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Single-step genomic evaluation with a metafounder for feed conversion ratio and average daily gain in Danish Landrace and Yorkshire pigs

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Abstract

Background

Single-step genomic best linear unbiased prediction (SSGBLUP) method is an effective approach for genetic evaluation. To overcome the issue that pedigree and genomic relationship matrices refer to different base populations, a single-step genomic method with a metafounder (MF-SSGBLUP) was put forward. The aim of this study was to compare the predictive abilities and bias of genomic evaluation based on MF-SSGBLUP compared with standard SSGBLUP. We did this for feed conversion ratio (FCR) and average daily gain (ADG) in DanBred Landrace (LL) and DanBred Yorkshire (YY) pigs using both univariate and bivariate models. Additionally, optimal weighting factors (ω) on pedigree-based relationship matrices for ADG and FCR in both SSGBLUP and MF-SSGBLUP were also investigated.

Results

In general, SSGBLUP and MF-SSGBLUP methods showed similar predictive abilities and biasedness of GEBVs. In LL, for ADG, the predictive ability for SSGBLUP was up to 0.355, while MF-SSGBLUP reached a highest predictive ability of 0.356; for FCR, the predictive ability for MF-SSGBLUP together with a bivariate model was highest (0.196) among all the different scenarios. In YY, performances of genomic prediction for ADG were almost similar among different scenarios and predictive ability for ADG was up to 0.347; for FCR, the highest predictive ability (0.355) was obtained in MF-SSGBLUP. In biasedness, SSGBLUP and MF-SSGBLUP performed

nearly the same, and bivariate models generally had less biasedness than univariate models. Additionally, in terms of the optimal weighting factors (ω), in LL, regardless of a univariate or a bivariate model was used, the optimal ω for ADG were around 0.2 in both SSGBLUP and MF-SSGBLUP; for FCR, 0.70 and 0.55 were the optimal ω in SSGBLUP and MF-SSGBLUP method, respectively. In YY, the optimal ω ranged from 0.25 to 0.35 for ADG and from 0.10 to 0.30 for FCR in different scenarios.

Conclusions

This study indicated that MF-SSGBLUP method performed at least as good as SSGBLUP for genomic evaluation. The optimal weighting factors (ω) in SSGBLUP and MF-SSGBLUP are not dramatically different. Overall, MF-SSGBLUP in combination with a bivariate model was recommended for single-step genomic evaluation for ADG and FCR in DanBred Landrace and Yorkshire pigs.

Keywords: Single-step GBLUP, Metafounder, Weighting factor, Model, Pigs

Background

Single-step genomic best linear unbiased prediction (SSGBLUP) has been successfully used as a standard genomic evaluation method in the pig industry [1]. Through using SSGBLUP, genomic selection (GS) can be implemented even if some animals are not genotyped, as it has an ability to integrate information from

64 phenotypic records, pedigree and genomic information on all the relevant animals [2,
65 3]. However, in regular SSGBLUP, some issues need to be solved. First, allele
66 frequencies that are used to construct the genomic relationship matrix theoretically
67 should be obtained from the base population [4]. Nevertheless, the base allele
68 frequencies are usually unknown, since the animals in the base population have
69 usually been dead for many years, and therefore are not genotyped [5]; second,
70 genomic relationship matrix and pedigree relationship matrix should refer to the same
71 (base) population to make them compatible. However, the (base) population is usually
72 unknown and the beginning of pedigree is often regarded as the base population,
73 which is an arbitrary choice. Thus, pedigree-based and marker-based relationship
74 matrices are not directly compatible [6]; third, the optimal weighting factors (ω) on
75 pedigree-based relationship matrix in a single-step genomic evaluation method might
76 be breed-specific and trait-specific, which need to be further investigated. Currently,
77 there are a few imperfect solutions to the above-mentioned issues. For example,
78 instead of using base allele frequencies, allele frequencies of the current population
79 are used to construct the genomic relationship matrix. Some studies adjusted the
80 marker-based relationship matrix to make it compatible with the pedigree-based
81 relationship matrix [7-9]. Breeding companies usually use a same weighting factor (ω)
82 for different traits, rather than using an optimal ω for each trait, leading to a decreased
83 accuracies of estimated breeding values [10]. Although these solutions have been
84 widely used in regular SSGBLUP and seemed to be effective in practice, the

above-mentioned issues in regular SSGBLUP were not totally solved and SSGBLUP had to be further developed and improved.

