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Spatio-temporal clustering of successive earthquakes: analysis of a global CMT catalog.

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21 **Abstract**

22 Spatio-temporal clustering of seismicity features is an interesting phenomenon that is
23 relevant for earthquake generation process and operational earthquake forecasting. We analyze
24 successive earthquakes that closely occur in space and time in order to clarify how large earthquakes
25 successively occur. We use the Global Centroid Moment Tensor catalog for the period from 1976 to
26 2016. Shallow earthquakes with a moment magnitude, M_w , of larger than or equal to 5.0 are analyzed.
27 We first sort all of the earthquakes in time to select a master event from the beginning. Then, we group
28 the earthquakes that occur within a horizontal distance (D) and a lapse time (T_a) from the master event
29 into a cluster. Next master event is selected from the catalog in order, and the same procedure is repeated.
30 We count the number of the clusters, which represent the successive earthquakes, for different D and
31 T_a . To examine whether or not successive earthquakes randomly occur, we compare the results with
32 simulations in which earthquakes are set to occur randomly in time but at the locations same with the
33 estimated centroid. The results show that the cumulative numbers of clusters for the simulation more
34 rapidly increase with the horizontal distance than those for real data at short distance ranges, and the
35 formers approach to the latter at long distance range. The triggering distance, at which the cumulative
36 numbers of real and simulation data merge, increases with increasing the magnitude of master event.
37 The triggering distance becomes smaller as the lapse time increases, which implies that the seismic
38 activity turns to become the normal condition in which the occurrence time intervals of large
39 earthquakes obey a Poisson distribution. The triggering distance increases with being almost
40 proportional to the 1/3 of the seismic moment of master earthquake, and the number of earthquakes
41 occurring in the region with positive Coulomb stress change (ΔCFF) are more than 60-80% of the total
42 number of the successive earthquakes. These results suggest that static stress change introduced by a
43 master event is one of the triggering mechanism of successive earthquakes.

44

45 **Key words:** Spatio-temporal clustering, successive occurrence, triggering distance, Coulomb stress
46 change.

47

48 **1. Introduction**

49 Some earthquake forecasting models are rooted in the idea that earthquakes can generate
50 other earthquakes and the triggering probability depends on space, time, and magnitude. A well-known
51 classical empirical scaling law is Omori law, which states that the occurrence rate of earthquakes after
52 a large earthquake (i.e., mainshock) decays with being proportional to t^{-p} where t is the time and p a
53 constant of about 0.7 – 1.1 (Utsu, 2002). Also, Gutenberg-Richter's law (Gutenberg and Richter, 1944),
54 which describes the magnitude-frequency distribution of earthquakes, is used in these methods. Another
55 empirical law, Bath law, is also important to understand the occurrence of earthquakes after a large
56 earthquake, which shows that the magnitude of the largest aftershock is about 1.2 less than that of the
57 main shock (Bath, 1965). For these decades, seismologists have investigated the spatio-temporal
58 distribution of seismicity based on these empirical characteristics. For example, epidemic type
59 aftershock sequence model (ETAS model; Ogata, 1998), which is based on the Omori law, Gutenberg-
60 Richter law and an idea that an earthquake generates a cluster of offspring earthquakes, has been applied
61 to the earthquakes at many regions to understand the regional or general characteristics of seismicity
62 and to evaluate the seismic hazard (e.g, Console and Murru, 2001; Helmstetter and Sornette, 2002;
63 Ogata and Zhuang, 2006; Kumazawa and Ogata, 2014).

64 Statistical characteristics of the seismicity is also examined by considering that spatio-
65 temporal distribution of earthquakes is independent of the dimensions of the region under consideration
66 and independent of the seismic magnitude (Kagan and Knopoff, 1980; Corral, 2004a; Marekova, 2014).
67 For instance, at Southern California, where high-quality seismic data are available for recent several
68 decades, both the inter-event distances (distance between earthquakes) and the inter-event times
69 (occurrence time difference between earthquakes) exhibit statistical distributions involving power-law
70 regimes (Bak et al. 2002; Corral, 2004a, 2004b; Corral, 2008; Davidsen and Paczuski, 2005). The
71 statistical characteristics of spatio-temporal distribution of seismicity is often examined by giving a
72 focus on the characteristics of main shock and aftershock sequences (Utsu and Seki, 1954; Utsu et al.,
73 1995; Felzer and Brodsky, 2006; Yukutake and Lio, 2017; Nicole, 2018; Tamaribuchi, 2018). Static or
74 dynamic stress changes is often used to explain these triggered seismicity (Gomberg et al. 1998; Hill et
75 al., 1993; Kilb et al., 2000; Toda et al. 2008, 2011; Freed, 2007)

76 On the other hand, there are some phenomena that are not well described by the classical
77 laws or ETAS model and/or by the statistical characteristics. For example, it is known that large
78 earthquakes are sometimes preceded by foreshocks: about 10 - 20 % of the main shocks with $M_w \geq 6$
79 accompany foreshocks (Reasenber, 1999). But, it is realized again that some of the foreshocks have a
80 magnitude larger than 6, which may severely cause earthquake disasters. For example, in Japan, two
81 days after an $M_w 7.3$ earthquakes, the 2011 Tohoku earthquake with magnitude $M_w 9.0$ occurred along
82 the Pacific plate boundary (Marsan and Enescu, 2012); an $M_w 6.5$ earthquake hit at Hinagu active fault

83 in Kyushu, Japan, on April 14, 2016, was followed by a large earthquake with M_w 7.3 that took place at
84 Futagawa active fault on April 16 (Goda et al., 2016). These large earthquakes may be classified as a
85 foreshock of the following main shock (Utsu, 1954). It is, however, natural that such a large foreshock
86 exceeding magnitude of about 6 is generally recognized as a main shock before the occurrence of the
87 following larger earthquake. It is also known that large earthquakes are sometimes successively
88 observed, which may not be explained by Bath's law and may not be attributed to the classical
89 aftershock activity. For example, along the Anatolian active fault system in Turkey, four large
90 earthquakes with magnitudes of $M_w > 7.0$ successively occurred for the period from 1939 to 1944 and
91 three for the period from 1953 to 1967. For 5 years after the 2004 Sumatra earthquake with an M_w 9.2,
92 three large earthquakes with $M_w > 7$ occurred along the plate boundary of Indian oceanic plates and
93 Sumatra Island in Indonesia: the M_w 8.7 Nias earthquake on March 28, 2005, which occurred directly
94 to the south of the rupture area of the Sumatra earthquake, the double earthquakes on September 12,
95 2007, the first M_w 8.5 at 11:10:26 occurred about 130 km southwest of Bengkulu on the southwest coast
96 of Sumatra island. On the same day, the second M_w 7.9 at 23:49:04 occurred about 205 km northwest of
97 Bengkulu and about 185 km south–southeast of Padang, in West Sumatra.

98 The present study, therefore, analyzes moderate and large earthquakes to clarify spatio-
99 temporal characteristics of successive earthquakes, which are defined in this study as that the
100 earthquakes occur close to each other both in space and time and may not be attributed to the aftershocks.
101 The present study uses a global earthquake catalog to examine the occurrence probability of another
102 earthquake after a previous one and clarify averaged characteristics of successive earthquakes. The
103 Coulomb stress change (ΔCFF) hypothesis is also examined to understand the generation mechanism
104 of these successive earthquakes. These evaluations can be important not only to understand the
105 earthquake triggering mechanisms but also to prepare for seismic hazards, because the second
106 earthquake can cause severe damages and disaster again in and around the area where a first large
107 earthquake occurs.

