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1 Characteristics of secondary-ruptured faults in the Aso Caldera 2 triggered by the 2016 Mw 7.0 Kumamoto earthquake

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5 **Abstract**

6 The 16 April 2016 Mw 7.0 Kumamoto earthquake caused prominent fault displacements and crustal
7 deformation, not only around the main rupture faults but also around numerous secondary-ruptured
8 faults. The physics and characteristics of such secondary faulting have not yet been studied in detail.
9 We investigated a set of two secondary faults that appeared at the timing of the Mw 7.0 quake in the
10 Aso Caldera by mainly using synthetic aperture radar interferometry and fault slip modeling. The two
11 faults were found to be associated with surface slip of several centimeters or more, in the oblique sense
12 of right-lateral and vertical. Fault slip inversions found that the slip was dominantly in normal sense
13 with smaller contribution from the right-lateral component. The deeper limit of the slips was estimated
14 to be around 1.3 km, which may coincide with the boundary between the superficial sediment layer and
15 the basement rock. The shallowness of the slip and the difference in the dip angles of the main
16 secondary fault and the Mw 7.0 seismogenic fault suggest separation of the two fault systems, although
17 the fault strike and sense of motions were similar. The amount of slip on the two secondary faults was
18 larger than that expected from the scaling law derived from seismogenic faults, which may indicate the
19 difference in the physics of seismogenic and secondary faultings.

20 **Keywords**

21 Secondary fault, InSAR, Crustal Deformation, 2016 Kumamoto Earthquake

22 **Introduction**

23 The 16 April 2016 Mw 7.0 Kumamoto earthquake, the largest event of the 2016 Kumamoto earthquake
24 sequence, caused prominent fault displacements and crustal deformation. Complex rupture patterns
25 associated with the earthquake were revealed by InSAR (e.g., Fujiwara et al 2016; Ozawa et al 2016),
26 SAR pixel offset analysis (e.g., Himematsu and Furuya 2016; Yue et al 2017), differential Lidar (Scott
27 et al 2018), and field surveys (Goto et al 2017; Kumahara, Y. and Research Group of Inter-University
28 2016; Shirahama et al 2016). Most studies on fault slip estimation using geodetic and seismic data
29 indicated that the maximum fault slip of the earthquake was around 5 meters or larger (e.g., Himematsu
30 and Furuya 2016; Kobayashi et al 2017; Kubo et al 2016; Tanaka et al 2019; Yue et al 2017). Multiple

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31 faults having different dip and rake angles were required to explain the geodetic and seismic data. Such
32 complex faulting has been revealed by modern instruments and analysis techniques also for other crustal
33 earthquakes of similar size (e.g., Elliott et al 2012; Hamling et al 2017; Oskin et al 2012; Wei et al 2011).
34 What makes the Kumamoto earthquake unique was numerous triggered secondary faultings captured by
35 InSAR (Fujiwara et al 2016; Ozawa et al 2016). Fujiwara et al (2016) found approximately 230 secondary
36 surface ruptures, some along previously mapped fault traces, and many others along unmapped locations.
37 Since the deformation around each of the secondary fault did not extend over a broad area, the fault slips
38 must have been limited to shallow depths (Ozawa et al 2016).
39 In this study, we focus on a set of secondary ruptured faults in the Miyaji district located in the northern
40 floor of Aso caldera. Ishimura et al (2017) reported that vertical and dextral displacements of less than
41 10 cm were found in the field along the faults in Miyaji. They also excavated a pit across a surface
42 break and found a nearly vertical fault structure. As stated earlier, the secondary faults do not seem
43 to be connected to the main source fault of the Kumamoto earthquake. If so, how do these secondary
44 faults extend to deeper depths? What is the relation between the rupture depth and the structural
45 properties of the rocks forming the shallow part of the crust? The purpose of this paper is to estimate
46 the fault geometry and slip distribution of the secondary faults in the Aso caldera by inverting InSAR
47 data observed from three different directions, in order to obtain insights on the nature of secondary faults.
48 This paper pairs with Ishimura et al (2020), who presents and discusses the results of a trench survey
49 conducted on the same secondary faults. The set of two studies enables us to deduce insights not only
50 on the ruptures that occurred in 2016 but also on past events including the long-term slip rates.