To overcome these issues, based on Christensen [6], Legarra et al. [5] developed a concept of metafounder. A metafounder is assumed to be a finite-sized pool of gametes, and animals in the base population randomly extract alleles from this pool to form diploids [5]. With the concept of metafounder, genomic relationships should be constructed using allele frequencies of 0.5, and a pedigree-based relationship matrix needs to refer to the base allele frequencies as well, which resulted in automatic compatibility between pedigree-based and marker-based relationship matrices. In other words, the issues of unknown allele frequencies in base populations and compatibility between two relationship matrices in SSGBLUP were in principle solved.

Since then, a few studies have focused on the applications of single-step genomic evaluation with metafounders (MF-SSGBLUP). For instance, Garcia-Baccino et al. [11] used simulated data to investigate the optimal ways of estimating the relatedness of animals in the base population (γ); Xiang et al. [12] employed MF-SSGBLUP on purebred pigs for their crossbred performances and Bradford et al. [13] compared the performances of SSGBLUP with three unknown parent groups with MF-SSGBLUP in dairy cattle and recommended the use of MF-SSGBLUP for genomic prediction; Macedo et al. [14] concluded that MF-SSGBLUP yielded unbiased estimates when pedigree information was not complete. Nevertheless, to our knowledge, there is lack

of studies on the comparison of how MF-SSGBLUP performs in genomic evaluation for productive traits (e.g.: feed conversion ratio, FCR and average daily gain, ADG) in pigs with the standard SSGBLUP method, especially that such records are available at the time of selection, and also using a multi-trait model, which is comprehensively used in pig breeding program. Besides, there were no studies investigating the effect of different weighing factors on pedigree-based relationship matrix in MF-SSGBLUP method. Therefore, the aims of this study are: (1) to compare the predictive abilities of genomic evaluation in SSGBLUP and MF-SSGBLUP; (2) to investigate the accuracies and biasedness of GEBVs in univariate and bivariate animal models in both SSGBLUP and MF-SSGBLUP methods; (3) to find optimal weighting factors (ω) on pedigree-based relationship matrices for ADG and FCR, in both SSGBLUP and MF-SSGBLUP. Results from this study can be applied directly in pig breeding industry.

Materials and Methods

Phenotypic recordings

In this study, all the datasets were provided by SEGES Danish Pig Research Centre. The traits of ADG (ADG = weight gain/days) and FCR (FCR = feed intake/weight gain) in the interval 30 to 100 kg were measured in both DanBred Landrace (LL) and DanBred Yorkshire (YY) pigs. In LL, ADG were recorded on 686,420 pigs, among which 18,889 pigs also had FCR recordings. In YY, ADG and FCR were recorded on

570,493 pigs and 19,387 pigs, respectively. All the phenotypic recordings were measured between the year 2000 and 2017. Pedigrees of the two breeds were traced back to the date 1 January 1994, and thus, there are 700,960 LL pigs and 582,114 YY pigs in the two pedigrees.

Genotypes

A total of 37,699 LL pigs and 37,845 YY pigs were genotyped with either the Illumina PorcineSNP60 Genotyping BeadChip v1 or v2. i.e. about 50% animals with each version. The two different chip versions were taken into account when applying a quality filter on SNPs. SNPs were mapped to pig chromosomes using the pig genome build 10.2 [15]. Quality controls were applied in LL and YY separately as follows: animals with call-rate smaller than 90% were first removed; SNPs with call-rate smaller than 90% were removed as well; SNPs with minor allele frequency smaller than 0.05 were filtered out; SNPs that deviated strongly from Hardy Weinberg equilibrium within breed ($p < 10e-7$) were also excluded. Fimpute v2.2 [16] was used to impute the missing SNPs. After quality control, 37,621 SNPs on 37,699 LL and 36,687 SNPs on 37,845 YY were retained for further analysis.