108

109 2. Data

110 We use the data catalog of centroid moment tensor (CMT) solutions provided by the
111 Global CMT project operated by Columbia University (Dziewonski, A. M., et al.; 1981; Ekström, G.,
112 et al.; 2012). CMT solutions of earthquakes have routinely been determined from analyses of observed
113 seismic waves recorded at stations distributed around the world, and the centroid, occurrence time and
114 moment magnitude of earthquakes occurring around the world are provided. The data for the period of
115 41 years from 1976 to 2016 are analyzed in the present study. Since CMT solutions are determined for
116 relatively large earthquakes that excite long-period waves propagating in a long-distance, there is no
117 omission in the data catalog for the earthquakes with a magnitude of equal to or larger than about 5.

118 This can be confirmed from the magnitude frequency distribution that follows Gutenberg-Richter's
119 relation (e.g., Nishimura, 2017). The present study, therefore, gives attentions into the earthquakes with
120 a magnitude larger than or equal to 5.

121

122 3. Method for searching successive earthquakes

123 The present study defines the successive earthquakes as plural earthquakes that occur close
124 to each other both in space and time and are not attributed to the aftershocks. We search such successive
125 earthquakes by using the following steps: (1) Sort the earthquakes in the CMT data catalog in time; (2)
126 a start time is set to be the beginning time of the catalog; (3) A master event with a moment magnitude
127 (M_w) ranging from M_{w1} to M_{w2} is selected in order from the start time. The earthquake is termed as
128 E_o^i , where i represents the number of master event; (4) When an earthquake larger than E_o^i occurs
129 within an interval time of t_b before the occurrence of E_o^i and within a distance of 2000 km from the
130 centroid of E_o^i , E_o^i is unused as a master event, and we go to step 7; (5) The earthquakes satisfying the
131 following two criteria are searched, and are defined as a triggered event belonging to the “cluster” of
132 E_o^i : (i) the earthquake occurs within a lapse time of T_a from the occurrence time of E_o^i ; (ii) the
133 horizontal distance from the epicenter of E_o^i is in the range from the minimum distance D_{min} to the
134 distance D ; (6) The start time is set to be just after the occurrence time of the i -th master event, and go
135 to step 3 to select a next master event ($i+1$) which is not belonging to the clusters previously determined;
136 (7) The procedures from steps (3) to (6) are repeated until the last earthquake in the catalog. We define
137 the earthquakes belonging in each cluster as “successive earthquakes”.

138 The time interval, t_b , which is used to remove the main shocks, is set to be 14 days,
139 because most of the largest aftershocks occur within 10 days after the occurrence of each main shock
140 (Utsu, 1957). Following Utsu and Seki (1954), we set the minimum distance, D_{min} , using the following
141 equation : $D_{min} = c\sqrt{A/\pi}$, where A is the slip area in km^2 determined from the magnitude of the
142 master event: $\log_{10} A = 1.02M_w - 4.0$. To sufficiently exclude the aftershocks of master event, we set
143 the coefficient c to be 3. Because the selection of main shocks may change the selection of aftershocks
144 (Felzer and Brodsky, 2006; Marson and Lengliné, 2010), we examine the effect of t_b and/or of c in
145 the following analyses.

146 Figure 1 illustrates how we define the master events using t_b and D (Steps 3 and 4), and
147 Figure 2 schematically shows how the number of cluster changes with the interval time T_a and the
148 distance D (Step 5). By counting the number of clusters and examining the distributions of cluster in
149 space, we clarify the characteristics of successive earthquakes in the following sections.

150

151 4. Results

152 4.1 Spatio-temporal distributions of successive earthquakes

153 We divide the earthquakes in the catalog into five magnitude ranges: $5.0 \leq M_w < 5.5$
154 (25299 earthquakes), $5.5 \leq M_w < 6.0$ (9186 earthquakes), $6.0 \leq M_w < 6.5$ (2753 earthquakes),
155 $6.5 \leq M_w < 7.0$ (931 earthquakes) and $M_w \geq 7.0$ (419 earthquakes). We count the number of
156 clusters for three lapse times ($T_a=60, 180$ and 365 days). The horizontal distance ranges (D) are also
157 changed: every 10 km from 10 to 500 km for the first two magnitude ranges ($M_w < 6.0$) and every 100
158 km from 100 to 2000 km for the other magnitude ranges ($M_w \geq 6.0$). Most of cumulative numbers of
159 clusters constantly increase with increasing the lapse time, T_a and with increasing horizontal distance
160 (Figure 3). But, for the magnitude ranges of $M_w < 6.5$, the cumulative numbers of clusters decrease in
161 the ranges of large T_a and/or large D . For example, for $5.0 \leq M_w < 5.5$, the cumulative number
162 begins to decrease from 120 km for all the lapse times. Such decreases are caused by that plural clusters
163 get together by extending the horizontal distance and increasing lapse time.

164 We may categorize the clusters into two groups: pair-event clusters and multiple-event
165 clusters. The former consists of a master event and another slave event, while the latter is formed by a
166 master event and two or more slave events. For $M_w \geq 7.0$, at least 70% of the clusters are categorized
167 as pair-event clusters at $T_a = 365$ days. The percentage of pair-event cluster decreases with decreasing
168 the earthquake magnitude ranges: 60% for $6.5 \leq M_w < 7.0$ and 38% for $6.0 \leq M_w < 6.5$. In
169 addition, almost half of the clusters show that the master event is followed by one or more slave events
170 with a larger magnitude. For example, for $M_w \geq 7.0$ and at $D= 500$ km, 8 clusters among 13 ones
171 include larger earthquakes than the master events at $T_a = 60$ days, 12 among 27 clusters at $T_a=180$
172 days, and 15 among 39 clusters at $T_a=365$ days.

173 **4.2 Comparison with the results obtained from random data**

174 Temporal distribution of large earthquakes is well described by a Poisson process when
175 aftershocks are excluded (e.g. Michael, 2011; Shearer and Stark, 2012). Hence, the results shown in the
176 previous subsection may be explained by such a random process, and no triggering mechanism may
177 exist. Here, we analyze simulated data to examine whether the observed successive earthquakes occur
178 randomly, or they are triggered by nearby earthquakes. Simulated data catalogs of earthquakes are
179 generated by randomly changing the origin times of the observed earthquakes while their centroids and
180 magnitudes are fixed (not changed from the observations). That is, the origin times are randomly set for
181 the observation period from 1976 to 2016 by using a random function in a computer code that can
182 generate random values equally distributing between 0 and 1. Then, the numbers of clusters are counted
183 by applying the same procedure as used for the real catalog. The simulations are done 100 times, and
184 the average numbers of clusters are calculated. In Figure 3, the spatio-temporal variation on the
185 cumulative numbers of clusters for simulated catalogs are plotted by dotted lines. The cumulative
186 numbers of clusters for the simulation more rapidly increase with the horizontal distance than those of
187 real data at short distance ranges. The cumulative numbers for the simulated data then approach or

188 become equal to those for the real data. Alternatively, the numbers of clusters for the real data are
189 always larger than those for the simulated data at shorter distance ranges, and merge to those for the
190 simulated data at long distance ranges. This result strongly suggests that the earthquakes trigger another
191 or more earthquakes in shorter distance ranges. The first intersection point where the number of
192 cumulative clusters obtained from the real data merges with that obtained with the simulated data
193 represents the distance where triggering ceases. We define this distance as “triggering distance”. For
194 example, the triggering distances are 200 km and 100 km at $T_a = 180$ days and $T_a = 365$ days,
195 respectively, for $6.0 \leq M_w < 6.5$. Those are 300 km and 200 km at 180 and 365 days for $6.5 \leq M_w <$
196 7 , respectively.

