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Flexible and Cost-Effective Deep Learning for Fast Multi-Parametric Relaxometry using Phase-Cycled bSSFP

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ABSTRACT

To accelerate the clinical adoption of quantitative magnetic resonance imaging (qMRI), frameworks are needed that not only allow for rapid acquisition, but also flexibility, cost-efficiency, and high accuracy in parameter mapping. In this study, feed-forward deep neural network (DNN)- and iterative fitting-based frameworks are compared for multi-parametric (MP) relaxometry based on phase-cycled balanced steady-state free precession (pc-bSSFP) imaging. The performance of supervised DNNs (SVNN), self-supervised physics-informed DNNs (PINN), and an iterative fitting framework termed motion-insensitive rapid configuration relaxometry (MIRACLE) was evaluated *in silico* and *in vivo* in brain tissue of healthy subjects, including Monte Carlo sampling to simulate noise. DNNs were trained on three distinct *in silico* parameter distributions and at different signal-to-noise-ratios. The PINN framework, which incorporates physical knowledge into the training process, ensured more consistent inference and increased robustness to training data distribution compared to the SVNN. Whole-brain relaxometry using DNNs proved to be effective and adaptive, suggesting the potential for low-cost DNN retraining. This work emphasizes the advantages of *in silico* DNN MP-qMRI pipelines for rapid data generation and DNN training without extensive dictionary generation, long parameter inference times, or prolonged data acquisition, highlighting the flexible and rapid nature of lightweight machine learning applications for MP-qMRI.

Introduction

Improving the efficiency and stability of quantitative magnetic resonance imaging (qMRI) methods is a crucial research task to enable clinical applicability, necessitating sophisticated acquisition, reconstruction, and postprocessing strategies. In addition to accurate morphological information, which MRI as a non-invasive imaging tool can provide to guide treatment¹, qMRI has the potential to reduce subjectivity, resolve hardware or protocol dependencies inherent to conventional qualitative imaging, and increase intra- or interscanner reproducibility², facilitating the decision-making process in the diagnosis and prognosis of diseases. Generally, qMRI aims at fitting multiple qualitative (weighted) images to quantitative parameter maps with a voxel-wise representation of biophysical and microstructural processes. The derived quantitative MR biomarkers, such as relaxometry metrics, offer great potential for early detection of pathological tissue changes or longitudinal monitoring of disease. Recent studies have shown that quantitative T_2 is an important marker of cortical pathology in multiple sclerosis patients^{3,4}, early detection of hippocampal sclerosis in mesial temporal lobe epilepsy⁵, cerebrovascular disease⁶, or early Alzheimer's disease^{7,8}. Quantitative T_1 has proven beneficial for longitudinal studies to access microstructural changes related to brain aging⁹ or Parkinson's disease¹⁰. To reduce acquisition time, multi-parametric qMRI (MP-qMRI) has been of particular interest, aiming at the simultaneous estimation of multiple intrinsically co-registered parameter maps and a more complete neuroimaging protocol within feasible scan times^{11,12}.

Steady-state free precession (SSFP) sequences are a popular choice for MP-qMRI due to their sensitivity to various biochemical and microstructural tissue properties, mixed T_1 and T_2 signal sensitivity, and efficiency¹³. Jara et al. reported that MP-qMRI frameworks can be divided into direct and indirect frameworks. The latter rely on clinically interpretable fully reconstructed weighted images for post hoc mapping of parameters of interest¹⁴⁻¹⁸. On the other hand, direct MP-qMRI frameworks, such as magnetic resonance fingerprinting (MRF)¹⁹, employ the acquisition of hundreds to thousands of data points using high undersampling factors to then quantify parameters of interest from the acquired tissue-specific signal evolutions. Thereby, MRF uses a pseudo-randomized pattern of continuously varying flip angles and repetition times, which is not necessarily efficient due to required relaxation delays to recover longitudinal magnetization. Recent studies

35 demonstrate whole-brain coverage using MRF, but at the cost of either prohibitively long combined image reconstruction
36 and dictionary generation times in the order of a few hours²⁰ or rather low resolution with thick slices to ensure sufficiently
37 high signal-to-noise-ratios (SNRs)^{21,22}. Indirect approaches, including phase-cycled balanced SSFP (pc-bSSFP)^{15,16} and
38 multi-pathway non-balanced SSFP¹⁴ imaging, allow fast and efficient acquisition of multiple contrasts without the need for
39 extensive undersampling, waiting times, or long reconstruction times, while providing isotropic whole-brain coverage.

40 Machine learning (ML) techniques, in particular deep neural networks (DNNs), have shown great success for both direct
41 and indirect MP-qMRI frameworks. DNNs are utilized for dictionary generation and matching in the case of MRF²²⁻²⁴ or
42 for multi-parametric inference from multi-contrast SSFP data^{18,25}. Data-driven model-free methods that leverage measured
43 input and ground truth data for supervised learning are capable of eliminating the estimation bias due to oversimplified existing
44 signal models, for example as a result of unaccounted microstructural features as in the case of single-component simultaneous
45 T_1 and T_2 quantification based on pc-bSSFP¹⁸. The primary constraints of in vivo supervised learning are the dependence of the
46 trained DNN on specific measurement protocols, time-consuming acquisition of ground truth data, limited hardware and data
47 accessibility, and unknown model assumptions as part of black-box modeling. In silico data generation, on the other hand,
48 allows maximum control over the training data used and is becoming increasingly important in the (pre)training of ML models.
49 Nevertheless, DNNs trained on in silico data for MP-qMRI are strongly influenced by the chosen training data distribution²⁶.
50 Gyori et al. showed that selecting a uniform or an in vivo data distribution for the target parameters of interest differently
51 affects the precision and accuracy of supervised DNN predictions. Recent research has compared supervised deep neural
52 networks with physics-informed self-supervised decoding-encoding deep neural networks in the context of joint diffusion and
53 T_1 quantification²⁷.

54 This study proposes the use of in silico pc-bSSFP data to train DNN models as flexible and cost-effective frameworks for
55 multi-parameter estimation. To this end, we compare three methods for in vivo whole-brain MP-qMRI relaxometry targeted on
56 the simultaneous estimation of T_1 and T_2 in tissue, including a supervised DNN (SVNN), a physics-informed self-supervised
57 DNN (PINN), and a conventional relaxometry method called motion-insensitive rapid configuration relaxometry (MIRACLE)¹⁵
58 as reference. We investigate the impact of training data distribution on the reliability of the parameter estimation for both
59 DNN methods. The robustness of the trained SVNNs and PINNs as well as conventional MIRACLE in the presence of
60 noise-corrupted data is analyzed based on a Monte Carlo (MC) estimation of accuracy and precision metrics. Ultimately, we
61 evaluate the flexibility of DNNs in learning the inverse signal model for parameter estimation in terms of convergence speed
62 during training and estimation speed of the final DNN models.

63 **Methods**

64 The following subsections describe the in vivo data acquisition and processing, the in silico signal generation, the DNN and
65 MIRACLE frameworks for relaxometry fitting, and the experiments to validate the in silico and in vivo performance. All in
66 vivo experiments were conducted at a field strength of 3 T (Magnetom Prisma, Siemens Healthineers, Erlangen, Germany)
67 and in accordance with the guidelines of the ethics committee of the Faculty of Medicine at the Eberhard Karls University of
68 Tübingen. Python and PyTorch were used for data simulation, data processing, as well as DNN training and fitting.

69 **Data Acquisition In Vivo**

70 For in vivo validation, sagittal 3D pc-bSSFP data were used, acquired in healthy subjects with a $N_{pc} = 12$ phase-cycling
71 scheme using radiofrequency phase increments ϕ evenly distributed in the range 0 to 2π rad: $\phi(j) = \pi/N_{pc} \cdot (2j - 1)$, where
72 $j = 1, 2, \dots, N_{pc}$. The bSSFP imaging protocol employed an isotropic resolution of $1.3 \times 1.3 \times 1.3 \text{ mm}^3$ with an image encoding
73 matrix of $176 \times 176 \times 128$, ensuring coverage of the entire brain. The repetition time TR and echo time TE were set to 4.8 ms
74 and 2.4 ms, respectively, and the nominal flip angle α_{nom} was fixed at 15° . Prior to the acquisition of each phase-cycle ϕ ,
75 256 dummy pulses were played out to establish steady-state conditions. Incorporating a 2-fold in-plane parallel imaging
76 (Generalized Autocalibrating Partial Parallel Acquisition (GRAPPA)) acceleration factor, the acquisition of whole-brain
77 12-point pc-bSSFP data was completed within 10 min and 12 s. The B_1^+ scaling factor ($\alpha_{act}/\alpha_{nom}$ = actual/nominal flip angle)
78 was calculated employing the vendor's standard B_1^+ mapping sequence^{28,29}, including a TR/TE/ α_{nom} of 14.2 s/2.4 ms/ 8° , 30
79 sagittal slices with a 100% slice gap, an in-plane resolution of $2.4 \times 2.4 \text{ mm}^2$, a slice thickness of 3 mm, and a total scan time
80 of 29 s.

