and
298 FISM reproduced the tendency of the observed values. Owing to the superior
299 wavelength resolution, the proposed model reproduced each EUV flare line,
300 which was not represented by the FISM. Figure 9 displays the light curves of the
301 EUV flare lines observed by SDO/EVE MEGS-A (top panel), estimated by the
302 proposed model (middle panel), and the FISM (bottom panel) for the M9.9-class
303 flare on January 1, 2014. The wavelength resolution of these light curves was 10
304 Å, which was the same as FISM. Therefore, the wavelength of Fe VIII and Fe
305 XX is 130 Å, Fe XV is 280 Å, Fe XVI is 330 Å, Fe XVIII is 90 Å, and He II is
306 300 Å as indicated in Figure 9. It is clear that the proposed model can reproduce
307 the flux of each line based on the formation temperature. Conversely, the light
308 curves of the FISM were virtually the same as the Fe XX observation of
309 SDO/EVE MEGS-A, regardless of the lines or events. Table 1 presents the EUV
310 flare time-integrated irradiance and EUV flare line rise time, observed by
311 SDO/EVE MEGS-A and calculated by the proposed model for the M9.9-class

312 flare on January 1, 2014, respectively.

313

314 **5. Statistical study for comparison between model and observation**

315 We compared the EUV flare time-integrated irradiance and EUV flare line rise
316 time obtained from the proposed model and SDO/EVE MEGS-A observation for
317 21 flare events using the same method as the event analysis in Section 4.

318 In this study, we used the default parameter values set in CANS 1D (see the
319 CANS 1D documentation). Afterwards, we set the optimal input energy for each
320 flare event as a variable parameter (see the equations (5) - (7)). The GOES
321 classes, flare dates, times, half-loop length estimations from the SDO/AIA
322 observation, and the input energy used in the proposed model for 21 flare events
323 are presented in Table 2.

324 First, we compared the flare time-integrated irradiance of each EUV line. Figure
325 10 displays the correlation of the EUV flare time-integrated irradiance of six
326 flare lines. All Fe lines have acceptable correlation with the observations.

327 However, the He II indicates poor correlation with the correlation coefficient of

0.24 (Figure 10f). As indicated in the regression lines in Figure 10, the Fe XVIII (Figure 10d) effectively reproduced the observed data. Fe XV (Figure 10b) and Fe XVI (Figure 10c) tended to be overestimated; the Fe VIII (Figure 10a), Fe XX (Figure 10e), and He II (Figure 10f) lines tended to be underestimated by the proposed model.

Afterwards, we compared the flare energies for two wavelength bands. Figure 11 displays the comparison results of the EUV flare time-integrated irradiance of two wavelength bands of 55 to 355 Å (Figure 11a) and 55 to 135 Å (Figure 11b). The results of the proposed model and FISM are plotted in red and blue, respectively. As indicated in Figure 11a, the 55 to 355 Å band was well reproduced by both the proposed model and FISM. The slopes of the regression lines were 0.81 ± 0.08 and 1.22 ± 0.02 , respectively, and the correlation coefficients were 0.92 and 0.99, respectively. Moreover, for the 55 to 135 Å band, the proposed model could reproduce the observations better than the FISM (Figure 11b). From Figure 11b, the slope of the regression line for the proposed model was 0.91 ± 0.08 , and the correlation coefficient was 0.94. Conversely, the

slope of the regression line for the FISM was 0.53 ± 0.01 , and the correlation coefficient is 0.99. From these results, the FISM tended to underestimate the EUV flare time-integrated irradiance at this relatively shorter wavelength band. Figure 12 displays the comparison results of the EUV flare line rise time statistically. The correlation coefficient of the Fe VIII was 0.95 (Figure 12a), Fe XV was 0.86 (Figure 12b), Fe XVI was 0.90 (Figure 12c), Fe XVIII was 0.92 (Figure 12d), Fe XX was 0.94 (Figure 12e), and He II was 0.80 (Figure 12f). It can be clearly observed that all Fe lines indicated acceptable correlations with the observations. From these scatter plots, the calculated rise time of Fe XV, Fe XVI, and Fe XX tended to be less than the observations (Figure 12b, c, e), whereas He II tended to be greater than the observations (Figure 12f).

6. Discussion and summary

We attempted to reproduce EUV flare emission spectra using a simple physics-based model that simulates the time evolution of emitting plasma distribution in the flare loop. We verified the EUV flare time-integrated

360 irradiance and EUV flare line rise time of EUV line emissions for 21 events by
361 comparing the calculation results of the proposed model and observed EUV
362 spectral data.

363 For the flare time-integrated irradiance, the proposed model succeeded in
364 reproducing the Fe VIII, Fe XVIII, and Fe XX lines (Figure 10a, d, e) as well as
365 the 55 to 355 Å and 55 to 135 Å band (Figure 11a). Our results indicate that the
366 physics-based model was effective in reproducing EUV flare irradiance for
367 wavelengths less than 140 Å. Conversely, the proposed model overestimated the
368 relatively longer wavelength lines, Fe XV and Fe XVI lines, emitted from
369 relatively cooler plasmas (Figure 10b, c). Thiemann et al. (2018) reported that
370 the peak EUV irradiance of emission lines with higher formation temperatures (>
371 9 MK) is proportional to the GOES XRS-B peak emission measure. Therefore,
372 our results could imply that the EUV irradiance of the emitting plasmas with a
373 lower formation temperature are not linearly proportional to the irradiance of the
374 hotter emission lines or soft X-ray flux.