197 Figure 4 plots the triggering distances versus the seismic moment M_o that is calculated
198 from an equation of $M_w = (2/3)(\log M_o - 9.1)$ (Hanks and Kanamori, 1979; Bormann, P., and D.
199 Giacomo, 2010). To convert the magnitude range to M_w , we use the average moment magnitude
200 calculated from all the earthquakes in each magnitude range. The triggering distance increases with
201 increasing the magnitude of master event while the triggering distances decrease with increasing lapse
202 time, T_a . Alternatively, a large earthquake can trigger an earthquake located far from his centroid
203 compared to small earthquakes, and triggering effect gradually diminishes with time around a large
204 earthquake. The triggering distance is almost proportional to 1/3 of the seismic moment.

205 Table 1 summarizes the percentages of successive earthquakes that occur within a
206 horizontal distance equal to the triggering distances for the all of the observed earthquakes. The
207 percentages for small earthquakes are large compared with those for large earthquakes, as the
208 percentages are about 5 % for $M_w \geq 7$ while those are about 40 % for $5.0 \leq M_w < 5.5$.

209 Figure 5 plots the locations of the successive earthquakes. It is recognized that these
210 successive earthquakes are distributed not only along subduction zones but also along rift zones. No
211 systematic localization is recognized.

212

213 **5. Discussion**

214 **5.1 Effects of the selection of parameters**

215 Parameters, t_b and c , play a key role in the selection of master events that are used as a
216 first event in each cluster and consequently for the selection of successive earthquakes that belong to
217 that cluster. For example, using smaller c introduce larger numbers of the clusters, and the cumulative
218 numbers especially in the small horizontal distance range are much changed. Hence, the judicious
219 choice of these two parameters must surely help to avoid an overestimation or underestimation of the
220 triggering distance. However, ambiguity remains in the selections of these parameters and there is no
221 robust criterion to define these parameters. In this subsection, therefore, we examine how these two

222 parameters affect the detection of successive earthquakes and estimation of triggering distances. We
223 analyze the real data by changing t_b from 14 days to 60 days, keeping $c=3$. We also examine the
224 effects of aftershock area by changing the parameter c from 3 to 1, fixing t_b at 14 days. Figure 4
225 shows the triggering distances estimated for different t_b and c . The triggering distances for $t_b=30$
226 or 60 days are not the same with those for $t_b=14$ days, but the differences are less than about 10 % at
227 each magnitude range (Figure 4(a)). Similar characteristics are observed for the parameter c (Figures 4
228 (b)). Decreasing c or increasing t_b does not introduce any significant bias in the estimation of
229 triggering distance. These results strongly suggest that the triggering distance is a stable parameter that
230 is not much affected by the selections of the parameters describing the aftershock activity (i.e., t_b and
231 c).

232 Using these two parameters (i.e., t_b and c) can reduce the possibility to include so called
233 aftershocks among successive earthquakes. Nevertheless, some aftershocks of a very large earthquake
234 may be contaminated as successive earthquakes in other magnitude ranges. Or, a main shock is defined
235 as a slave event of a foreshock with a large magnitude. For example, the Tohoku earthquake with
236 $M_w 9.0$ on March 11, 2011, occurred after a foreshock with $M_w 7.3$ on March 9, and are followed by
237 many aftershocks with $M_w \geq 7$. In the case of the magnitude range $M_w < 7.5$, these $M_w \geq 7$
238 earthquakes are not counted as successive earthquakes, because those earthquakes occurred within a
239 distance less than D_{\min} ($=741$ km) are removed as the aftershocks of the $M_w 9.0$ earthquakes by the
240 procedure shown in section 3. But, when the magnitude range is set to be $7 \leq M_w < 9.5$, the $M_w 9.0$
241 is defined as a slave event of the $M_w 7.3$ on March 9 with the following slave events ($M_w 7.9$ and
242 $M_w 7.6$ occurred on March 11, 2011) which must be classified as the aftershocks of $M_w 9.0$. However,
243 even if these $M_w 7.9$ and $M_w 7.6$ are not counted as successive earthquakes, the number of clusters does
244 not change. Also, we have checked that, for the cases in which large earthquakes with $M_w \geq 7$ are
245 followed by other such large earthquakes, the following earthquakes are removed as aftershocks by the
246 procedure section 3.

247 In Figure 3, the curves of cumulative numbers of clusters for large magnitude ranges and
248 short lapse times are represented by straight lines in log-log plots (power laws), while those for small
249 magnitude ranges and long lapse time tend to show convex shapes. Such difference may be caused by
250 the effect of background seismicity: the background seismicity comes to be dominant as the lapse time
251 increases and/or the magnitude range decreases (Richards, et al., 2010). There is no direct way to
252 exclude such background seismicity effect in our analyses, but the curves of cumulative numbers for
253 the simulated data show similar characteristics. Hence, the estimated triggering distance is considered
254 to be not much affected by the background seismicity.

255

256 5.2 Stability of the Simulated data

257 To measure the triggering distances, we performed 100 times of simulation and obtained
258 averaged cumulative numbers of clusters against the horizontal distance. This makes a stabilized
259 simulation result, but the real data is also just one sample so that the obtained clusters may be a result
260 of fluctuated phenomena. Therefore, to examine how the triggering distances are stably estimated, we
261 evaluate the fluctuation of estimation by measuring the triggering distance by analyzing each simulation
262 data. Figure 6 shows the frequencies of triggering distance obtained from 100 simulated data for T_a
263 =180 and 365 days, $c=3$ and $t_b = 14$ days. The triggering distances are scattered in a few hundred
264 kilometers, although the peaks of the frequencies are almost matched with the triggering distances
265 obtained from the averages of 100 simulations. As the magnitude or lapse time increases, the scatter
266 seems to become smaller. This suggests that large number of data may decrease the scatter and improve
267 the reliability.

268 5. 3 Relation to Coulomb stress change

269 Several mechanisms have been proposed to explain the observed spatio-temporal
270 clustering of earthquakes. Static stress change caused by deformation in the vicinity of a large
271 earthquake may change the Coulomb stress changes on the seismic fault planes (i.g., King et al., 1994;
272 Stein, 1999, Hardebeck et al. 1998; Gomberg, 2005, Toda, 2011). Dynamic stress change associated
273 with the passage of seismic waves excited by a large earthquake is also another possible mechanism to
274 trigger nearby earthquakes (e.g., Felzer and Brodsky, 2006). Viscoelastic relaxation, which is caused
275 by viscous flow in the lower crust or upper mantle after the occurrence of a moderate to large earthquake
276 may also change the stress condition of fault plane (e.g., Freed and Lin, 2001). Large earthquakes may
277 migrate crustal fluids to generate fluid pore diffusion. Such process may decrease the normal stress on
278 seismic faults in the crust or plates and lead to trigger other earthquakes (Sibson et al., 1975; Sibson,
279 1981; Hickman et al., 1995). Among them, we examine the Coulomb stress changes caused by large
280 earthquakes as a triggering mechanism of nearby large earthquakes, because many various case studies
281 support the static stress change as one of the most probable earthquake triggering mechanism
282 (Hardebeck et al. 1998; Toda et al. 2008, 2011; Ishibe et al. 2017).