81 **Data Processing In Vivo**

82 Registration and segmentation tasks were performed using the FSL³⁰ and SPM³¹ software packages. To correct for motion over
83 the course of the 10 min scan, intra-registration along the phase-cycle dimension was achieved by registering the magnitude of
84 each phase-cycle to the magnitude of the sixth phase-cycle and applying each transformation to the corresponding phase data.
85 In addition, rigid body registration was used to align the B_1^+ baseline anatomical image to the mean magnitude image from
86 the motion-corrected pc-bSSFP data. The obtained transformation was applied to the B_1^+ map, which was then 3D median

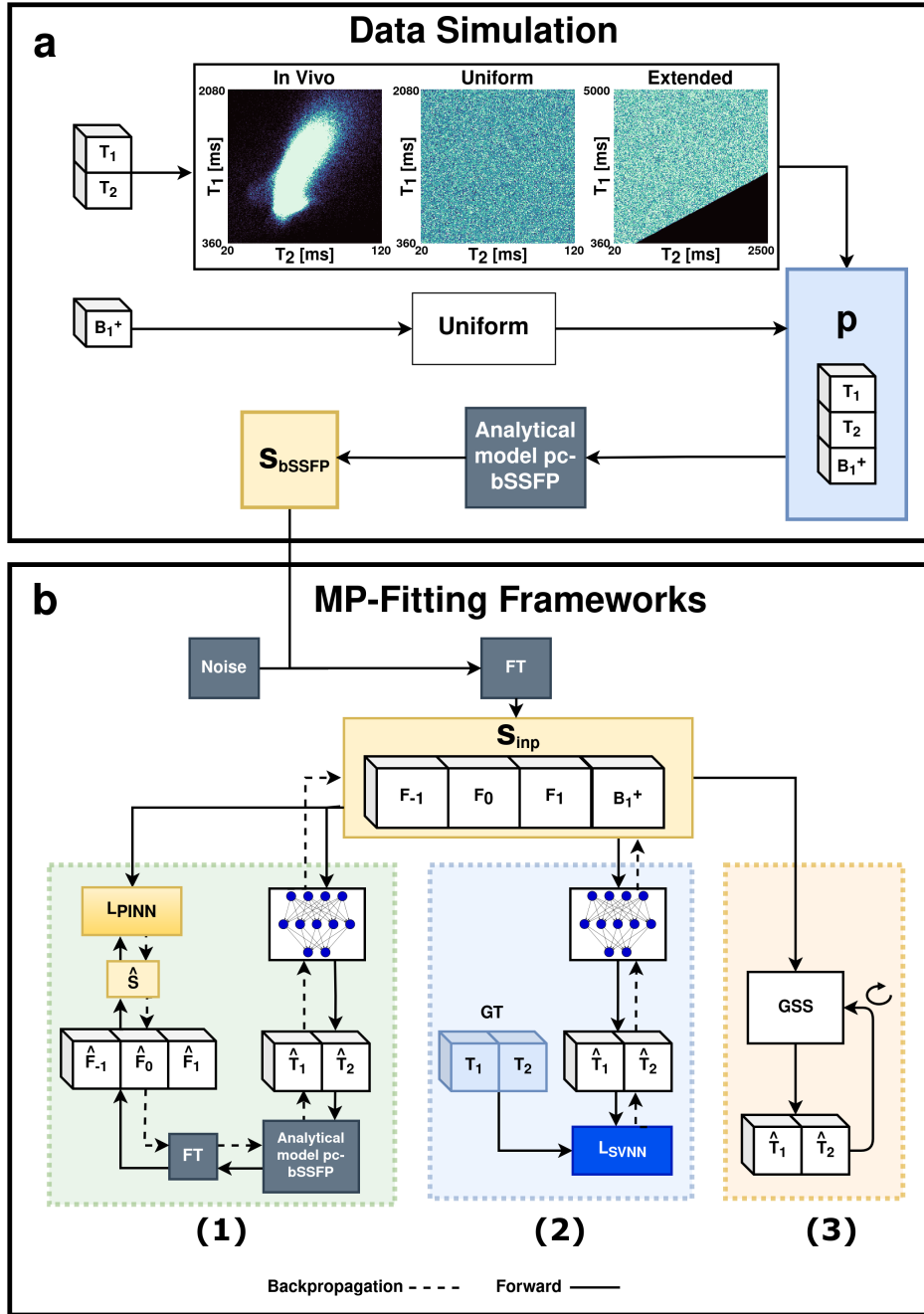


Figure 1. The workflow proposed in this work. **(a) Data Simulation:** The input parameters $\mathbf{p} = \{T_1, T_2, B_1^+\}$ entering the analytical bSSFP signal model (see Equation 1) were sampled from three different distributions (in vivo, uniform, and uniform extended) for T_1 and T_2 , and from a single uniform distribution for B_1^+ . The sequence parameters from the in vivo acquisition protocol (TR , TE , α_{nom} , N_{pc}) were used to draw 400,000 signal samples S_{bSSFP} from each T_1 and T_2 distribution. **(b) Multi-Parametric-Fitting Frameworks:** The input to each of the three frameworks, which means the physics-informed neural network (PINN, 1), the supervised neural network (SVNN, 2), and the iterative golden section search (GSS) fitting (MIRACLE, 3), consisted of the amplitudes of the three lowest order SSFP configuration modes computed from a Fourier transform (FT) of the phase-cycled bSSFP signal with the option to add noise and in addition of B_1^+ . 1) and 2) use the same multilayer perceptron architecture to estimate the inverse signal model and predict the parameters \hat{T}_1 and \hat{T}_2 . 1) uses the predicted \hat{T}_1 and \hat{T}_2 to generate an estimated signal \hat{S} and compare it to the input signal S_{inp} in the L_{PINN} loss, while 2) compares the predicted \hat{T}_1 and \hat{T}_2 directly to the respective ground truth (GT) T_1 and T_2 in the L_{SVNN} loss.

87 filtered (kernel size = [10, 10, 10]). The three lowest order SSFP configuration modes F_{-1} , F_0 , and F_1 were computed based
 88 on a 12-point discrete Fourier transform of the complex pc-bSSFP data and the magnitudes of the configuration modes were
 89 further subjected to Gibbs ringing removal³². Voxel-wise normalization using Euclidean distance was performed to match the
 90 in silico data. For in vivo SNR determination, the average signal level was obtained as the mean signal in a whole-brain tissue
 91 mask applied to the magnitude of the F_0 configuration, pooled across three representative subjects. The average noise level was
 92 determined as the mean standard deviation in a background mask applied to the same data. The average SNR level pooled
 93 across all three subjects was 25. The definition of the masks for the in vivo SNR determination is illustrated in Supplementary
 94 Fig. S1.