51 **InSAR Analysis and Features of the Displacement Field**

52 We investigate two faults located in the Miyaji district, Aso City, Kumamoto Prefecture, within the
53 Aso caldera (Figure 1). The targeted faults run in the direction of N50°E, roughly parallel to the main
54 rupture fault of the Mw 7.0 Kumamoto earthquake. Hereafter we call these faults as Miyaji faults.
55 In order to capture displacements around the faults from different directions, three sets of ALOS-2 SAR
56 images obtained along three different line-of-sight (LOS) directions were used to form interferograms
57 (Table 1). According to the local residents, the faulting in Miyaji occurred simultaneously with the Mw
58 7.0 rupture. In principle, measurements from three independent directions enable us to obtain the three-
59 dimensional displacement field, but the north-south component has relatively large uncertainty (Wright

et al 2004; Morishita et al 2016). This limitation is inherent to InSAR, originating from the fact that the LOS horizontal directions are close to east or west (Table 1).

Table 1. ALOS-2 SAR data used for computing the interferograms.

Path	Frame	Satellite Direction	Looking Direction	Incidence Angle ($^{\circ}$)	LOS Horizontal Direction ($^{\circ}$) [†]	Dates (yy.mm.dd)	Perpendicular Baseline (m)
126	670	Ascending	Left	24.4	76	16.04.15-16.04.29	217.1
130	650	Ascending	Right	33.9	260	15.12.03-16.04.21	147.1
23	2950	Descending	Right	36.1	100	16.03.07-16.04.18	125.4

[†] Direction ground to satellite, measured clockwise from North.

We conducted a 2-pass interferometry with RINC software (Ozawa et al 2016). We multi-looked the images by 4 and 7 in the range and azimuth directions, respectively, which resulted in the spatial resolution of approximately 15–20 meters in the two directions. Digital ellipsoidal height model developed by T. Tobita (Geospatial Information Authority of Japan, GSI) and T. Ozawa (National Research Institute for Earth Science and Disaster Resilience of Japan) based on the digital elevation model of the Geospatial Information Authority of Japan was used for geocoding and computation of topographic phase. We used an adaptive spectral filter (Baran et al 2003), followed by median filter (5×5) and mean filter (3×3) to reduce noise. The resulting interferograms show high coherence in the target area (Figure 2). While similar fringe patterns were obtained for Paths 126 and 23 (obliquely from ENE and ESE, respectively), the interferogram of Path 130 (obliquely from WSW) exhibits considerably different fringe pattern. For phase unwrapping of the interferograms (conversion from phase to displacements), SNAPHU (Chen and Zebker 2000) was used. We subsequently converted the relative displacements mapped by the interferograms to absolute (referenced) displacements by using the GNSS displacements as a reference. For that purpose, we used the coseismic GNSS displacements in the SAR line-of-sight (LOS) direction, observed at two stations of the GNSS Earth Observation Network System (GEONET) operated by GSI (Figure 2a-c). The offset for each interferogram was estimated in such a way that the misfit between the corrected InSAR displacements and GNSS displacements was minimized at the GNSS sites. Namely, we estimated the offset l for each interferogram by

$$l = \sum_{i=1}^2 (u_i^{\text{InSAR}} - u_i^{\text{GNSS}}) / 2, \quad (1)$$

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80 where u_i^{InSAR} and u_i^{GNSS} denote the InSAR and GNSS displacements in the LOS direction at the i -
81 th GNSS station location, respectively. For each unwrapped interferograms, the estimated offset was
82 subtracted to produce referenced LOS displacements (Figure 3).

83 We then decomposed the unwrapped and referenced InSAR displacements in three LOS directions to the
84 two horizontal (EW and NS) and vertical displacements, followed by further conversion of the EW and
85 NS components into the horizontal component along N50°E, approximately parallel to the strike of the
86 Miyaji faults.

87 The displacement field along the N50°E horizontal direction (Figure 4a) shows localized displacements
88 around the Miyaji faults, superimposed by broad regional right-lateral movement that mainly resulted
89 from the rupture of the main fault of the Mw 7.0 Kumamoto earthquake. The vertical displacements
90 (Figure 4b), on the other hand, exhibits north-side-down vertical displacements across two strands of
91 faults. More closely looking, each of two strands of faults is composed of multiple smaller faults located
92 *en echelon* (see Ishimura et al (2020) for detailed interpretation). The N50°E horizontal component is
93 noisier than the vertical one because of the relatively large uncertainty in the NS displacements.