283 The change of Coulomb failure function (ΔCFF) is defined as $\Delta CFF = \Delta\tau + \mu'\Delta\sigma$,
284 where $\Delta\tau$ is the shear stress change, $\Delta\sigma$ is the normal stress change and μ' is the apparent coefficient of
285 friction [e.g., Reasenber and Simpson, 1992]. We calculate ΔCFF for two nodal planes of a slave event
286 by using a moment tensor solution of its master event. We calculate ΔCFF using Coulomb3.3 program
287 provided by USGS (<https://www.usgs.gov/software/coulomb-3>). Since Global CMT catalog only
288 provides a moment tensor solution assuming a point source, we assume an appropriate fault length, L ,
289 and width, W , of a master event by using an empirical relation on the magnitude and fault size presented
290 in Wells and Coppersmith (1994): $L = 10^{-3.22+0.69*M_w}$ and $W = 10^{-1.01+0.32*M_w}$. We make all
291 calculations in an elastic half-space with a shear modulus 3.2×10^4 MPa, a Poisson's ratio of 0.25 and

292 $\mu' = 0.4$. The source is assumed to be the master event of each cluster and the receivers are all slave
293 events belonging to that cluster. We only analyze the earthquakes with magnitude of larger than 6.

294 Figure 7 shows the frequency distributions of ΔCFF for the three magnitude ranges
295 calculated on the two candidate fault planes. Most of the ΔCFF are distributed around 0 Pa, but
296 positive ΔCFF tends to be distributed in a wider range than negative ones. The percentages of positive
297 ΔCFF for the first fault plane are 80% for $6.0 \leq M_w < 6.5$, 69% for $6.5 \leq M_w < 7.0$ and 60% for
298 $M_w \geq 7.0$, respectively, and those for the second fault plane 77%, 72%, and 62%, respectively. This
299 result suggest that Coulomb stress change may play a role on the generation of triggered earthquakes.
300 However, when 10^3Pa is used as a threshold stress for triggering successive earthquakes, which is
301 the same order of the stress perturbation generated from the solid earth tide that may trigger earthquakes
302 (e.g., Tanaka et al., 2002a and 2002b), the percentage of the slave events that satisfy the triggering
303 condition decrease down to about 40 to 45 % for the magnitude ranges of larger than 6.

304
305 About 27 % of slave events occurred in the region with negative ΔCFF . Also, the triggering
306 distances decreases with lapse time. These may not be explained by the triggering mechanism of static
307 stress changes caused by master events. Triggering mechanism of, for example, dynamic stress (strong
308 motion) by main shock, slower deformation processes due to visco-elastic behavior in crust and mantle,
309 and the ambient stress field due to plate tectonic motion, or unknown process may explain such
310 triggering.

311

312 5. Conclusion

313 We have systematically examined the spatio-temporal clustering of earthquakes after the
314 occurrence of a moderate or large earthquake by analyzing one of the most reliable modern seismic data
315 catalog of centroid moment tensor solutions. We examined the number of earthquakes that closely
316 occurred in a space and time from master earthquakes and compare the results with those obtained from
317 the simulated data in which the earthquakes randomly occur in time. The results show that the large
318 earthquakes trigger nearby large earthquakes beyond so called aftershock areas. The triggered
319 earthquakes are about 5 to 40 % of all the earthquakes for the magnitude ranges of $5 \leq M_w < 9.5$,
320 which are distributed not only along subduction zones but also along rift zones. Triggering distances,
321 which defines the distance from the master earthquake to triggered earthquakes, increase with
322 increasing the magnitude of master earthquake, and decrease with increasing the lapse time. The
323 triggering distance increases with being proportional to the 1/3 of the seismic moment of master
324 earthquakes. More than 60% of the triggered earthquakes occur in the region with positive ΔCFF caused
325 by master event. These results suggest that static stress changes may generate successive large
326 earthquakes. The estimated percentages of the successive earthquakes for magnitude range and

327 horizontal distance from the master large earthquake can be used for evaluating an occurrence
328 possibility of next large earthquakes.

329

330 **Abbreviations**

331 CMT: Centroid moment tensor; ETAS: Epidemic type aftershock sequence; CFF: Coulomb failure
332 function.

333

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337

338 **Authors' contributions**

339 TMB performed data analyses with TN. Both authors discussed the results and contributed to the paper
340 writing. Both authors read and approved the final manuscript.

341

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344

345 **Availability of data and materials**

346 The data catalog of centroid moment tensor (CMT) solutions analyzed in the current study are available
347 via (www.globalcmt.org). We use Coulomb3.3 program to calculate the change in Coulomb failure
348 function (Δ CFF) that is available via (<https://www.usgs.gov/software/coulomb-3>).

349

350 **Competing interests**

351 The authors declare that they have no competing interests.

352

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492

493 **Figure Legends**

494 Figure 1. Schematic illustration of the selection method of master event and the removal of the
495 aftershocks. We sort the earthquake catalog in time, and we select the first earthquake as a master event
496 in a given magnitude range. We then find slave events and select a next master event from the catalog
497 and repeat these process. q_1 is the first master event (E_0^1), and q_2 is its slave event. q_3 is out of the
498 magnitude range so that this is not selected as a master event. q_4 is not selected as a mater event,
499 because it occurs within 2000 km distance and $t_b \leq 14$ days from a larger earthquake, q_3 . q_5 is
500 selected as master event (E_0^2) because it occurs at distance larger than 2000 km from a larger earthquake
501 q_3 even though within $t_b \leq 14$ days (but without no slave event). q_6 is an earthquake out of target
502 magnitude. q_7 is not selected as a master event because it is close to q_6 . q_8 is selected as master
503 event (E_0^3) because it is larger than q_7 even though occurs within 2000 km distance and $t_b \leq 14$
504 days from q_7 . q_9 is also selected as master event (E_0^4) because it occurs at a distance larger than
505 2000km and $t_b > 14$ days from a larger earthquake, q_6 , and q_{10} is its slave event.

506

507 Figure 2. Schematic illustrations to show how different clusters of successive earthquakes are defined
508 for different choices of D and T_a . Blue circles represent master events, gray circles slave events and
509 each gray ellipse indicates a group of successive earthquakes (clusters). (a) A group of clusters obtained
510 for initial D and T_a . To remove aftershock activity, we do not use the earthquakes (S_i) occurring within
511 a distance of D_{min} that is determined from the magnitude of master event. (b) Green circle and green
512 ellipse represent new slave events and a new cluster, respectively, obtained by increasing D . (c) Orange
513 circle and orange ellipse represent a new slave event and a new cluster, respectively, obtained by
514 increasing T_a . (d) New slave events and new clusters obtained by increasing both D and T_a .

515

516 Figure 3. Cumulative numbers of the observed (solid lines) and simulated (dotted lines) clusters versus
517 horizontal distance for three lapse times ($c=3$ and $t_b = 14$ day. Note that the ranges of vertical axis
518 are different for (a) – (e). Arrows indicate the triggering distances where the cumulative numbers of
519 the observed and simulated clusters merge (see text).

520 Figure 4. Relationships between the triggering distances and seismic moment. Triggering distances are
521 measured for different parameters t_b (a) and c (b).

522

523 Figure 5. Spatial distributions of the successive earthquakes determined for (a) $M_w \geq 7.0$ (b) $6.5 \leq$
524 $M_w < 7.0$, and (c) $6.0 \leq M_w < 6.5$. Blue, orange, maroon colors represent the successive earthquakes
525 occurring within distances of 100, 500 and 1000 km, respectively, within a lapse time of 180 days.