95 **Data Generation In Silico**

96 Synthetic single isochromat pc-bSSFP signals S_{bSSFP} were generated using the forward on-resonant bSSFP signal model
 97 $S_{\text{bSSFP}}(\mathbf{p}, \mathbf{u})$ with parameters $\mathbf{p} \in \{T_1, T_2, B_1^+\}$ (longitudinal relaxation time T_1 ; transverse relaxation time T_2 ; transmit field
 98 scaling factor $B_1^+ = \alpha_{\text{act}}/\alpha_{\text{nom}}$), sequence parameters $\mathbf{u} \in \{\text{TR}, \text{TE}, \alpha_{\text{nom}}, N_{\text{pc}}\}$ (repetition time TR, echo time TE, nominal
 99 flip angle α_{nom} , number of phase cycles N_{pc}), and initial magnetization $M_0 = 1$ ³³:

$$S_{\text{bSSFP}} = M_0 \frac{(1 - E_1)(1 - E_2 e^{-i\phi}) \sin \alpha_{\text{act}}}{C \cos \phi + D} e^{-\text{TE}/T_2} \quad (1)$$

with

$$E_{1,2} = e^{-\text{TR}/T_{1,2}} \quad (2)$$

$$C = E_2(E_1 - 1)(1 + \cos \alpha_{\text{act}}) \quad (3)$$

$$D = (1 - E_1 \cos \alpha_{\text{act}}) - (E_1 - \cos \alpha_{\text{act}})E_2^2 \quad (4)$$

and

$$\phi[0, 2\pi] = \pi/N_{\text{pc}} \cdot (2j - 1), j = 1, 2, \dots, N_{\text{pc}} \quad (5)$$

100 The target parameters T_1 and T_2 were sampled from three different distributions (see [Figure 1](#)): a uniform distribution
 101 with T_1 ranging from 360 to 2080 ms and T_2 ranging from 20 to 120 ms, a uniform distribution with an extended T_1 range
 102 from 360 to 5000 ms and an extended T_2 range from 20 to 2500 ms, and an in vivo distribution with the same range as the
 103 uniform distribution, but by sampling from a 2D density map generated based on the T_1 and T_2 brain voxel distributions of
 104 three healthy subjects obtained from existing gold standard 2D multi-slice inversion-recovery turbo-spin-echo (T_1) and 2D
 105 multi-slice single-echo spin-echo (T_2) scans with variable inversion and echo times, respectively. Corresponding anatomical
 106 magnetization-prepared rapid gradient-echo (MPRAGE) data³⁴ were skull-stripped and used for white matter (WM), gray
 107 matter (GM), and cerebrospinal fluid (CSF) segmentation. Voxels containing pure CSF according to the performed segmentation
 108 were excluded from the density estimation. The T_1 and T_2 parameter boundaries of the in vivo and uniform distribution were
 109 approximated as the mean ± 2 standard deviations of the values in the defined brain masks of three subjects. Additionally,
 110 $T_1 < T_2$ parameter combinations were excluded for all distributions. For each distribution, 400,000 samples were generated,
 111 resulting in a total training data size of 38.4 MB and 6.4 MB for the input and target data, respectively. B_1^+ was uniformly
 112 sampled in the range 0.7 to 1.3 and an on-resonant condition with an off-resonance $\Delta B_0 = 0$ Hz was assumed. Sequence
 113 parameters were set according to the in vivo pc-bSSFP protocol. For in silico performance validation, an additional 2D grid
 114 (200 x 200 steps) of linearly sampled T_1 and T_2 values in the uniform distribution range as well as 40,000 in vivo test data
 115 points sampled from the 2D in vivo density map were generated for pc-bSSFP signal simulation ($B_1^+ = 1$).

116 **Relaxometry**

117 For direct comparison, the DNNs were designed to take the same input data as MIRACLE, i.e. the magnitude of the three
 118 lowest order SSFP configuration modes (F_{-1} , F_0 , F_1) and B_1^+ , as shown in [Figure 1](#). MIRACLE fitting was performed using
 119 an iterative golden section search minimization algorithm with an initial T_1 estimate of 1000 ms^{14, 15}. SVNNs and PINNs
 120 were based on a fully connected feed-forward multilayer perceptron with four inputs, two hidden layers of 64 neurons each,
 121 followed by a ReLU activation function, and an output sigmoid layer of two neurons for T_1 and T_2 estimation. The resulting

122 model contained 4610 trainable parameters, leading to a total size of 21 kB. The trainable parameters were initialized using
 123 PyTorch's default layer initialization³⁵ and the Adam optimizer³⁶. A fixed learning rate of $2 \cdot 10^{-4}$, a batch size of 128, an early
 124 stopping with a patience of 25 epochs, and a maximum of 300 epochs were used for DNN training. Within each training batch,
 125 the real and imaginary parts of the pc-bSSFP data were corrupted by additive Gaussian noise samples with a noise level of
 126 $\eta = 0.074/(\sqrt{2} \cdot \text{SNR})$ and $\text{SNR} \in \{\text{inf}, 50, 25, 10\}$, where η is zero if $\text{SNR} = \text{inf}$. The three lowest order SSFP configuration
 127 modes were computed as described above in the subsection *Data Processing In Vivo*. While both DNN frameworks were
 128 designed to decode the inverse signal model from the pc-bSSFP signals to target relaxometry parameters, two different loss
 129 strategies were used as proposed by Grussu et al.²⁷: a signal loss $L_{\text{PINN}} = \text{MSE}(\hat{S}, S_{\text{inp}})$ involving the analytical pc-bSSFP
 130 signal model and subsequent Fourier transform of the complex signal in the encoding step to compute the mean squared error
 131 (MSE) between the signal from the predicted target parameters \hat{S} and the input signal S_{inp} (see Figure 1b, part 1), and a target
 132 parameter loss $L_{\text{SVNN}} = \text{MSE}(T_i, \hat{T}_i)$ with $i = 1, 2$, which computes the MSE between the model parameter predictions \hat{T}_1 and
 133 \hat{T}_2 and the ground truth target parameters T_1 and T_2 (see Figure 1b, part 2).

134 **Validation In Silico**

135 Each DNN framework, trained with different distributions and SNR levels, as well as the MIRACLE framework were validated
 136 on 5000 MC samples by augmenting the complex pc-bSSFP signals from the 2D linear grid and in vivo distribution test data
 137 of T_1 and T_2 values with additive noise from a Gaussian distribution and $\text{SNR} \in \{\text{inf}, 50, 45, 40, 35, 30, 25, 20, 15, 10\}$. To test
 138 the accuracy and precision of each framework on in silico data, the mean μ_{MC} , standard deviation σ_{MC} , and relative standard
 139 deviation $\sigma_{\text{rel}} = \sigma_{\text{MC}}/\mu_{\text{MC}}$ of the parameter predictions across all MC samples were calculated. The relative error between the
 140 MC mean of the parameter predictions $\hat{y}_{\mu_{\text{MC}}}$ and the respective ground truth value y was calculated for both DNN frameworks
 141 on the 2D linear T_1 and T_2 sampling grid as $\varepsilon_{\text{rel}} = (\hat{y}_{\mu_{\text{MC}}} - y)/y \cdot 100$. In addition, the coefficient of determination (CoD) was
 142 calculated for all frameworks, distributions, and SNR levels for the entire 2D grid and the in vivo test data. The CoD was
 143 computed as a global metric as follows:

$$\text{CoD} = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_{i\mu_{\text{MC}}})^2}{\sum_{i=1}^n (y_i - \bar{y})^2} \quad (6)$$

where:

- n is the number of observations,
- y_i is the observed value for the i th observation,
- $\hat{y}_{i\mu_{\text{MC}}}$ is the MC mean of the predicted values for the i th observation,
- \bar{y} is the mean of the observed values.

144 **Validation In Vivo**

145 For each relaxometry framework, simultaneous whole-brain T_1 and T_2 estimation was performed in healthy subjects. SVNN
 146 and PINN frameworks trained without the addition of noise during training ($\text{SNR} = \text{inf}$) were used for in vivo inference. To
 147 compare the effect of different training data distributions on prediction accuracy, the absolute difference between the DNN
 148 predictions from the trainings with three distributions and the MIRACLE prediction was calculated. In addition, MC sampling
 149 was performed on an exemplary axial slice of the in vivo data with 5000 samples and six augmented ROIs with additional
 150 Gaussian noise added to the real and imaginary parts of the acquired pc-bSSFP data before calculating the SSFP configuration
 151 modes.

152 The effectiveness of the DNN frameworks to learn the inverse signal model for MP-qMRI was investigated by calculating
 153 the CoD between whole-brain relaxometry predictions of each epoch and the final epoch of a training process for whole-brain
 154 WM, GM, and WM+GM tissue masks. Furthermore, a single-epoch PINN training was performed and applied to the in vivo test
 155 subject. The entire process of in silico data generation, single-epoch learning, and in vivo inference was timed and compared to
 156 the MIRACLE algorithm on whole brain pc-bSSFP data (single CPU thread on Intel(R) Xeon(R) W-2255 CPU @ 3.70GHz,
 157 62.5 GB RAM). To assess the benefit of the trained DNN frameworks, the inference time for simultaneous in vivo whole-brain
 158 relaxometry was additionally measured for all three frameworks on input data interpolated to different isotropic resolutions of
 159 1.3 mm, 1.0 mm, 0.8 mm, 0.6 mm, and 0.4 mm.