94 The profiles of displacements across the faults show clear displacement offsets at the location of the faults
95 (Figure 5). The offsets approximately amount to 5cm and 8cm, for the northern and southern faults
96 respectively, in both vertical and right-lateral profiles. On the northern fault, the maximum vertical and
97 dextral surface slip measured from the InSAR displacements were 8 cm and 19 cm, respectively, whereas
98 those for the southern fault were 12 cm and 19 cm, respectively (Ishimura et al 2020).

99 **Fault Slip Inversion**

100 **Method**

101 Our main interests on the secondary faulting can be summarized by two questions: 1) What are the
102 depths of the slipped portion of the faults? 2) How are the two secondary faults related to each other? To
103 answer these questions, we estimated the fault slip models of the two secondary faults using the inversion
104 procedure developed and conducted in previous studies (Fukushima et al 2013, 2018; Ghayournajarkar
105 and Fukushima 2020). For more detailed explanation on the inversion procedure, see Fukushima et al
106 (2013).

107 For preparation of the inversion dataset, we first removed the regional long-wavelength displacements
108 caused mainly by the fault rupture of the Kumamoto earthquake. The regional displacements were

109 modeled by a two-dimensional cubic polynomial function expressed by

$$d_{trend} = a_1 + a_2x + a_3y + a_4x^2 + a_5xy + a_6y^2 + a_7x^3 + a_8x^2y + a_9xy^2 + a_{10}y^3, \quad (2)$$

110 where a_1, \dots, a_{10} are constants estimated by the least squares method, and x and y are longitude and
 111 latitude. The resulting two-dimensional polynomial function was subtracted from the original to extract
 112 the displacements due to the rupture of Miyaaji faults (Figure 6b). After removal of the long-wavelength
 113 displacements, the data were subsampled with concentric grids (Figure 6c).

114 We used triangular dislocation elements to express curved fault surfaces, and faults were discretized with
 115 an average interval of 200 meters. We solved for the geometry and slip distribution on the northern
 116 and southern secondary faults simultaneously. We assumed that, for each of the northern or southern
 117 fault, the small en-echelon structures mentioned above were connected to a single fault at depth, and
 118 approximated the top of the fault to be a smooth curve close to a straight line. The bottom side of the
 119 fault was assumed to be a straight line parallel to the top side. The lengths of the faults were taken large
 120 enough to cover the extent where deformation was observed in the interferograms. The widths of the
 121 faults were taken large enough after trials and errors so that the slipped area does not reach the bottom
 122 of the assumed faults.

123 We solved for the amount of slip on the triangular elements, dip and rake angles of the two faults, and
 124 the weight of the smoothing of the slip distribution. Slips on the fault elements have linear relationship
 125 to the observed data, whereas the other parameters have nonlinear relationship to the data. This is hence
 126 a mixed linear-nonlinear inverse problem.

127 The likelihood function p was defined as follows (Fukuda and Johnson 2008):

$$p(s, \mathbf{m}, \sigma^2, \alpha^2 | \mathbf{d}) = C(\sigma^2)^{N/2}(\alpha^2)^{-M/2} \exp \left[\frac{1}{2} \left(\frac{1}{\sigma^2} (\mathbf{d} - \mathbf{G}(\mathbf{m})\mathbf{s})^T \Sigma_d^{-1} (\mathbf{d} - \mathbf{G}(\mathbf{m})\mathbf{s}) + \frac{1}{\alpha^2} (\mathbf{L}(\mathbf{m})\mathbf{s})^T (\mathbf{L}(\mathbf{m})\mathbf{s}) \right) \right], \quad (3)$$

128 where C is an arbitrary constant, \mathbf{d} is the data vector (length N), \mathbf{s} is a model vector composed of linear
 129 parameters (slip on the triangular elements, length M), σ^2 is the variance of the data which was set to
 130 $1.0 \times 10^{-4} \text{ m}^2$ based on the calculation in the far-field, α^2 is the weight of the smoothing matrix $\mathbf{L}(\mathbf{m})$,
 131 \mathbf{m} is a model vector composed of the dip and rake angles of the two faults, $\mathbf{G}(\mathbf{m})$ is the design matrix
 132 relating the slip on the fault elements to displacements on the ground surface, and Σ_d^{-1} is the inverse of
 133 the data covariance matrix.