526

527 Figure 6. Frequency distributions of the triggering distances calculated for 100 simulated data. The
528 observed triggering distances measured from the average of the simulation are indicated by red dotted
529 lines. Two lapse times (T_d) are examined: (a,b,c) for 365 days and (d,e,f) for 180 days.

530

531 Figure 7. Frequency distribution of Coulomb stress change calculated for the first fault plane (a,b,c) and
532 the second one (d,e,f). Solid and dotted red lines indicate ΔCFF of 0 Pa and 10^3 Pa, respectively.

533

534 **Table Legends**

535 Table 1. Successive earthquakes within triggering distance.

536

537

Figures

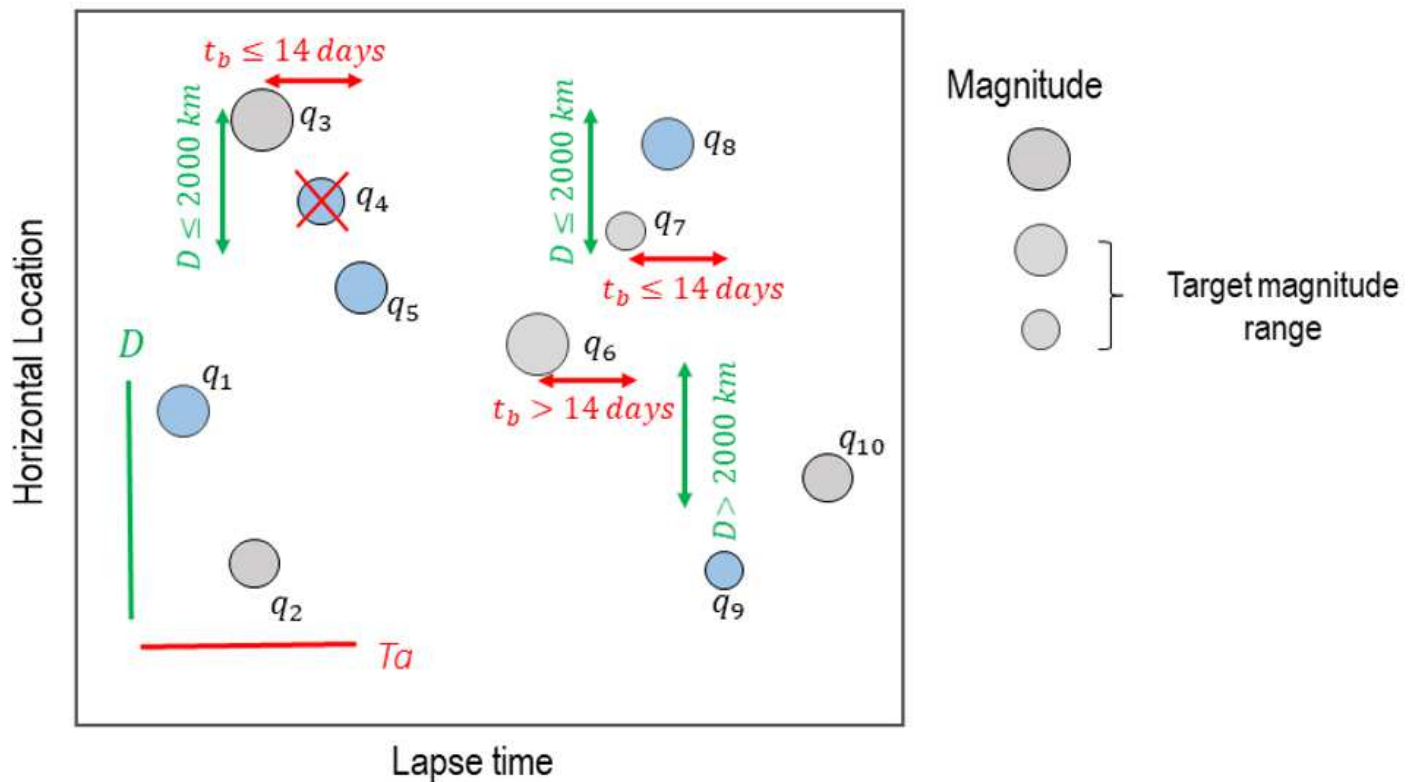


Figure 1

Schematic illustration of the selection method of master event and the removal of the aftershocks. We sort the earthquake catalog in time, and we select the first earthquake as a master event in a given magnitude range. We then find slave events and select a next master event from the catalog and repeat these process. q_1 is the first master event (E_0^1), and q_2 is its slave event. q_3 is out of the magnitude range so that this is not selected as a master event. q_4 is not selected as a mater event, because it occurs within 2000 km distance and $t_b \leq 14$ days from a larger earthquake, q_3 . q_5 is selected as master event (E_0^2) because it occurs at distance larger than 2000 km from a larger earthquake q_3 even though within $t_b \leq 14$ days (but without no slave event). q_6 is an earthquake out of target magnitude. q_7 is not selected as a master event because it is close to q_6 . q_8 is selected as master event (E_0^3) because it is larger than q_7 even though occurs within 2000 km distance and $t_b \leq 14$ days from q_7 . q_9 is also selected as master event (E_0^4) because it occurs at a distance larger than 2000km and $t_b > 14$ days from a larger earthquake, q_6 , and q_{10} is its slave event.