Methods of constructing relationship matrix

In SSGBLUP, the inverse of combined marker-based and pedigree-based relationship matrix was constructed according to Christensen and Lund [3] and Christensen et al. [9], which was:

$$H^{-1} = \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{G}_w^{-1} - \mathbf{A}_{22}^{-1} \end{bmatrix} + \mathbf{A}^{-1},$$

148 where $\mathbf{G}_\omega = (1 - \omega)\mathbf{G} + \omega\mathbf{A}_{22}$ and \mathbf{A}_{22} contained pedigree-based relationships
 149 among genotyped pigs; \mathbf{G} matrix was constructed following Vanraden [4] method 1:
 150 $\mathbf{G} = \frac{(\mathbf{m} - 2\mathbf{p}_i)(\mathbf{m} - 2\mathbf{p}_i)^T}{\sum 2p_i(1 - p_i)}$, where \mathbf{m} is a matrix with entries $m_{ij} = 0, 1, 2$ for genotypes AA ,
 151 AB and BB , respectively. In theory, \mathbf{p}_i should be allele frequencies in the base
 152 population, but as we mentioned above, in practice, \mathbf{p}_i were often computed from
 153 observed genotypes. To be compatible with the pedigree-based relationship matrix, \mathbf{G}
 154 matrix was scaled to create a \mathbf{G}_a matrix, following Christensen et al. [9]: $\mathbf{G}_a =$
 155 $\beta\mathbf{G} + \alpha$, where β and α were obtained by solving the following equations:
 156 $Avg(diag(\mathbf{G}))\beta + \alpha = Avg(diag(\mathbf{A}_{22}))$ and $Avg(\mathbf{G})\beta + \alpha = Avg(\mathbf{A}_{22})$. This
 157 \mathbf{G}_a matrix was used instead of matrix \mathbf{G} in the formula for combined marker-based
 158 and pedigree-based relationship matrix above. To test the effects of different
 159 weighting factors (ω) between the pedigree-based and marker-based relationship
 160 matrices on genomic predictions, ω values between 0.05 and 0.95 with a gap of 0.05
 161 were investigated for the SSGBLUP method. Inverse pedigree-based relationship \mathbf{A}
 162 matrix was constructed according to the Henderson rule [17].
 163 In MF-SSGBLUP, to construct the inverse combined relationship matrix, the first step
 164 was to estimate a parameter γ in both LL and YY, respectively, which represents the
 165 relatedness for base animals. In this study, we followed Garcia-Baccino et al. [11] and
 166 Xiang et al. [12] using the method of generalized least squares (GLS) for estimating γ .
 167 Christensen [6] and Garcia-Baccino et al. [11] showed that $\gamma = 8\sigma_p^2$ and σ_p^2 is
 168 variance of true allele frequencies in the base population. In other words, to estimate

169 γ , the σ_p^2 needs to be estimated first, which was done by GLS method in this study.

170 The detailed steps of obtaining σ_p^2 and γ can be found in our previous study [12].

171 After getting γ for both LL and YY, the inverse combined relationship matrix

172 $\mathbf{H}(\gamma)^{-1}$ was constructed as follows:

$$173 \quad \mathbf{H}(\gamma)^{-1} = \begin{bmatrix} \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{G}_{\omega}^{-1} - \mathbf{A}(\gamma)_{22}^{-1} \end{bmatrix} + \mathbf{A}(\gamma)^{-1},$$

174 where the marker-based relationship matrix $\mathbf{G} = (\mathbf{m} - \mathbf{1}\mathbf{1}')(\mathbf{m} - \mathbf{1}\mathbf{1}')' / s$ and

175 \mathbf{m} is the allele contents matrix with entries 0, 1, 2 for genotypes AA , AB and BB ,

176 respectively, and s is a scaling parameter, which is half of the number of used

177 markers [18]. This method was the same as ssGBLUP_M in Garcia-Baccino et al.