160 **Results**

161 **In Silico**

162 The impact of including image noise explicitly into the DNN training process by adding noise of a predefined level to the in
 163 silico training data is analyzed by an MC sampling of the in silico test data for DNNs trained on three different training data

distributions (cf. Figure 2). To ensure comparability with the acquired in vivo data, the noise added during training was matched to the SNR of 25 present in the masked brain tissue of the in vivo pc-bSSFP data and applied to the test data. As evident from Figure 2, training DNN frameworks under non-ideal conditions with noise-corrupted training samples does not imply better accuracy on test data with equal SNR level. While the accuracy of PINNs trained on noise-corrupted data (Figure 2b, right) appears similar to that of PINNs trained on noise-free data (Figure 2a, right), SVNNs perform worse when training includes noise (Figure 2, left). Furthermore, it can be observed that the performance of the trained PINN models is largely independent of the training data distribution, in contrast to the SVNN frameworks. In the case of the uniform distribution with extended parameter range, the SVNN shows reduced accuracy compared to the other two distributions. Since training with additional noise evidently does not improve prediction performance, the following analysis focuses on the application of DNNs trained on noise-free in silico data. Therefore, the indication of SNR or noise levels refers in the following exclusively to the test data rather than the training data.

The prediction performance dependence of the DNNs trained with noise-free data and MIRACLE on the SNR of the in silico test data is evaluated in Figure 3 by the calculation of the CoD, reflecting the agreement between the mean MC predictions and the ground truth for test data from a linear sampling grid (cf. Figure 3, left column) and from the in vivo distribution (cf. Figure 3, right column). High CoD values can be observed for MIRACLE at SNR levels down to $\approx 15 - 20$ until the accuracy starts to break down (cf. Figure 3a). While the difference between the CoD of the DNNs and MIRACLE (ΔCoD) is neglectable for high test SNR levels, the performance of the DNNs trained with the uniform and in vivo distributions is superior to MIRACLE at low SNR levels (≤ 15) (cf. Figure 3b and c). The DNNs trained with the uniform extended distribution show reduced CoD values on noisy test data comparable to MIRACLE. Only exception is the SVNN-based T_2 estimation, which shows a clearly lower accuracy than MIRACLE for the in vivo distribution test data in case of the uniform extended training data distribution (cf. Figure 3c, right).

The robustness of the DNNs trained with data distributions matched to the in vivo tissue T_1 and T_2 range, i.e. uniform and in vivo distributions, is further corroborated by the precision analysis in Figure 4. The relative standard deviation $\sigma_{rel}(T_i)$ of the MC simulation for in silico test data from a linear grid with an SNR = 25 reflecting in vivo conditions is lower than MIRACLE for both SVNNs and PINNs trained with the uniform or in vivo distribution while the DNNs trained with the uniform extended distribution demonstrate similar precision as MIRACLE. The performance advantage of the DNNs trained with the uniform and in vivo distribution is enhanced in low SNR scenarios (see Supplementary Fig. S2, SNR = 10).

191 **In Vivo**

192 In line with the in silico results in Figure 2 and Figure 3, the trained DNNs show high agreement with MIRACLE relaxometry
193 in brain tissues when tested on unseen in vivo data, especially for the parameter distributions, which are optimized for brain
194 tissue at the employed field strength (cf. Figure 5). The relaxation parameter values predicted by the SVNN framework, which
195 was trained with the uniform extended distribution and thus for a parameter range covering not only relaxation times in tissues
196 but also in fluids, deviate from T_1 and T_2 provided by MIRACLE. On the other hand, the PINN framework shows greater
197 robustness to the underlying training data distribution with lower differences to the MIRACLE predictions, especially for T_2 ,
198 but also T_1 . Furthermore, the in vivo MC sampling demonstrates an increased precision (lower σ_{MC}) for DNNs trained with the
199 uniform (cf. Figure 6) and in vivo (not shown) distributions as compared to MIRACLE, thus confirming the in silico findings
200 illustrated in Figure 4. In accordance with the in silico results, mean and standard deviation of in vivo MC samples match the
201 MIRACLE performance for DNNs trained with the uniform extended distribution (see Supplementary Fig. S3).

202 **Flexible and Cost-Effective Relaxometry**

203 The adaptability and flexibility of in silico DNN training is evaluated in Figure 7a (SVNN) and Figure 7b (PINN) by the
204 CoD between the in vivo predictions of each epoch and the final epoch in different whole-brain tissue masks as well as the
205 overall validation loss across epochs, representatively for a DNN training using the uniform data distribution. Final training
206 convergence with a CoD > 0.99 was reached after about 200 epochs. However, already within the first epochs, T_1 and T_2
207 relaxation times of brain tissues are learned effectively. This is corroborated by CoD values higher than 0.93 and 0.88 after
208 the very first, and higher than 0.99 and 0.97 after the first ten epochs for the SVNN (cf. Figure 7a) and PINN (cf. Figure 7b),
209 respectively, across all investigated tissue masks. Training of a single epoch was completed after only about 9 s for the SVNN
210 and 14 s for the PINN frameworks using a single CPU thread. The effectiveness of single-epoch versus final-epoch training is
211 demonstrated for in vivo whole-brain relaxometry in Figure 7c and d for the SVNN and PINN frameworks, respectively. The
212 entire process of training data simulation, single-epoch model training, and whole-brain in vivo inference at 1.3 mm isotropic
213 resolution took only about 12 s and 17 s for the SVNN and PINN frameworks, respectively, thus only about 45 % and 64 %
214 compared to the inference time of the MIRACLE algorithm applied to the same data by using the same computing power.

215 A clear advantage of using DNNs over the MIRACLE framework for simultaneous whole-brain relaxometry is the inference
216 time, as demonstrated in Figure 8. When the resolution of the in vivo input data is increased from 1.3 mm to 0.8 mm or even
217 to 0.4 mm isotropic voxel sizes, the inference time increases exponentially from 26.7 s to 96.9 s to 769.8 s for MIRACLE,