375 Regarding the EUV flare line rise time, the proposed model could derive the time

376 evolution of the EUV line emission by simulating the time evolution of the
377 temperature in the flare loop. This tendency can be observed from the fact that
378 the difference of peak time depending on the formation temperature of the
379 emitting plasma was reproduced by the proposed model as indicated in Figure 9.
380 The Fe XX line, which was emitted from the highest formation temperature
381 plasma, had the shortest rise time (Figure 12d), and the He II line, which emitted
382 from the lowest formation temperature, had the longest rise time (Figure 12f).
383 This is because the time evolution of each EUV flare line is determined by the
384 temperature of the emitting plasma in the proposed model.
385 For the He II emission line, both the time-integrated irradiance (Figure 10f) and
386 EUV flare line rise time (Figure 12f) were poorly reproduced by the proposed
387 model. This is because the proposed model neglected the EUV emissions from
388 below the transition region, which is the origin of the optically thick plasmas,
389 and hence, we did not calculate the radiation transfer. The proposed model is
390 based primarily on the physical process following the soft X-ray emission.
391 Therefore, a future work is to construct a model that can accurately reproduce the

392 EUV emission from optically thick plasmas that are dominant in the impulsive
393 phase.

394 In this study, we used, for the most part, the default parameter values set in the
395 CANS 1D (see the CANS 1D documentation). Then, we used the half-loop
396 length estimated from observation, and set the optimal input energy for each flare
397 event as a variable parameter. These parameters are listed in Table 2. Our results
398 indicate that the EUV emissions from emitting plasma with relatively high
399 formation temperature could be reproduced using only the flare input energy as a
400 variable parameter.

401 As mentioned above, our results indicate that the physics-based model is
402 effective for reproducing EUV flare emissions. The proposed model succeeded
403 in reproducing not only the EUV emission intensity of Fe lines with high
404 formation temperature but also the time evolution of all Fe lines during a flare.

405 Because the Earth's ionosphere and thermosphere are sensitive to EUV emissions
406 from the Sun (Qian et al. 2011), an accurate estimation of the EUV irradiance
407 and duration during solar flares is important from the viewpoint of space weather.

408 Therefore, we consider that the simple model used in this study can contribute to
409 the space weather forecast operation.

410

411 **Declarations**

412 **Ethics approval and consent to participate**

413 No applicable

414 **Consent for publication**

415 No applicable

416 **List of abbreviations**

417 **AIA:** Atmospheric Imaging Assembly

418 **CANS:** Coordinated Astronomical Numerical Software

419 **CC:** Correlation Coefficient

420 **CCD:** Charge-Coupled Device

421 **EBTEL:** Enthalpy-Based Thermal Evolution of Loops

422 **EUV:** Extreme Ultraviolet

423 **EVE:** Extreme Ultraviolet Variability Experiment

424	FISM: Flare Irradiance Spectral Model
425	GOES: Geostationary Operational Environmental Satellite
426	MEGS: Multiple EUV Grating Spectrograph
427	SEE: Solar EUV Experiment
428	SEM: Solar EUV Monitor
429	SDO: Solar Dynamics Observatory
430	SIDs: Sudden Ionospheric Disturbances
431	SOHO: Solar and Heliospheric Observatory
432	TIMED: Thermosphere Ionosphere Mesosphere Energetics and
433	Dynamics
434	UV: ultraviolet
435	UT: universal time
436	XRS: X-ray Sensors
437	
438	Availability of data and materials
439	The SDO/EVE level 2 data version 6 data are available at

440 http://lasp.colorado.edu/eve/data_access/eve_data/products/level2/. FISM

441 data are available at https://lasp.colorado.edu/lisird/data/fism_flare_hr/.

442 The flare event data used in this study can be found in Hinode flare
443 catalogue (https://hinode.isee.nagoya-u.ac.jp/flare_catalogue/).

444 **Competing interests**

445 The authors declare that they have no competing interests.

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451 **Authors' contributions**

452 SN performed statistical study for solar flare spectrum data and drafted
453 the manuscript. KW, TK, SI and TK discussed the results and edited the
454 manuscript. All authors read and approved the final manuscript.

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556

557 **Figure legends Table Legends**

558 Figure 1. Example of GOES XRS-B observation.

559 The light curve of soft X-ray flux (1 to 8 Å) observed by the GOES XRS-B for the
560 M9.9-class flare on January 1, 2014 (upper panel). The light curve of the soft X-ray
561 time derivative flux (lower panel). The vertical dotted, solid, and dashed lines indicate
562 the flare start time, peak time, and end time, respectively.