134 Since $\mathbf{L}(\mathbf{m})$ and $\mathbf{G}(\mathbf{m})$ are functions of the geometrical model parameters, these matrices are fixed once

135 the values of \mathbf{m} are fixed. For the design matrix $\mathbf{G}(\mathbf{m})$, we used solutions of angular dislocations in a
 136 homogeneous elastic half-space (Thomas 1993) with an assumption of Poisson’s ratio of 0.25. We adopted
 137 the smoothing matrix defined by Maerten et al (2005), where the operator concerning the i -th element
 138 and the three elements in contact of it is expressed by

$$\mathbf{L}(\mathbf{m})_i = \frac{2}{l_i} \sum_{j=1}^3 \frac{s_j - s_i}{h_{ij}}. \quad (4)$$

139 Here, h_{ij} is the distance between the center of the i -th and j -th elements, s_i and s_j are the i -th and j -th
 140 elements in \mathbf{s} , and $l_i = \sum_{j=1}^M h_{ij}$, where M is the number of elements, is the sum of the distance between
 141 element centers.

142 We assumed that the inverse of the data covariance matrix Σ_d^{-1} was an identity matrix, meaning that
 143 we assumed no spatial correlation of noise. Trials with data correlation taken into account led to models
 144 that had slip deeper than a few kilometers and large residuals in the vicinity of the faults. This problem
 145 occurred probably because taking the data correlation into account is equivalent to placing less weight
 146 into short-scale variations in data; that is, the inversion algorithm attempted to search for models that
 147 fit with relatively small amplitude of large wavelength noise variations rather than the short wavelength
 148 signal around the faults.

149 The nonlinear parameters were solved using Particle Swarm Optimisation (PSO) (Eberhart and Kennedy
 150 1995). PSO is a Monte-Carlo search algorithm and it evaluates the likelihood function for many sets of
 151 nonlinear parameter values. For each set, the slip distribution (values of slip on the fault elements) on
 152 each fault was solved with a damped least-squares method with non-negativity constraints. The misfit
 153 of the least-squares inversion was used to evaluate the likelihood function.

154 As for the model uncertainties, neighbourhood approximation and Monte-Carlo integration of the like-
 155 lihood function (Equation 3) was performed to form the probability density function (Sambridge 1999),
 156 and the standard deviation of the slip distribution was calculated from the diagonal elements of the
 157 model covariance matrix. The 95% confidence intervals of the non-linear parameters were calculated
 158 by discarding the top and bottom 2.5% of the one-dimensional marginal probability density functions
 159 (Fukushima et al 2013).

160 **Results**

161 The convergence of the nonlinear parameters (Figure 7 top) and the one-dimensional marginal probability
 162 distribution of the parameters (Figure 7 bottom) show that wide ranges of model parameters were searched

163 and the search converged toward one single set of model parameters, leaving a clear peak in each marginal
164 probability distribution. The dip angle of the northern fault was less constrained compared with the
165 southern one (Table 2), but the difference in the confidence intervals indicate that the northern fault is
166 dipping steeper than the southern one. The dip angles of the northern and southern faults were 63° and
167 42° , respectively, for the maximum likelihood model. As for the rake angles, similar values of around
168 240° were estimated for the two faults, indicating dominantly normal faulting with smaller amount of
169 right-lateral slip.

Table 2. Confidence intervals and maximum likelihood model parameters.

	Lower Bound	Maximum Likelihood	Upper Bound
Dip (N)	47°	63°	90°
Dip (S)	35°	42°	50°
Rake (N)	227°	245°	269°
Rake (S)	233°	237°	244°
$\log \alpha^2$	0.74	2.15	3.97

170 The geometry and slip distributions of the faults of the maximum likelihood model and the uncertainty
171 of slip are shown in Figures 8 and 9. Larger dip angle for the northern fault means that the two faults
172 are converged at depth, forming splay fault branching. It is worth pointing out that the convergence
173 depth coincides with the deeper limit of the slipped area of the southern fault. One should note, however,
174 that our results do not warrant the connection of the two fault at depth because the shallow slip on the
175 northern fault do not extend down to the depth where two fault surfaces are converged. This set of fault
176 slip models well explains the data (Figure 10).

177 The estimated slip extends from the surface to ~ 0.5 km with a peak slip of 11 cm, and to ~ 1.3 km with
178 a peak slip of 19 cm, for the northern and southern faults, respectively. For the northern fault, the
179 maximum standard deviation was 3.7 cm, whereas the standard deviation for most of the southern fault
180 elements shallower than 1.5 km was less than 5 cm (Figure 9). The estimated slip at most area along the
181 faults can be considered real, given the small amount of standard deviation of slip.