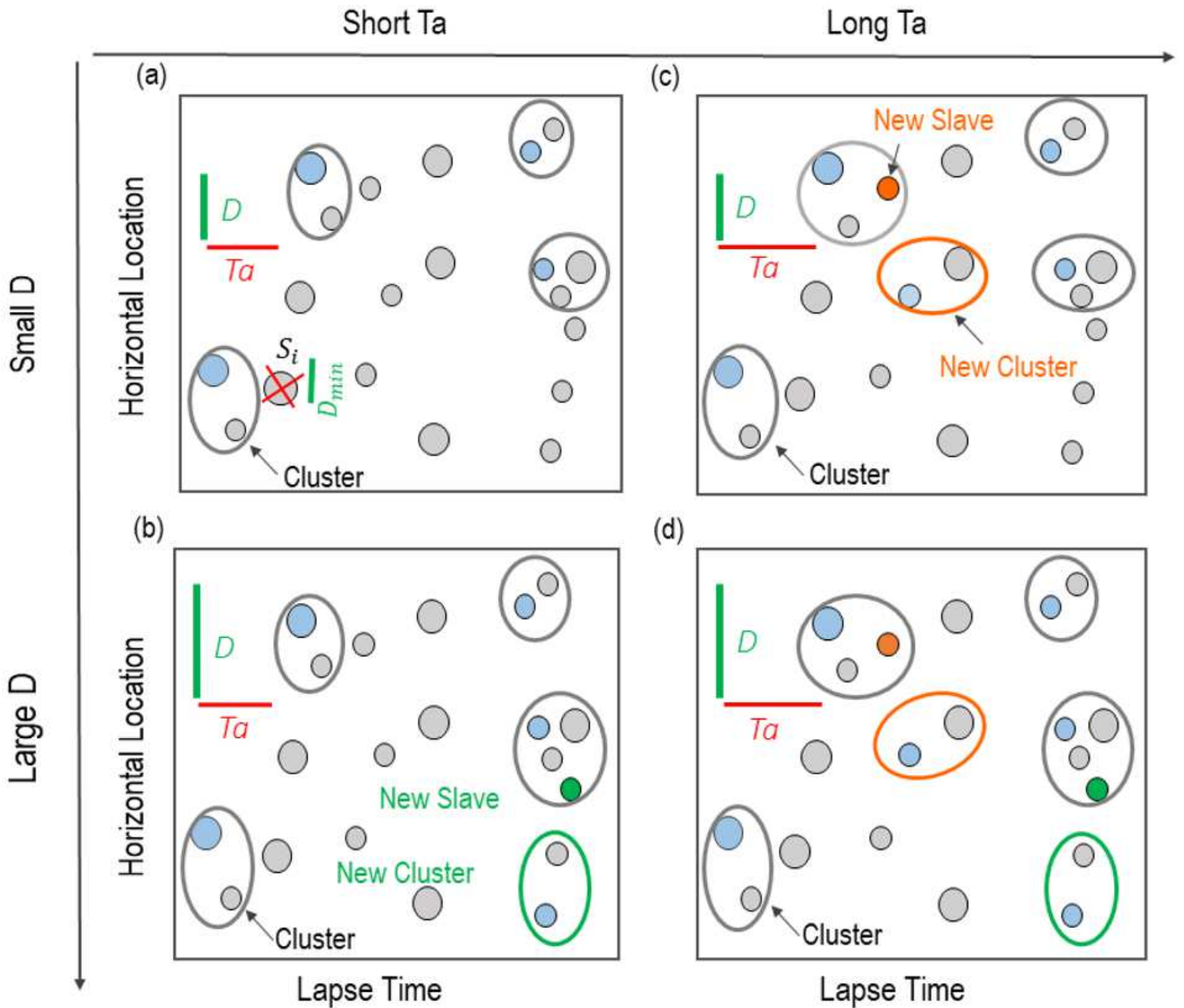


Figure 2

Schematic illustrations to show how different clusters of successive earthquakes are defined for different choices of D and T_a . Blue circles represent master events, gray circles slave events and each gray ellipse indicates a group of successive earthquakes (clusters). (a) A group of clusters obtained for initial D and T_a . To remove aftershock activity, we do not use the earthquakes (S_i) occurring within a distance of D_{min} that is determined from the magnitude of master event. (b) Green circle and green ellipse represent new slave events and a new cluster, respectively, obtained by increasing D . (c) Orange circle and orange ellipse represent a new slave event and a new cluster, respectively, obtained by increasing T_a . (d) New slave events and new clusters obtained by increasing both D and T_a .

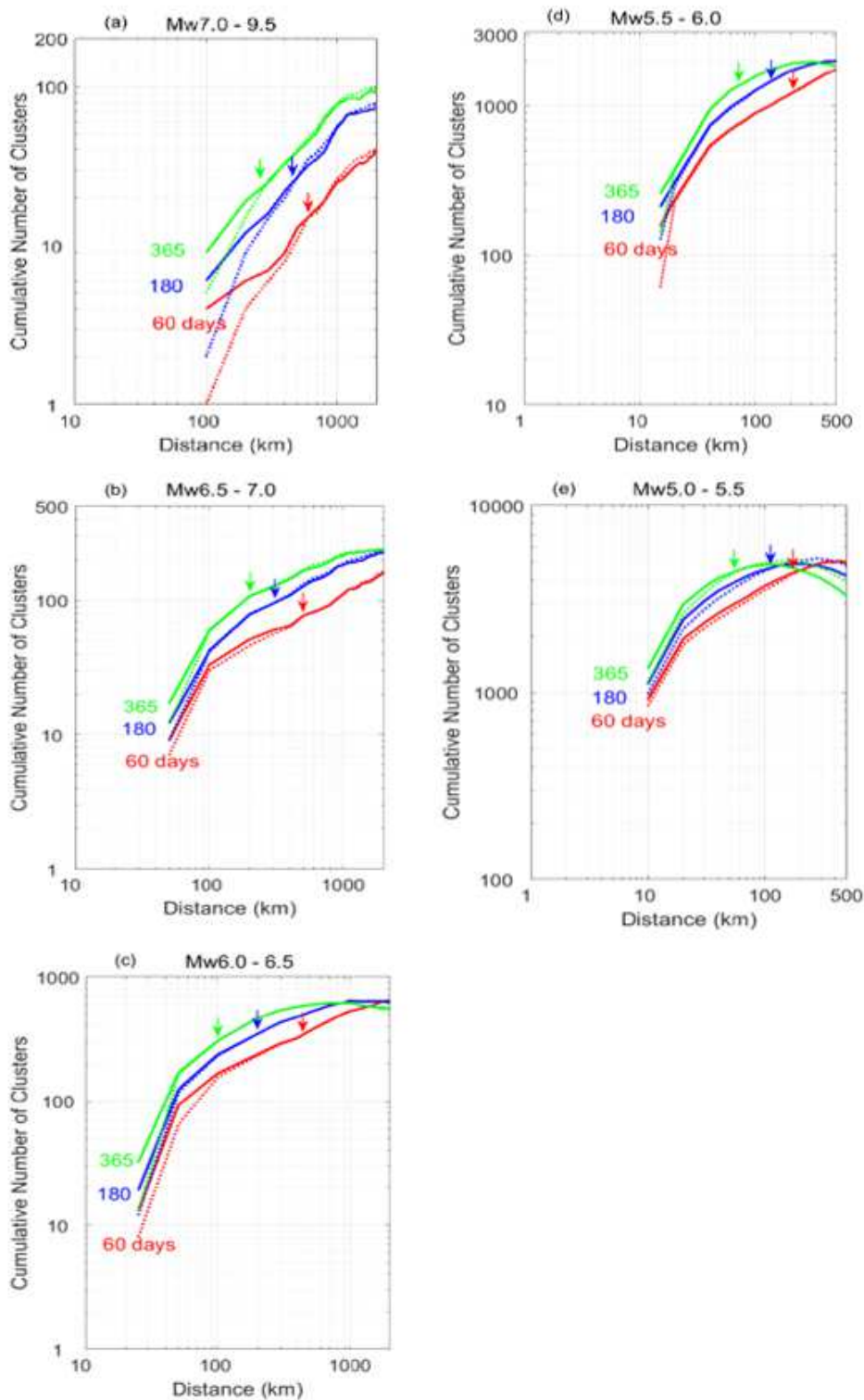


Figure 3

Cumulative numbers of the observed (solid lines) and simulated (dotted lines) clusters versus horizontal distance for three lapse times ($c=3$ and $t_b=14$ day). Note that the ranges of vertical axis are different for (a) – (e). Arrows indicate the triggering distances where the cumulative numbers of the observed and simulated clusters merge (see text).