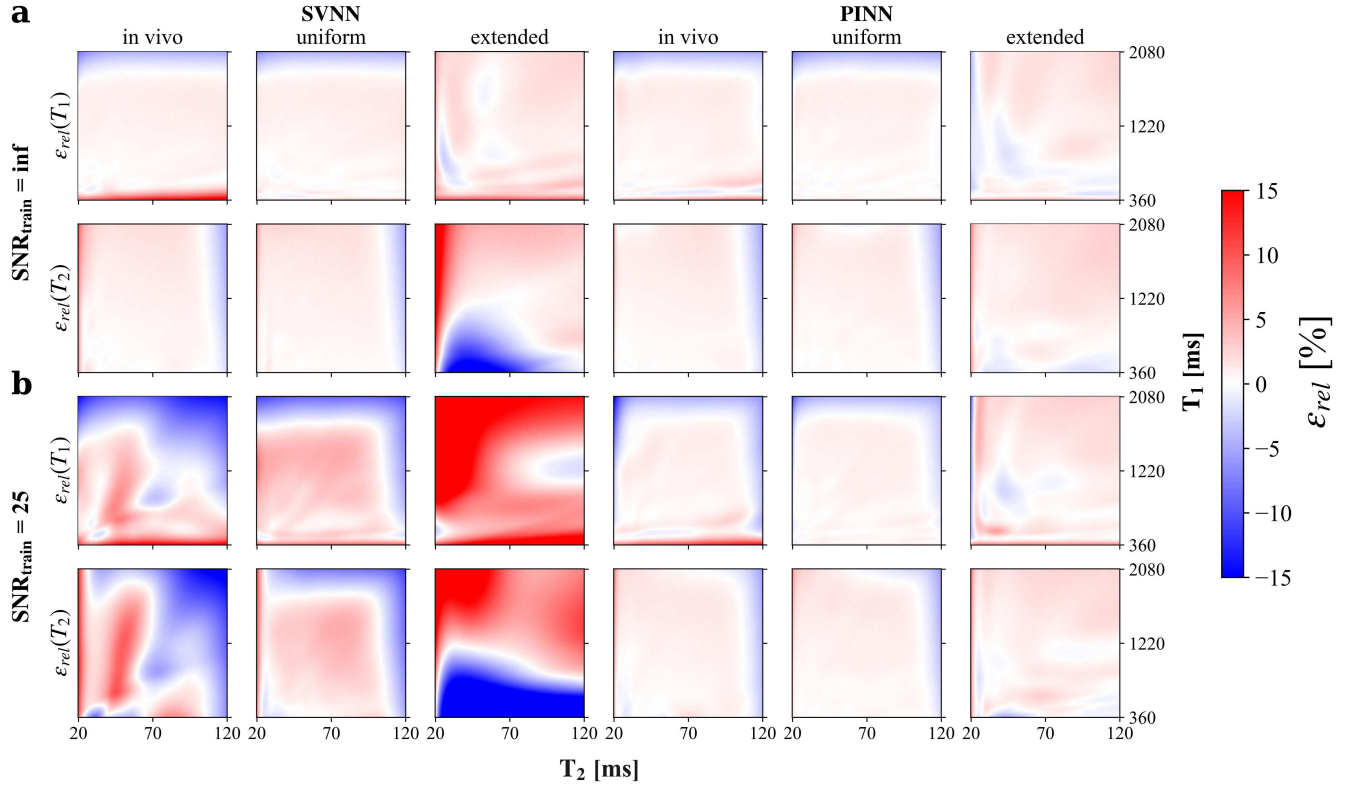


Figure 2. Influence of training data SNR and training data distribution on accuracy of investigated DNNs in silico. The relative error in percent $\varepsilon_{rel}(T_i) = (\hat{T}_{i,\mu_{MC}} - T_i)/T_i \cdot 100$ with $i = 1, 2$, between the mean of the MC simulation $\hat{T}_{i,\mu_{MC}}$ and the ground truth T_i , is quantified for T_1 and T_2 parameter estimates of the SVNNs (left) and PINNs (right) trained on noise-free (**a**, SNR = inf) and noise-corrupted (**b**, SNR = 25) data with different training data distributions. The MC estimation is performed on a noise-corrupted in silico linear test grid with SNR = 25 matched to in vivo conditions as well as a T_1 and T_2 range corresponding to brain tissues (consistent with the parameter range of the in vivo and uniform distribution employed for DNN training). Parameter over- and underestimation with respect to the ground truth are shown in red and blue, respectively.

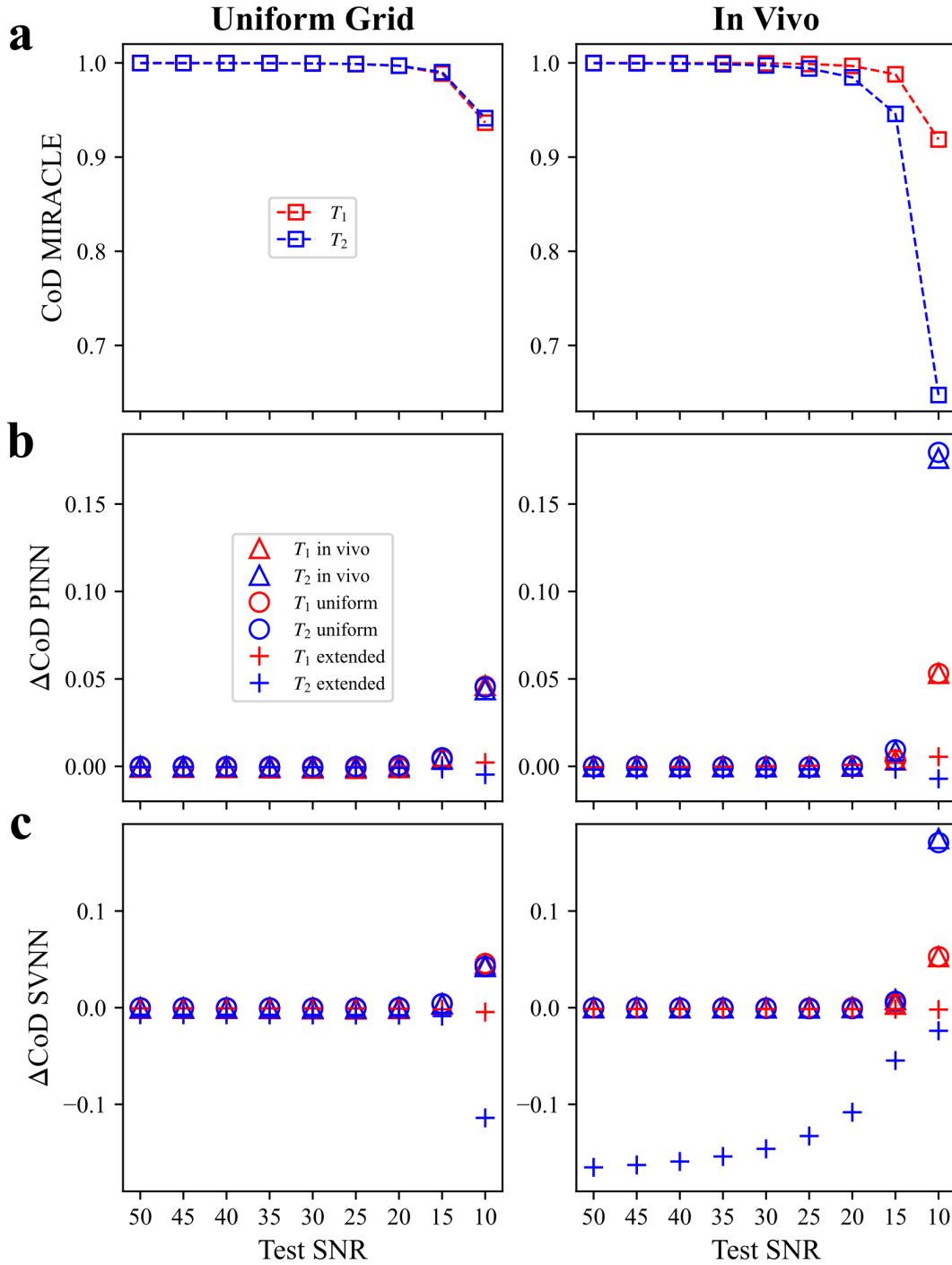


Figure 3. Coefficient of determination versus test data SNR of investigated DNNs relative to MIRACLE in silico. The CoD between the mean MC relaxation parameter predictions $\hat{T}_{i\mu_{MC}}$ and the ground truth T_i with $i = 1, 2$ (T_1 in red and T_2 in blue) is shown for the linear test grid (left column) and the in vivo distribution test data (right column). **(a)** CoD versus test data SNR for MIRACLE (\square). **(b)** and **(c)** The absolute CoD difference between the DNNs and MIRACLE ($\Delta\text{CoD} = \text{CoD}_{\text{DNN}} - \text{CoD}_{\text{MIRACLE}}$) versus test data SNR for the PINN **(b)** and the SVNN **(c)**. For both SVNN and PINN, three models trained on noise-free data (SNR = inf) with different data distributions are evaluated: in vivo (\triangle), uniform (\circ), and uniform extended distribution ($+$). Note that positive/negative values in **(b)** and **(c)** are referring to higher/lower CoD values of the DNNs relative to MIRACLE.

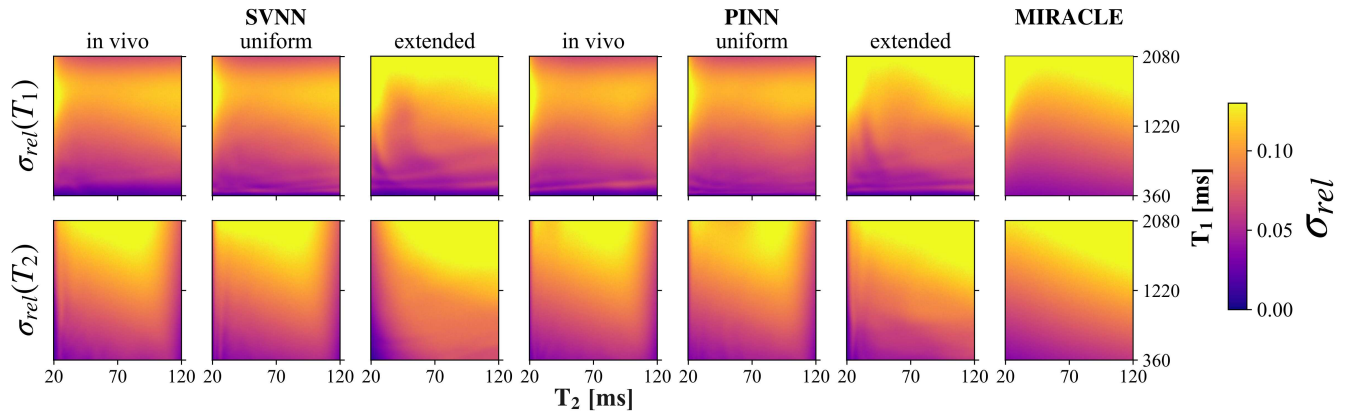


Figure 4. Influence of training data distribution on precision of investigated DNNs versus MIRACLE in silico. The precision of T_1 and T_2 quantification is evaluated by MC sampling with an **SNR level of 25**, matched to the in vivo data, applied to an in silico linear test grid with T_1 in the range 360 to 2080 ms and T_2 in the range 20 to 120 ms. The relative standard deviation $\sigma_{rel} = \sigma_{MC}/\mu_{MC}$, with μ_{MC} and σ_{MC} corresponding to the mean and standard deviation of the MC simulation is plotted for all three frameworks (SVNN, PINN, MIRACLE) and in case of the DNNs for all three trained data distributions. All DNNs were trained without additional noise applied to the training data (SNR = inf).