178 [11]. In this study, 37,621 SNPs and 36,687 SNPs were used for LL and YY,

179 respectively and thus s was 18,810.5 and 18,343.5 for LL and YY, respectively. To

180 capture the residual polygenetic effects, matrix \mathbf{G} was replaced by $\mathbf{G}_{\omega} = (1 -$

181 $\omega)\mathbf{G} + \omega\mathbf{A}(\gamma)_{22}$. Similar to SSGBLUP, values of ω between 0.05 and 0.95 with a gap

182 of 0.05 were investigated. The inverse of pedigree-based relationship matrix $\mathbf{A}(\gamma)^{-1}$

183 was constructed according to the usual rule [5], and matrix $\mathbf{A}(\gamma)_{22}$ was constructed

184 following Colleau [19]. Matrix $\mathbf{A}(\gamma)_{22}^{-1}$ is the inverse of matrix $\mathbf{A}(\gamma)_{22}$.

185 **Statistical models**

186 Both univariate and bivariate animal models were applied for ADG and FCR in LL

187 and YY, respectively. The statistical models for ADG and FCR were as follows:

$$188 \quad \mathbf{y}_{ADG} = \mathbf{X}_{ADG}\boldsymbol{\beta}_{ADG} + \mathbf{Z}_{ADG}\mathbf{a}_{ADG} + \mathbf{M}_{ADG}\mathbf{litter}_{ADG} + \mathbf{W}_{ADG}\mathbf{pen}_{ADG} + \mathbf{e}_{ADG},$$

$$189 \quad \mathbf{y}_{FCR} = \mathbf{X}_{FCR}\boldsymbol{\beta}_{FCR} + \mathbf{Z}_{FCR}\mathbf{a}_{FCR} + \mathbf{e}_{FCR},$$

190 where \mathbf{y}_{ADG} and \mathbf{y}_{FCR} contain phenotypic recordings for ADG and FCR,
 191 respectively; $\mathbf{X}_{ADG}\boldsymbol{\beta}_{ADG}$ and $\mathbf{X}_{FCR}\boldsymbol{\beta}_{FCR}$ represent fixed effects, which include
 192 section (physical unit for animals present at the same point of time) effect, sex effect
 193 and covariates of the starting weights for ADG and FCR, respectively; \mathbf{a}_{ADG} and
 194 \mathbf{a}_{FCR} are additive effects for ADG and FCR, respectively; \mathbf{litter}_{ADG} and \mathbf{pen}_{ADG}
 195 are random birth litter effects and random pen effects for ADG; \mathbf{Z} , \mathbf{M} , \mathbf{W} are the
 196 respective incidence matrices; \mathbf{e}_{ADG} and \mathbf{e}_{FCR} are the random residual effects. It
 197 was assumed that random litter effects and pen effects follow normal distributions, as:
 198 $\mathbf{litter}_{ADG} \sim N(\mathbf{0}, \mathbf{I}\sigma_{litter}^2)$ and $\mathbf{pen}_{ADG} \sim N(\mathbf{0}, \mathbf{I}\sigma_{pen}^2)$, where \mathbf{I} is an identity matrix.
 199 In the univariate models, vectors \mathbf{a}_{ADG} and \mathbf{a}_{FCR} were assumed normally
 200 distributed with mean $\mathbf{0}$ and (co)variance structures equal to $var(\mathbf{a}_{ADG}) = \mathbf{H}\sigma_{a_ADG}^2$
 201 and $var(\mathbf{a}_{FCR}) = \mathbf{H}\sigma_{a_FCR}^2$ in SSGBLUP, and $var(\mathbf{a}_{ADG}) = \mathbf{H}(\gamma)\sigma_{a_ADG}^2$ and
 202 $var(\mathbf{a}_{FCR}) = \mathbf{H}(\gamma)\sigma_{a_FCR}^2$ in MF-SSGBLUP. In the bivariate model, \mathbf{a}_{ADG} and
 203 \mathbf{a}_{FCR} were assumed to follow a multivariate normal distribution:
 204
$$\begin{pmatrix} \mathbf{a}_{ADG} \\ \mathbf{a}_{FCR} \end{pmatrix} \sim N\left(\mathbf{0}, \begin{pmatrix} \sigma_{a_ADG}^2 & \sigma_{a_ADG, a_FCR} \\ \sigma_{a_FCR, a_ADG} & \sigma_{a_FCR}^2 \end{pmatrix} \otimes \mathbf{H}\right)$$
 in SSGBLUP and
 205
$$\begin{pmatrix} \mathbf{a}_{ADG} \\ \mathbf{a}_{FCR} \end{pmatrix} \sim N\left(\mathbf{0}, \begin{pmatrix} \sigma_{a_ADG}^2 & \sigma_{a_ADG, a_FCR} \\ \sigma_{a_FCR, a_ADG} & \sigma_{a_FCR}^2 \end{pmatrix} \otimes \mathbf{H}(\gamma)\right)$$
 in MF-SSGBLUP, where
 206 $\sigma_{a_ADG}^2$, $\sigma_{a_FCR}^2$ and σ_{a_ADG, a_FCR} are additive genetic variances for ADG, additive
 207 genetic variances for FCR and additive genetic covariance between ADG and FCR,
 208 respectively. Note that in MF-SSGBLUP, (co)variance components cannot be directly
 209 compared with the normal scale that assumes animals in the base population are