563

564 Figure 2. Example of EUV spectrum observation.

565 The EUV spectrum at the GOES XRS-B peak time (18:52 UT) observed by the
566 SDO/EVE MEGS-A for the M9.9-class flare on January 1, 2014. This EUV spectrum is
567 subtracted from the value of each wavelength before the flare as the background. The

568 EUV flare lines focused on in this study are indicated as the vertical dotted lines.

569

570 Figure 3. Examples of EUV flare line light curves.

571 The light curves of each EUV flare line (Fe VIII, Fe XV, Fe XVI, Fe XVIII, Fe XX, and

572 He II from the top to bottom panels) observed by the SDO/EVE MEGS-A for the

573 M9.9-class flare on January 1, 2014. The solid lines indicate the observed values with

574 10 s cadence. The dotted lines indicate the 110 s running average values of the observed

575 data. The 3 min average values before the flare are subtracted from each light curve as

576 background. The vertical dotted, solid, and dashed lines indicate the flare start time,

577 peak time, and end time, respectively. The arrows indicate the peak time for each EUV

578 flare line.

579

580 Figure 4. Example of fit GOES XRS-B light curve for the M9.9-class flare on January 1,

581 2014.

582 The observed (red) and fit (green) light curves during the M9.9-class flare on January 1,

583 2014 using the Gauss-Newton method.

584

585 Figure 5. Example of flare ribbon observation.

586 The flare ribbon observation by the SDO/AIA 1600 Å for the M9.9-class flare on

587 January 1, 2014. The yellow contour indicates the region with an intensity 40 times

588 greater than the standard deviation of the quiet region. The red arrow indicates the

589 ribbon distance defined in this study.

590

591 Figure 6. Calculated results of CANS 1D.

592 The hydrodynamic calculation results with CANS 1D for (a) temperature distribution,

593 (b) density, (c) pressure, and (d) plasma velocity along the loop. The time evolution is

594 represented by the change of the line color from blue to red.

595

596 Figure 7. Observed and reproduced light curves of GOES XRS-A and XRS-B.

597 The dashed and solid lines indicate the reproduced and observed light curve of GOES

598 XRS during the M9.9-class flare on January 1, 2014, respectively. The red and blue

599 lines represent GOES XRS-B and XRS-A, respectively.

600

601 Figure 8. Example of EUV time-integrated spectra during flare.

602 The EUV time-integrated spectra during the flare for the M9.9-class flare on January 1,

603 2014. The dashed red, blue, and solid green lines indicate the calculated spectra of the

604 proposed model, FISM, and observed spectra by SDO/EVE MEGS-A, respectively. The

605 wavelength resolution for FISM is 10 Å; the proposed model and SDO/EVE MEGS-A

606 observation is 1 Å. The arrows indicate the EUV lines focused on in this study.

607

608 Figure 9. Example of EUV flare line light curves.

609 The EUV flare line light curves for the M9.9-class flare on January 1, 2014. The

610 wavelength resolution of the light curves is 10 Å, which is the same as FISM. The

611 panels indicate the light curves of Fe VIII and Fe XX 130 Å (red), Fe XV 280 Å (cyan),

612 Fe XVI 330 Å (purple), Fe XVIII 90 Å (orange), and He II 300 Å (blue) obtained by the

613 SDO/EVE MEGS-A observation (top panel: solid line), the proposed model estimation

614 (middle panel: dashed line), and FISM estimations (bottom panel: dotted line),

615 respectively. The slope of regression and correlation coefficient (CC) for each model

616 are shown at the upper left and bottom right.

617

618 Figure 10. Comparison results of EUV flare line time-integrated irradiance.

619 The relationship between the SDO/EVE MEGS-A observations and the proposed model

620 estimations of the EUV flare time-integrated irradiance for (a) Fe VIII, (b) Fe XV, (c)

621 Fe XVI, (d) Fe XVIII, (e) Fe XX, and (f) He II. In each panel, the solid line indicates

622 the regression of each plot; the dashed line indicates the straight line with slope of “1”.

623 The slope of regression and correlation coefficient (CC) are shown at the bottom right.

624

625 Figure 11. Comparison results of EUV flare band time-integrated irradiance.

626 The relationship between the SDO/EVE MEGS-A observations and proposed model

627 estimations of the EUV flare energies of two wavelength bands for (a) 55 to 355 Å and

628 (b) 55 to 135 Å. The results of the proposed model are plotted in red; FISM results are

629 plotted in blue. In each panel, the solid line indicates the regression of each plot; the

630 dashed line indicates the straight line with slope of “1”, the slope of regression is shown

631 at the upper left and bottom right.

632

633 Figure 12. The comparison results of the EUV flare line rise time.

634 The relationship between the SDO/EVE MEGS-A observations and proposed model

635 estimations of the EUV flare line rise time for the (a) Fe VIII, (b) Fe XV, (c) Fe XVI,

636 (d) Fe XVIII, (e) Fe XX, (f) He II. In each panel, the dashed line indicates the straight

637 line with slope of “1”, the correlation coefficient (CC) is shown at the bottom right.

638

639 Table 1. Comparative parameters for the M9.9-class flare on January 1, 2014.

640

641 Table 2. Flare event list for this study.