182 The moment magnitudes for the northern and southern faults amount to 3.52 and 4.36, respectively.
183 Here we assumed the rigidity of 6.2 GPa calculated from the density of $1,900 \text{ kg/m}^3$ (Komazawa 1995)
184 and the shear velocity of 1.8 km/s (Abe et al 2010). As far as the authors are aware, the smallest moment

185 magnitude of surface-rupturing earthquakes found so far in the world is Mw 4.7 of the 2007 Katanning
186 earthquake in Australia (Dawson et al 2008; King et al 2019), highlighting the peculiarity of the secondary
187 ruptures.

188 **Discussion**

189 **Relation to the subsurface structure**

190 The superficial structure beneath the northern part of the Aso caldera floor, also called the Aso Valley,
191 consists of sediments deposited in the caldera lake underlain by the pumice flow from the Kuju volcano
192 (Matsumoto and Fujimoto 1969). Further down, basement rock of granite has been identified deeper
193 than ~500 meters near the northern rim of the caldera (Matsumoto and Fujimoto 1969).

194 Beneath the location of the Miyaji faults, the data of gravity (Komazawa 1995; Miyakawa et al 2016),
195 seismic velocity structure (Sudo and Kong 2001; Abe et al 2010), and electrical resistivity (Handa et al
196 1998; Hase et al 2005; Hata et al 2016, 2018; Matsushima et al 2020) altogether indicate a low-density
197 (porous having high water content) superficial layer of 1 to 2 km, which can be attributed to the lake
198 deposits and pumice flow.

199 The consistency between the thickness of the superficial sediment layer and the depth extent of the
200 estimated slip (~1.3 km) indicates that the fault ruptured the sediment layer. Although our results
201 cannot exclude the possibility that the fault extends further down, it is more likely that Miyaji faults are
202 “root-less” and cause minor ruptures within the superficial layer, considering the fact that the slip of the
203 penultimate event was almost the same as the 2016 one (Ishimura et al 2020).

204 The optimal dip angle of the northern and southern faults were 63° and 42°, respectively. Since the dip
205 angles found in the trench were nearly vertical (Ishimura et al 2020), it is implied that the Miyaji faults
206 are listric. The dip angle of the main southern fault is smaller than the Futagawa fault responsible for
207 the Mw 7.0 Kumamoto main rupture, estimated in a range of 65°–79° (Kubo et al 2016; Himematsu and
208 Furuya 2016; Ozawa et al 2016; Yue et al 2017). This supports the lack of continuation of Miyaji faults
209 to the main Futagawa fault structure.

210 **Effect of Earth’s layered structure**

211 The deformation field in the crust due to faulting is dependent on the properties of the surrounding
212 medium. It has been known that ignoring the effect of layering biases the estimated fault depth to be
213 shallower than the actual depth, when the fault is located beneath a compliant surface layer (Cattin et al

1999; Savage 1998; Segall 2010). In our case, the faults are inferred to be located in a compliant surface layer overlain by stiffer bedrock. We performed a synthetic test to evaluate the degree of bias in the depth and dip angle estimated under the simplified assumption of homogeneous half-space.

As the actual fault slip, we assumed a uniform slip of 1 m on a rectangle reaching the ground surface with length of 2 km, dip angle of 45°, and rake angle of 240°. We tested with different widths, hence with different bottom depths of the faulting.

We assumed that the Earth is formed by a compliant layer of 2 km thickness having rigidity of 6.2 GPa and a half-space beneath it having rigidity of 33 GPa; the latter was given based on the shear velocity of 3.5 km/s (Abe et al 2010) and the density of 2,700 kg/m³ (Komazawa 1995) (Figure 11a).

The observation points were assumed to be distributed in a concentric grid, similar to the data we used for the inversion. The eastern, northern, and vertical displacements at the observation points were calculated by the EDGRN/EDCMP package (Wang et al 2003) (Figure 11b-d).

The three-dimensional displacements were inverted to estimate the fault width and dip angle using PSO for each case of actual fault width. The results revealed that the effect of layering was minor for our studied case (Figure 12). When the actual width was smaller than or equal to 1.0 km, the estimated width was nearly equal to or slightly smaller than the actual width. When the actual width was larger than 1.0 km, the estimated width was slightly larger than the actual width. The maximum degree of overestimation was 7.5% (for the case where the actual width was 1.5 km). As for the dip angle, non-systematic deviation of less than 2.5 degrees from the actual dip angle was observed when the actual width was smaller than 0.5 km, which probably resulted from relatively small number of points on which deformation was observed. Systematic underestimation of approximately one degree or less was observed when the actual width was larger than or equal to 0.5 km.