unrelated. For this purpose, all the genetic (co)variance components in the MF-SSGBLUP were multiplied by $(1 - \gamma/2)$, where γ is from the respective LL or YY population [5, 18].

Scenarios and genetic parameters

Estimates of (co)variance components and heritabilities (h^2) was investigated in four different scenarios for both ADG and FCR: (1) SSGBLUP method in a univariate model (*UNI_SSGBLUP*); (2) MF-SSGBLUP method in a univariate model (*UNI_MF-SSGBLUP*); (3) SSGBLUP method in a bivariate model (*BI_SSGBLUP*) and (4) MF-SSGBLUP method in a bivariate model (*BI_MF-SSGBLUP*). Estimates of genetic correlation between ADG and FCR (r_g) was only studied in the two bivariate scenarios: *BI_SSGBLUP* and *BI_MF-SSGBLUP*. All of the four scenarios were studied in both LL and YY populations. For heritabilities, with the SSGBLUP method,

they were calculated as $h_{ADG}^2 = \frac{\sigma_{a_ADG}^2}{\sigma_{a_ADG}^2 + \sigma_{litter}^2 + \sigma_{pen}^2 + \sigma_{e_ADG}^2}$ and $h_{FCR}^2 = \frac{\sigma_{a_FCR}^2}{\sigma_{a_FCR}^2 + \sigma_{e_FCR}^2}$

for ADG and FCR, respectively. In scenarios *UNI_MF-SSGBLUP* and *BI_MF-SSGBLUP*, as mentioned above, all the variance components had to be scaled first. Thus, the heritabilities for ADG and FCR in scenarios *UNI_MF-SSGBLUP* and

BI_MF-SSGBLUP were calculated as: $h_{ADG}^2 = \frac{\sigma_{a_ADG}^2 * (1 - \gamma/2)}{\sigma_{a_ADG}^2 * (1 - \gamma/2) + \sigma_{litter}^2 + \sigma_{pen}^2 + \sigma_{e_ADG}^2}$ and

$h_{FCR}^2 = \frac{\sigma_{a_FCR}^2 * (1 - \gamma/2)}{\sigma_{a_FCR}^2 * (1 - \gamma/2) + \sigma_{e_FCR}^2}$. In terms of genetic correlation between ADG and FCR

(r_g), in both *BI_SSGBLUP* and *BI_MF-SSGBLUP*, r_g was calculated as: $r_g =$

$\frac{\sigma_{a_ADG, a_FCR}}{\sqrt{\sigma_{a_ADG}^2 * \sigma_{a_FCR}^2}}$. Software DMU was used to estimate the variance components [20].