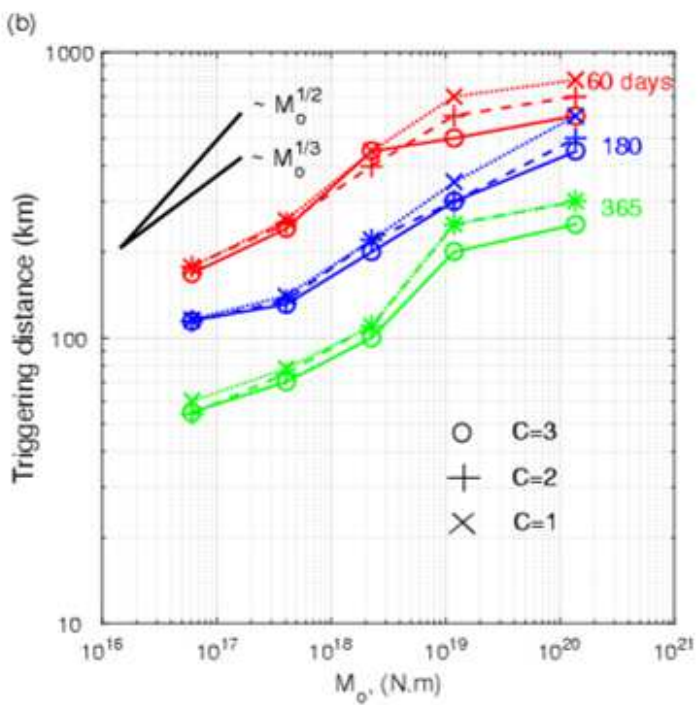
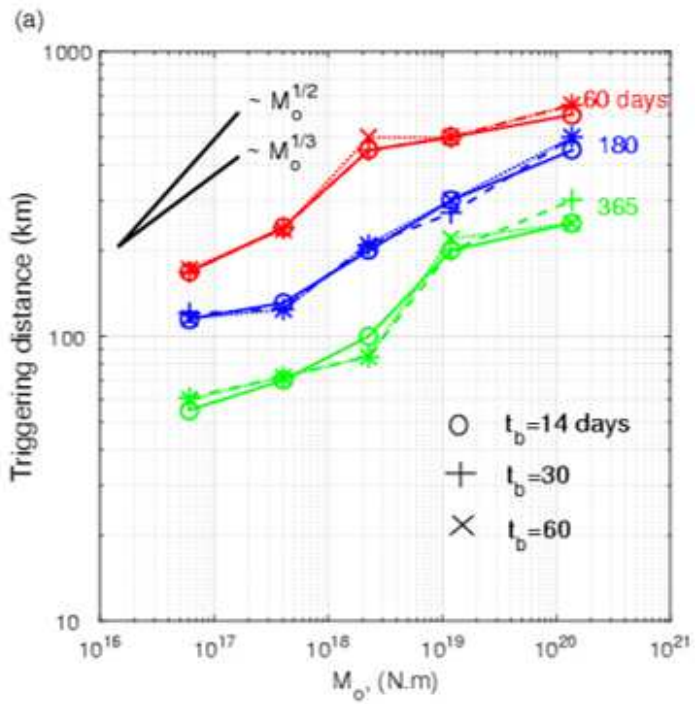


Figure 4

Relation between triggering distances and seismic moment. Triggering distances are measured for different parameters t_b (a) and c (b).

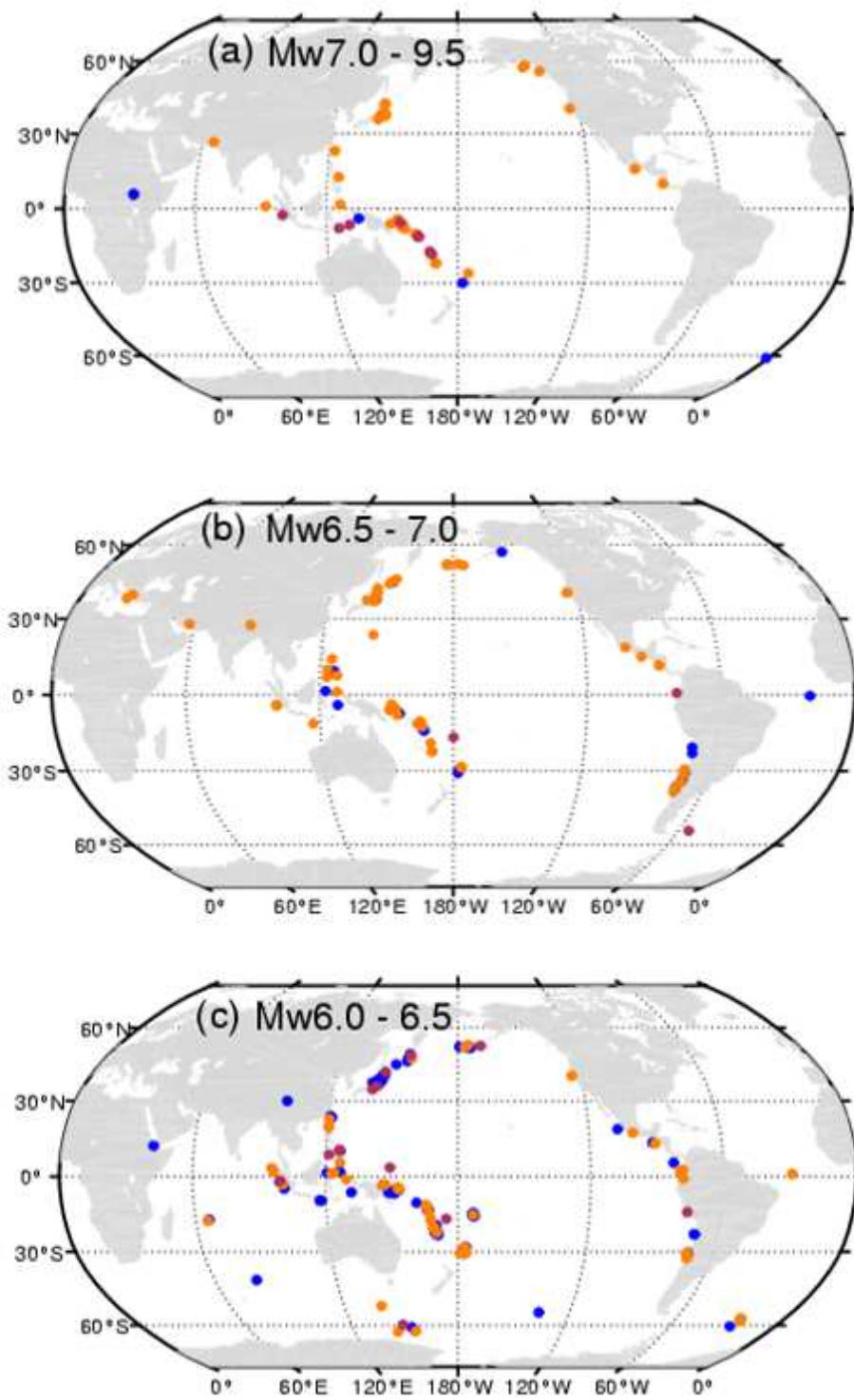


Figure 5

Spatial distributions of the successive earthquakes determined for (a) $M_w \geq 7.0$ (b) $6.5 \leq M_w < 7.0$, and (c) $6.0 \leq M_w < 6.5$. Blue, orange, maroon colors represent the successive earthquakes occurring within distances of 100, 500 and 1000 km, respectively, within a lapse time of 180 days.