From the synthetic test, we conclude, for the purpose of this research, that the assumption of homogeneous half-space and hence the discussion on the rupture depth made in the previous section were valid.

Fault scaling

Wells and Coppersmith (1994) derived empirical relationships among magnitude, rupture length and width, rupture area, and average displacement, from 244 historical events in the world. Wells and Coppersmith (1994) gave, for strike-slip and normal faults,

$$\log(\text{MD}_s) = -1.69 + 1.16 \log(\text{SRL}_s), \quad (5)$$

242 and

$$\log(\text{MD}_n) = -1.98 + 1.51 \log(\text{SRL}_n). \quad (6)$$

243 where MD_x and SRL_x ($x=s$ for strike-slip and $x=n$ for normal slip) correspond to the maximum surface
244 slip (m) and surface rupture length (km), respectively. Substituting the approximate surface rupture
245 lengths of 1 km and 2 km of the northern and southern faults in Miyaji, the expected amount of strike-slip
246 would be 2.0 cm and 4.6 cm, respectively, and that of normal slip would be 1.1 cm and 3.0 cm, respectively.
247 The amount of maximum dextral surface slip measured from the InSAR displacements on the northern
248 and southern faults was, on the other hand, 8 cm and 19 cm, respectively, and that of normal slip was
249 12 cm and 19 cm, respectively (Ishimura et al 2020). The large deviations of the observed values from
250 the relationship of Equation (5) and (6) may indicate that secondary faults tend to slip more than the
251 average of seismogenic faulting. Whether this tendency is a ubiquitous characteristic is an intriguing
252 question to be investigated in future studies.

253 **Conclusions**

254 The Mw 7.0 Kumamoto earthquake triggered numerous secondary faultings. We obtained detailed fault-
255 parallel and vertical displacement fields around a set of two secondary-ruptured faults in Miyaji located
256 in the Aso caldera by conducting InSAR analysis using the ALOS-2 SAR data. The results revealed
257 clear dextral and vertical slip offsets across the two faults.

258 By conducting fault slip inversions, we further found that the northern and southern faults ruptured
259 down to ~ 0.5 km and ~ 1.3 km, with the optimal dip angles of 65° and 42° , respectively. The two faults
260 seemed to form a splay structure whose connection depth lay at ~ 1.3 km. The deeper limit of the rupture
261 may correspond to the base of the superficial sediment layer. The shallowness of the ruptures as well
262 as the difference in the dip angles of the main southern fault and the steeper dip angle of the Futagawa
263 fault, the main seismogenic fault responsible for the Mw 7.0 quake, suggest that the secondary faults are
264 separated from the seismogenic fault system.

265 Our analysis suggested that the slip on the Miyaji secondary faults was larger than expected from
266 the scaling law proposed for seismogenic faults (Wells and Coppersmith 1994). Systematic studies of
267 secondary faulting, being detected for the Kumamoto earthquake case (Fujiwara et al 2016; Ozawa et al
268 2016) and other earthquakes by InSAR and differential Lidar techniques, will be able to elucidate the
269 characteristics of secondary faults and provide insights into the physics of faulting.

270 **Declarations**

271 **Ethics approval and consent to participate**

272 Not applicable

273 **Consent for publication**

274 Not applicable

275 **List of abbreviations**

276 **ALOS-2** Advanced Land Observing Satellite 2

277 **InSAR** Interferometryc Synthetic Aperture Radar

278 **LOS** Line of sight

279 **GEONET** GNSS Earth Observation Network System

280 **GSI** Geospatial Information Authority of Japan

281 **PSO** Particle Swarm Optimisation

282 **SAR** Synthetic Aperture Radar

283 **Availability of data and materials**

284 The datasets used and/or analyzed during the current study are available from the authors upon request.

285 **Competing interests**

286 The authors declare that they have no competing interests.

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290 **Authors' contributions**

291 YF led the preparation of the paper and conducted InSAR analysis and modeling. DI conducted field
292 survey and discussed the geological interpretation of the modeled results. All authors read and approved
293 the final manuscript.

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