Predictive abilities

231 To compare the performances of genomic evaluation between SSGBLUP and
 232 MF-SSGBLUP and investigate the effects of different weighting factors (ω) on
 233 genomic predictions, the predictive abilities were measured as correlation between
 234 corrected phenotypes (Y_c) and genomic estimated breeding values (\hat{a}) in different
 235 scenarios ($cor(Y_c, \hat{a})$), following Christensen et al. [9]. A Hotelling-Williams t-test at
 236 a 5% confidence level was applied to evaluate the statistical significance of the
 237 differences between predictive abilities in different scenarios. Phenotypes were
 238 corrected for all the fixed effects and random effects other than additive genetic effect
 239 ($Y_c = \hat{a} + residuals$). To avoid the possible preference of a specific single-step
 240 method in the process of calculating Y_c , traditional BLUP method in combination
 241 with a univariate model was used to obtain Y_c .
 242 Data recordings were split into training populations and validation populations by
 243 using a cut-off date of 1 May 2016. Validation populations consisted of young pigs
 244 born between 1 May 2016 and 1 February 2017. Thus, 654,908 LL and 541,301 YY
 245 were included in the training populations, respectively, and among them, 29,825 LL
 246 and 30,144 YY were genotyped, respectively. The validation populations contained
 247 31,515 LL and 29,192 YY, respectively, while 7,700 LL and 7,645 YY were
 248 genotyped, respectively. Validation populations were divided into subgroups of
 249 genotyped and non-genotyped animals. For each of the YY and LL populations,
 250 predictive abilities were investigated in the two subgroups as well as in the whole
 251 validation population. Meanwhile, regression coefficients of Y_c on \hat{a} in different

scenarios were calculated as an indicator of biasedness of the genomic predictions.

Table 1 provides an overview of the numbers of animals in the different datasets.

Results

Estimation of γ in MF-SSGBLUP

In MF-SSGBLUP, before constructing the inverse combined relationship matrix, parameter γ should be estimated first. The estimates were $\hat{\gamma}_L = 0.605$ for LL and $\hat{\gamma}_Y = 0.553$ for YY.

Scenarios and genetic parameters

Table 2 shows estimated genetic parameters for ADG and FCR in all the scenarios, and genetic correlations (r_g) between ADG and FCR in bivariate scenarios (*BI_SSGBLUP*, *BI_MF-SSGBLUP*) in LL and YY populations.

In LL, additive genetic variances of ADG ($\sigma_{a_{ADG}}^2$) and FCR ($\sigma_{c_{FCR}}^2$) were similar among the four scenarios. Heritabilities for ADG ($h_{a_{ADG}}^2$) and FCR ($h_{a_{FCR}}^2$) were almost constant across different scenarios ($h_{a_{ADG}}^2$ ranged from 0.23 to 0.24 and $h_{a_{FCR}}^2$ ranged from 0.10 to 0.11). For genetic correlations between ADG and FCR, r_g in scenario *BI_MF-SSGBLUP* (-0.27) showed higher negative correlations than that in scenario *BI_SSGBLUP* (-0.19).

In YY, as a whole, we obtained similar results as in LL. All the four scenarios generally showed similar estimated variance components, except for the estimates of additive genetic variances for ADG ($\sigma_{a_{ADG}}^2$) and FCR ($\sigma_{a_{FCR}}^2$). In the two

metafounder scenarios (*UNI_MF-SSGBLUP* and *BI_MF-SSGBLUP*), $\sigma_{a_{ADG}}^2$ and $\sigma_{a_{FCR}}^2$ were slightly higher than that in other two SSGBLUP scenarios. Heritabilities were stable across different scenarios, where $h_{a_{ADG}}^2$ varied between 0.26 and 0.28 and $h_{a_{FCR}}^2$ varied between 0.19 and 0.20. Genetic correlations between ADG and FCR were same (-0.46) in scenarios *BI_MF-SSGBLUP* and *BI_SSGBLUP*.

Predictive abilities

The diagrams of correlation coefficients between corrected phenotypes (Y_c) of ADG and FCR, and genomic estimated breeding values (\hat{a}) in different scenarios ($cor(Y_c, \hat{a})$) with a dynamic ω are shown in Figure 1.

In LL, for ADG, four scenarios performed nearly the same (highest $cor(Y_c, \hat{a}) = 0.355$), and the optimal weighting factors (ω) were 0.20, 0.15, 0.20 and 0.25 in scenarios *UNI_SSGBLUP*, *UNI_MF-SSGBLUP*, *BI_SSGBLUP* and *BI_MF-SSGBLUP*, respectively. For FCR, predictive abilities in bivariate scenarios (0.19) were a bit higher than those in the univariate scenarios (0.16). The optimal ω were 0.70 in both *UNI_SSGBLUP* and *BI_SSGBLUP*, and 0.55 in both *UNI_MF-SSGBLUP* and *BI_MF-SSGBLUP*.