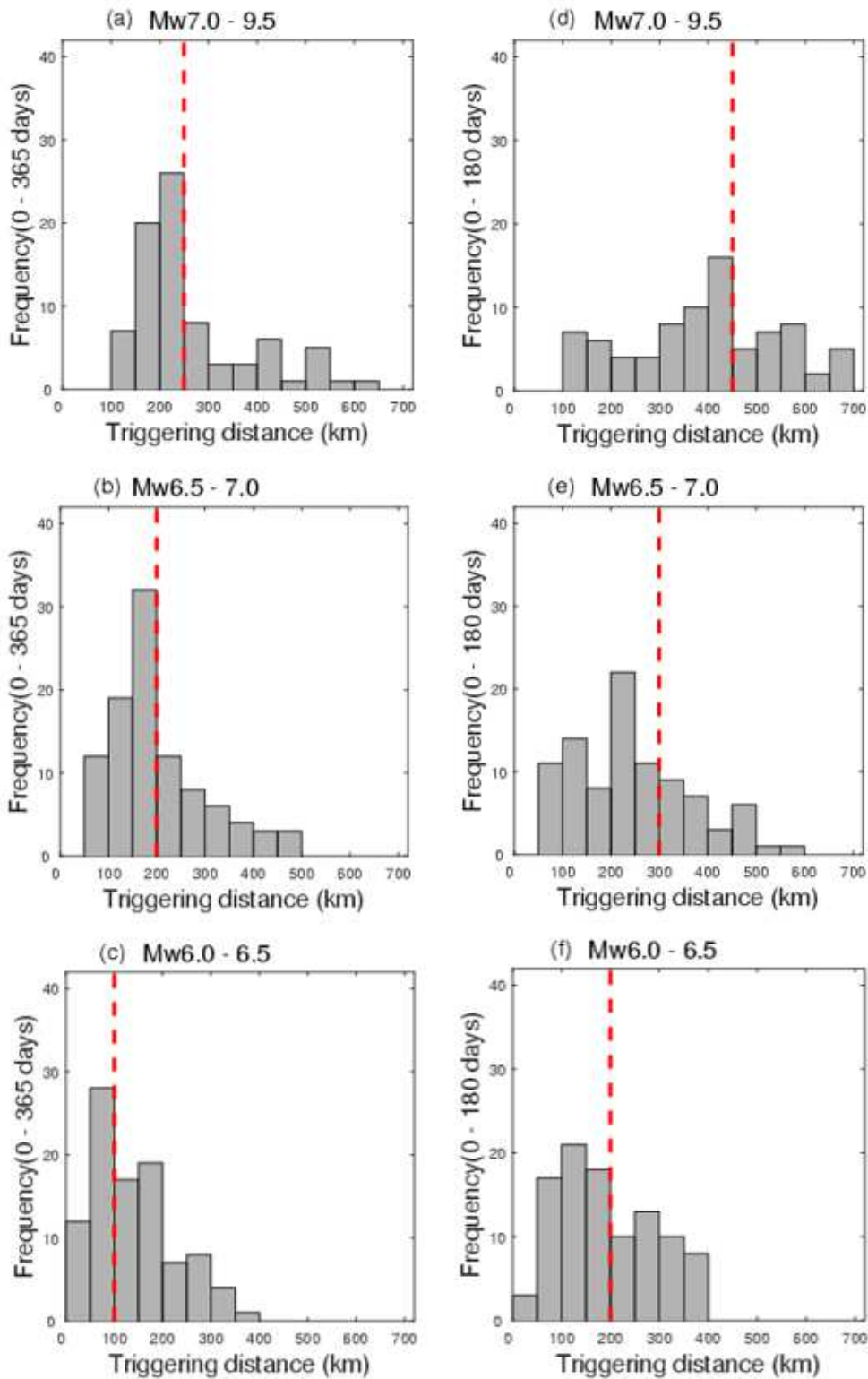


Figure 6

Frequency distributions of the triggering distances calculated for 100 simulated data. The observed triggering distances measured from the average of the simulation are indicated by red dotted lines. Two lapse times (T_a) are examined: (a,b,c) for 365 days and (d,e,f) for 180 days.

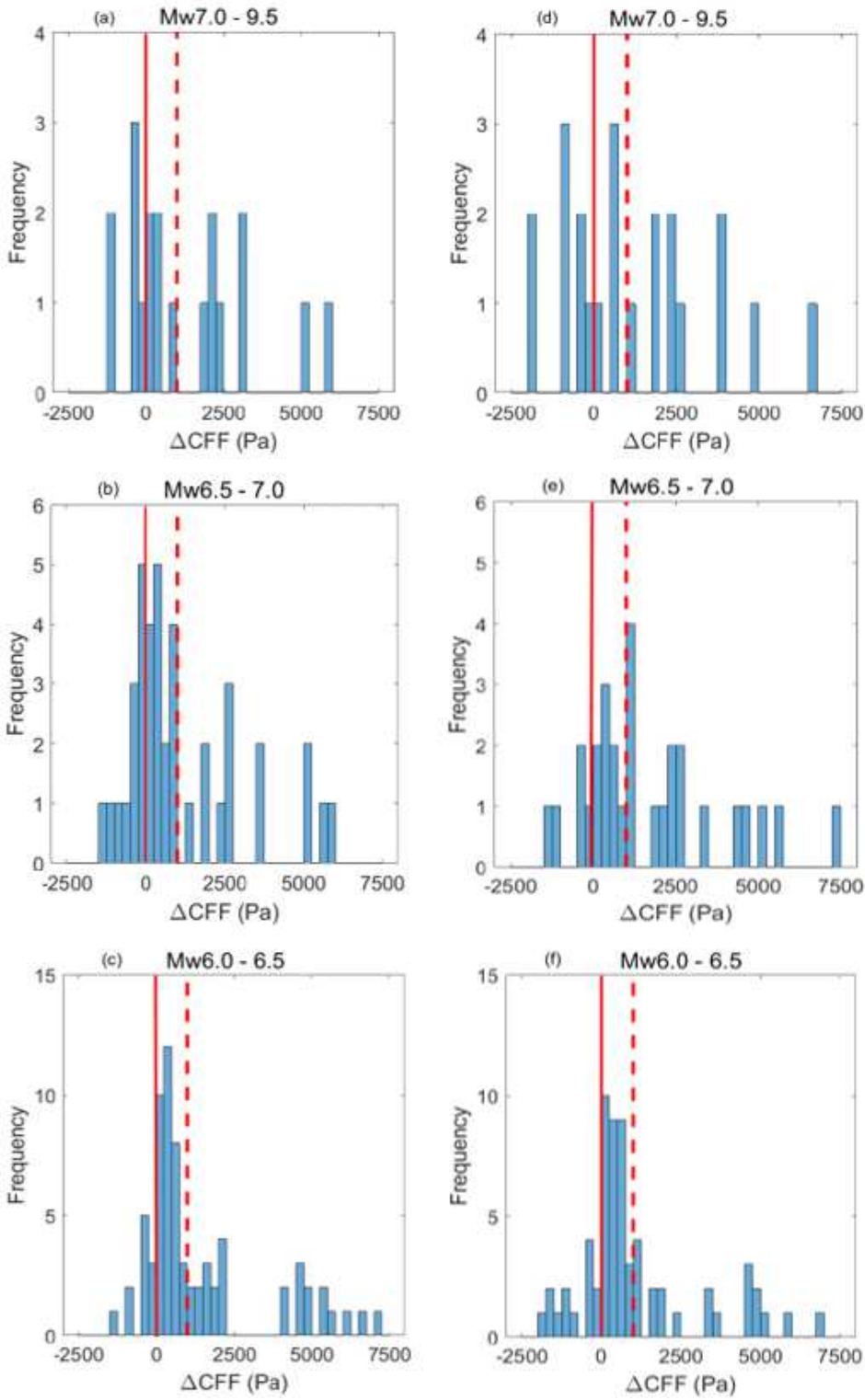


Figure 7

Frequency distribution of Coulomb stress change calculated for the first fault plane (a,b,c) and the second one (d,e,f). Solid and dotted red lines indicate ΔCFF of 0 Pa and 10^3 Pa, respectively.

Supplementary Files

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