218 compared to 2.3 s to 9.9 s to 78.0 s for the PINN (and similarly for the SVNN). The inference time using DNNs is thus always
 219 in the order of one magnitude lower, allowing fast parameter estimation for very high-resolution whole-brain data in only about
 220 10 % of the inference time compared to MIRACLE.

221 Discussion

222 Since the optimization of DNN model architectures may require new measurements, re-running of DNN training, or adaptation
 223 to changing tissue parameter characteristics at different field strengths as in case of relaxation times, flexible and effective DNN
 224 frameworks are desired. The results presented in this work suggest the combination of in silico trained DNNs with pc-bSSFP
 225 imaging as a fast and adaptable framework for MP-qMRI relaxometry. In silico DNN training allows full control over sequence
 226 parameters and tissue parameter distributions, does not require any extra measurements of ground truth data, and is able to
 227 efficiently learn the inverse signal model. Both supervised and self-supervised physics-informed DNNs have been successfully
 228 implemented and trained on different in silico data distributions, achieving a performance matching or exceeding the one of
 229 reference iterative multi-parametric fitting approaches such as MIRACLE with whole-brain in vivo inference times on unseen
 230 test data, which are an order of magnitude shorter in comparison to MIRACLE.

231 MC simulations based on in silico data (cf. Figure 2) revealed a strong sensitivity of SVNN estimation accuracy to the
 232 training data distribution, but also to the SNR level of the training data while the PINN models remained highly unaffected by
 233 the distribution and noise characteristics of the training samples. Generally, the DNNs trained on noise-corrupted training data
 234 and tested on data at the same SNR level did not reveal any ability to improve T_1 and T_2 prediction performance as compared to
 235 DNNs trained without any additional noise. Increasing the complexity of DNNs may allow to capture the noise present in the
 236 training data. However, sample-wise noise addition may be unrealistic for the spatially varying noise characteristics encountered
 237 in reconstructed MR images and hinder efficient learning of the signal model, especially for smaller DNN architectures with
 238 fewer trainable parameters. Provided the accessibility of larger cohort data sets, image-based DNNs could be investigated in
 239 future for denoising tasks.

240 The DNNs trained on noise-free in silico data with a uniform parameter distribution matched to the relaxation time range
 241 of tissues or an in vivo parameter distribution performed reliably in the presence of noise on the test data, with an advantage
 242 over MIRACLE for low SNR scenarios (cf. Figure 3), which may be particularly beneficial for potential future applications at
 243 low-fields ($B_0 \leq 1.5$ T). As evident from the results presented in Figure 4 for a realistic pc-bSSFP SNR level applied to the test
 244 data (determined for 3T and 1.3 mm isotropic resolution), the precision of the trained DNNs is affected by the training data
 245 distribution. For distributions tailored to the relaxation time range of interest, DNNs show ability to reach higher precision than
 246 MIRACLE, motivating the optimization of DNN frameworks for targeted tissue parameter ranges. The lower the SNR of the
 247 input data, the more pronounced becomes the precision advantage of the DNNs over MIRACLE (cf. Supplementary Fig. S2).

248 The in silico results were successfully reproduced on in vivo test data, revealing a stronger dependence on the training data
 249 distribution of the SVNN framework compared to the PINN framework (cf. Figure 5). The observed influence of training data

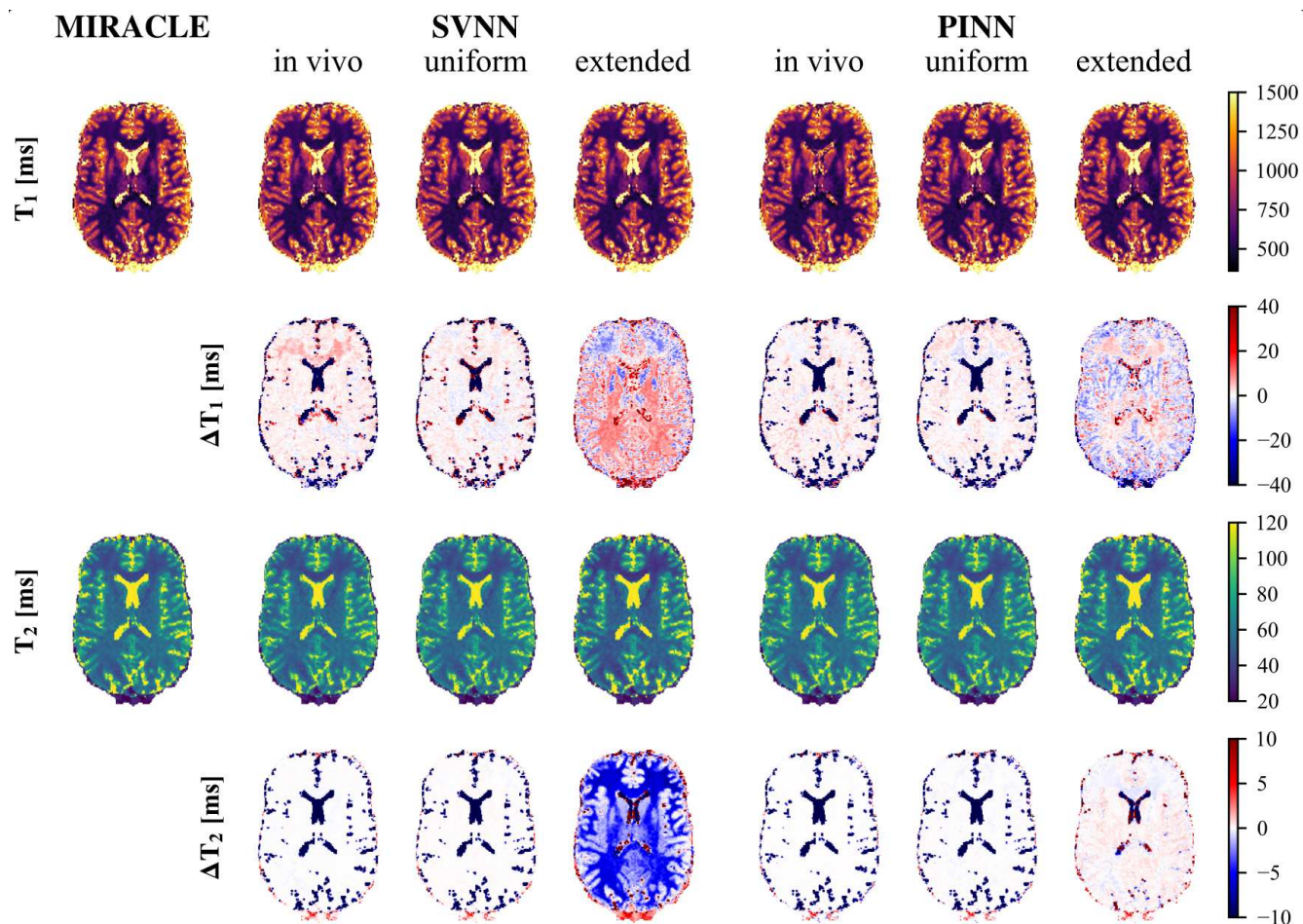


Figure 5. In vivo analysis of the effect of the DNN training data distribution relative to MIRACLE. A representative axial slice of the in vivo whole-brain T_1 (first row) and T_2 (third row) predictions of an unseen test subject is shown for the MIRACLE framework (first column), and both DNNs, each trained on in silico data without additional noise ($\text{SNR} = \text{inf}$) and three different distributions (in vivo, uniform, and uniform extended). The absolute differences between the DNN predictions and the MIRACLE prediction are shown in the second and fourth row for T_1 and T_2 , respectively. Red and blue refer to an over- and underestimation of the DNN framework predictions relative to the MIRACLE framework predictions, respectively.

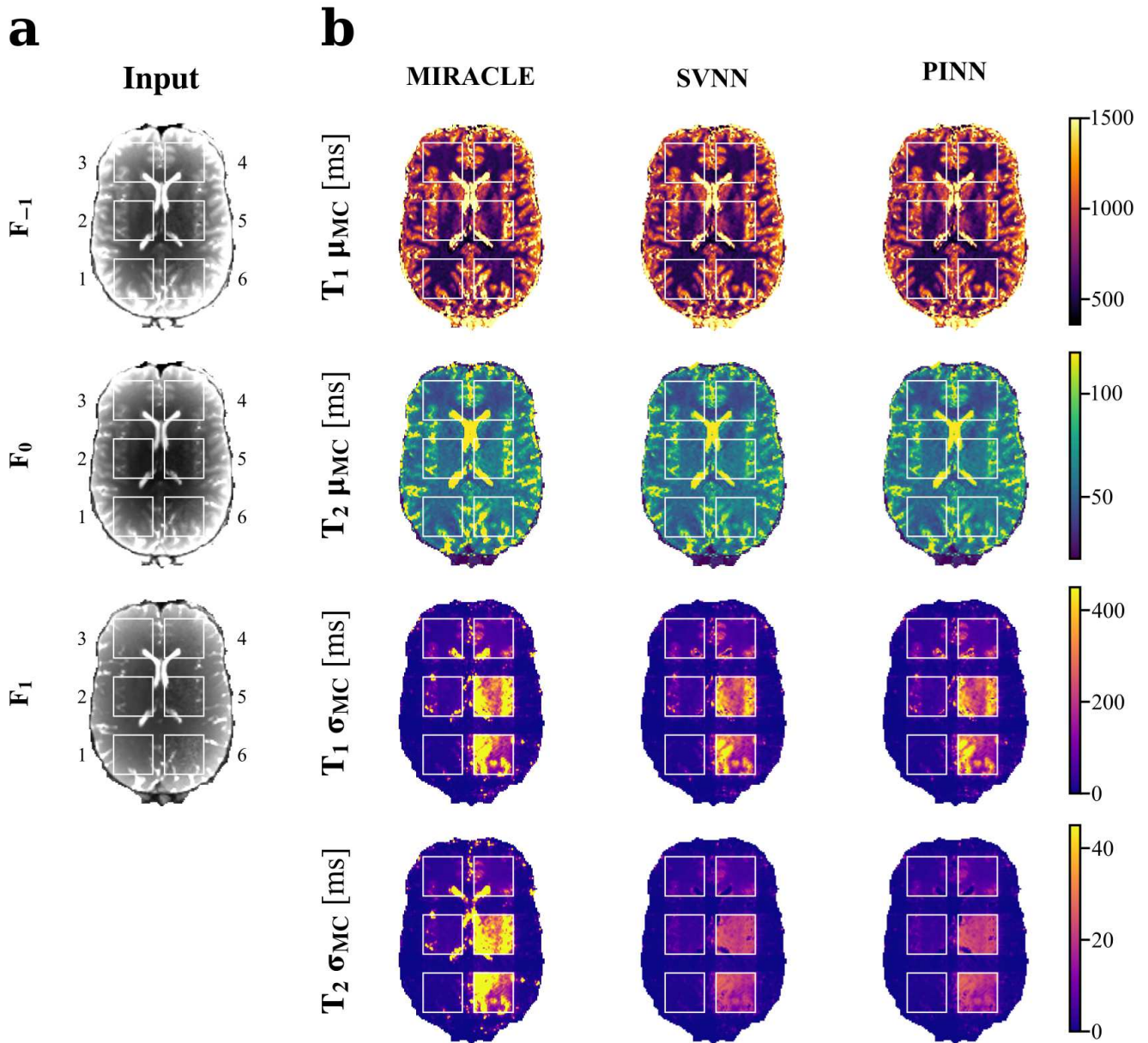


Figure 6. Robustness in the presence of noise-corrupted in vivo test data of SVNN and PINN versus MIRACLE, illustrated for a representative axial slice of an unseen test subject. (a) The multi-contrast input for quantification of the relaxation parameters, i.e. the magnitude of F_{-1} , F_0 , and F_1 , for an individual MC noise sample. (b) The mean (μ_{MC} , rows 1+2) and standard deviation (σ_{MC} , rows 3+4) of the in vivo MC parameter predictions. The displayed results refer to DNNs trained on in silico data with the **uniform distribution** and no additional noise (SNR = inf). In addition to the existing noise of the in vivo test data, noise sampled from a Gaussian distribution with six different standard deviations ($\eta \in \{1, 2, 4, 8, 12, 16\}$ and respective in vivo SNRs $\in \{18, 14, 11, 7, 5, 4\}$) was added to the real and imaginary parts of the pc-bSSFP data in six different rectangular ROIs, labeled 1-6 in the order of increasing noise levels.

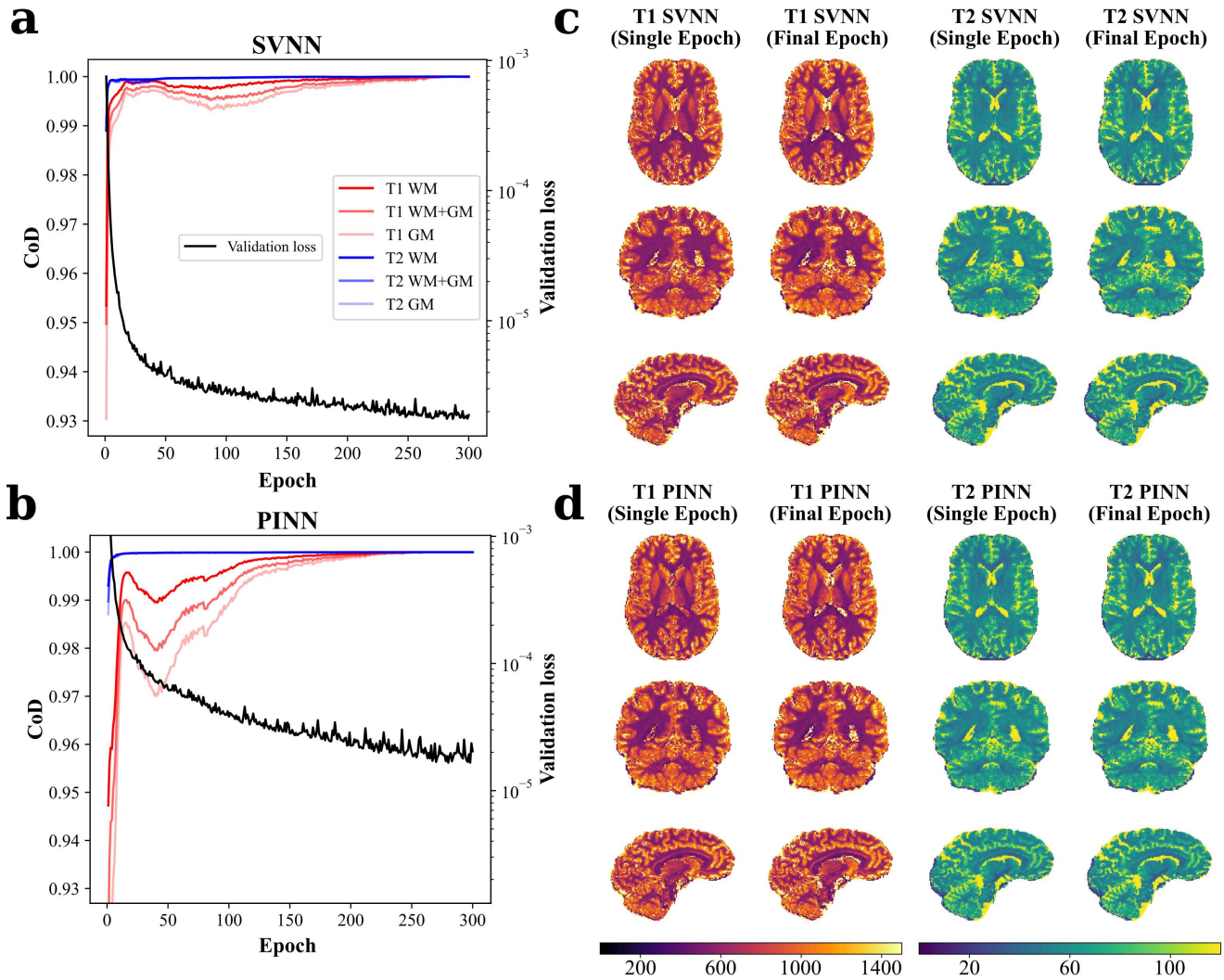


Figure 7. Efficiency of DNN inverse signal model learning versus epochs, corroborated by representative relaxation time maps of single-epoch in vivo whole-brain inference. The CoD during SVNN (a) and PINN (b) training is calculated for each epoch with respect to the final-epoch model and plotted versus epochs for in vivo T_1 (red) and T_2 (blue) predictions in whole-brain WM, GM, and WM+GM tissue masks of an unseen test subject. Additionally, the validation loss for both DNN frameworks is shown in black on a logarithmic scale. The employed DNNs were trained on the in silico uniform noise-free data distribution. Note that the final validation loss of the SVNN framework is on the order of one magnitude lower than the one of the PINN framework due to the different definitions of the loss functions and embedding of physical constraints for the PINN. Corresponding representative axial, coronal, and sagittal slices of in vivo whole-brain T_1 and T_2 single-echo versus final-epoch predictions of an unseen test subject are shown for SVNN (c) and PINN (d).

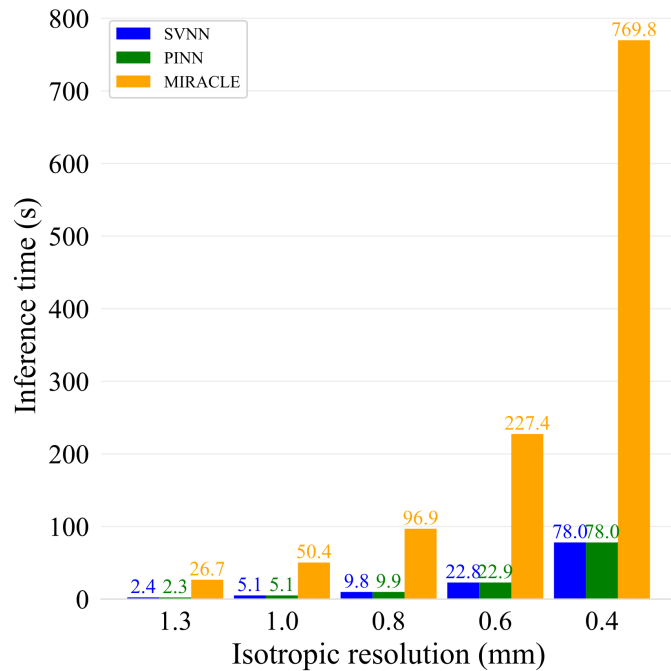


Figure 8. Whole-brain relaxometry inference times for different isotropic resolutions of the input data. The inference times in seconds of each multi-parametric relaxometry framework (SVNN: blue, PINN: green, MIRACLE: orange) are calculated for the whole-brain input data of a test subject interpolated to different isotropic resolutions of 1.3, 1.0, 0.8, 0.6 and 0.4 mm. Inference is performed using a single CPU thread (Intel(R) Xeon(R) W-2255 CPU @ 3.70GHz, 62.5 GB RAM).

250 distribution on the accuracy of SVNNs is consistent with existing research^{26,37}. Epstein et al. proposed to adjust the in silico
 251 ground truth labels by precomputed labels from maximum likelihood estimation and to extend the supervised loss to improve
 252 the accuracy of SVNNs³⁷. On the other hand, the observed robustness of physics-informed DNNs to the underlying training
 253 data distributions can be explained by a successful utilization of the analytical pc-bSSFP signal model, which encodes the
 254 estimated parameters into the pc-bSSFP signal during the learning process. Additionally, we observed that the DNNs, which
 255 were trained on data distributions optimized for the brain tissue parameter range, achieved lower standard deviations in the in
 256 vivo MC simulations for added noise levels and thus increased precision compared to MIRACLE (cf. Figure 6), in line with the
 257 in silico findings.

258 Inherent to the architecture of PINNs are the boundaries of the achievable parameter values, which are predefined by the
 259 developer, prohibiting extrapolation. Thus, a limitation of PINNs is the need for retraining if the parameter range of interest
 260 falls outside the simulated range. Similarly, the performance of SVNNs is expected to be impaired for parameter combinations
 261 not contained in the training set. Furthermore, this work is restricted to a single-component signal model by assuming that
 262 only a single T_1 and T_2 component at a single resonance frequency contributes to the acquired pc-bSSFP signal evolutions in
 263 tissues, thus not accounting for characteristic asymmetries in the frequency response of bSSFP. Those reflect anisotropies in
 264 tissue microstructure with a correlation to diffusion metrics, e.g. in WM³⁸⁻⁴¹, or the sensitivity to chemical shift, which can be
 265 exploited for fat fraction mapping⁴². Comparable to MIRACLE, this results in an underestimation of T_1 and T_2 in brain tissues
 266 with respect to gold standard spin-echo-based reference methods^{15,16}.

267 In contrast to PINN, SVNN architectures are capable to identify nonlinear feature decodings, which cannot be modeled
 268 analytically. This can be exploited for the training of model-free SVNNs on in vivo data with independent ground truth MR
 269 measurements for each target parameter. However, supervised learning on in vivo data may be prone to input and target
 270 misalignment and necessitate prohibitively long scan times due to the need for ground truth data acquisition. Furthermore, the
 271 common ground in qMRI is dynamic and even current gold standard methods can be subject to various adverse instrumental
 272 factors related to the underlying sequence, hardware, or fitting routine, potentially leading to a quantification bias⁴³.

273 Due to the ability to simulate, train, and infer tissue parameters in only a few seconds as demonstrated here (cf. Figure 7), in
 274 silico DNN training provides a cost-effective option and can easily be adapted to altered sequence parameters, new anatomical
 275 targets, or different field strengths, without requiring extensive MR data collection. While this work focuses on a direct
 276 comparison with MIRACLE, the input of the implemented DNNs can conveniently be extended to include phase information
 277 and thus to extract additional parameters, e.g. ΔB_0 . Once trained, the investigated DNNs are able to infer multi-parametric

278 relaxation characteristics an order of magnitude faster than traditional iterative fitting as only a few matrix multiplications need
279 to be performed (cf. [Figure 8](#)). This has high value in terms of clinical applicability or for studies necessitating the processing
280 of large data cohorts. Future work may include the extension of the signal model employed for in silico DNN training to
281 multi-compartment scenarios, the implementation of image-based architectures to benefit from anatomical information, and the
282 application to pathological test data to validate the generalization performance in a clinical context.

283 In conclusion, we have derived adaptable cost-effective deep learning frameworks for multi-parametric relaxometry based
284 on pc-bSSFP data, which are characterized by rapid convergence during training, parameter inference times of only a few
285 seconds once training is concluded, and the ability to embed physical knowledge into the training process. By tailoring the
286 underlying training data distribution to the target parameters of interest, superior performance to conventional fitting approaches
287 could be achieved, especially in low-SNR scenarios, motivating further investigations at low field strengths.

288 Data availability

289 The data sets analysed during the current study are available via the data sharing platform [KEEPER](#). Upon request, a password-
290 protected fully anonymized data set of a test subject can be downloaded.

291 Code availability

292 The source code and trained models for this study will be publicly available upon acceptance on [Github](#).

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391 **Author contributions statement**

392 Initial data collection: R.H. Conceptualization: F.B., R.H. Funding acquisition: K.S., R.H. Investigation: F.B., R.H. Method
393 development: F.B., R.H. Method implementation: F.B., L.M., J.S., Q.W. Resources: K.S., R.H. DNN model training and
394 testing: F.B. Supervision: R.H. Visualization: F.B. Writing—original draft: F.B., R.H. Writing—review & editing: F.B., L.M.,
395 J.S., Q.W., K.S., R.H.

396 **Competing interests**

397 The authors declare no competing interests.

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