In YY, for ADG, curves of predictive abilities in four scenarios were almost on top of each other. The highest predictive abilities (0.347) appeared when ω was set at around 0.30 in different scenarios. For FCR, univariate models performed slightly better than bivariate models when ω were lower than 0.85. In univariate models, highest predictive abilities of FCR were 0.355, where ω were set to 0.10 and 0.15 in

294 *UNI_SSGBLUP* and *UNI_MF-SSGBLUP*, respectively. In bivariate models, when ω
295 were set to 0.25 and 0.30 in *BI_SSGBLUP* and *BI_MF-SSGBLUP*, highest predictive
296 abilities of 0.344 turned up.

297 As a whole, with same ω , performances of genomic evaluation were not much
298 different among four scenarios. Meanwhile, we observed that scenario
299 *BI_MF-SSGBLUP* potentially had some superiority of predictive abilities compared to
300 other scenarios in genomic evaluation.

301 In addition, to compare the performances of genomic evaluation in genotyped and
302 non-genotyped animals, validation populations were first divided into genotyped
303 subgroups and non-genotyped subgroups in both LL and YY, and then predictive
304 abilities were calculated on both subgroups with the estimated optimal ω . Predictive
305 abilities of genomic prediction with an optimal ω in the validation populations for
306 ADG and FCR are displayed in Table 3. For same trait and same population, based on
307 the Figure 1, the optimal ω in SSGBLUP and MF-SSGBLUP were nearly the same.
308 Thus, we only investigated the performances of genomic evaluation on both
309 genotyped and non-genotyped animals with four optimal ω : 0.20, 0.70, 0.25 and 0.10
310 for ADG in LL, FCR in LL, ADG in YY and FCR in YY, respectively.

311 According to Table 3, no matter if a univariate model or a bivariate model was used,
312 SSGBLUP and MF-SSGBLUP showed similar predictive abilities for genotyped
313 subgroups and non-subgroups. Within each scenario, animals in genotyped subgroups
314 always presented higher predictive abilities than those in non-genotyped subgroups.

Biasedness of genomic predictions was investigated as regression coefficients of corrected phenotypes (\mathbf{Y}_c) on the genomic estimated breeding values ($\hat{\mathbf{a}}$). The changes of biasedness for both ADG and FCR in different scenarios in both LL and YY with ω ranging from 0.05 to 0.95 with a gap of 0.05 are shown in Figure 2. In general, regression coefficients increased with the weighting factors (ω). In LL, among different ω , when ω was 0.95, the regression coefficients were closest to 1. More specifically, for ADG, the changes of regression coefficients were nearly the same in all the four scenarios; for FCR, regression coefficients in univariate models deviated more from 1 than those in bivariate models. In YY, for ADG, scenario *BI_MF-SSGBLUP* was best among the four different scenarios since the regression coefficients were closest to 1. For FCR, there were no dramatic differences among the four scenarios. When ω was 0.15, genomic predictions presented smallest biasedness in all the scenarios.

Similarly, the biasedness of genomic predictions was studied separately in both genotyped and non-genotyped subgroups of validation populations. The results of biasedness with an estimated optimal ω in the four scenarios are shown in Table 4. Overall, animals in the non-genotyped animals had less biasedness of genomic prediction than those in the genotyped subgroup.

Discussion

In this work, we compared the performances of genomic evaluation in both regular

SSGBLUP and MF-SSGBLUP for the important productive traits ADG and FCR in both DanBred Landrace and DanBred Yorkshire pigs. We first estimated γ for constructing $\mathbf{H}(\gamma)^{-1}$ matrix in MF-SSGBLUP, then compared genetic parameters and predictive abilities between SSGBLUP and MF-SSGBLUP, either in a univariate or a bivariate model. Through this study, we also detected the optimal weighting factors for ADG and FCR in both SSGBLUP and MF-SSGBLUP.

Estimation of γ in MF-SSGBLUP

In the current study, γ estimates were 0.605 and 0.553 in MF-SSGBLUP of LL and YY populations respectively, which were different from other estimates in these populations (0.756 of LL and 0.730 of YY) [12]. As mentioned in Legarra et al. [5], several factors influence the values of γ , such as effective population size, and the SNP panel used. The current study and previous studies originated from the same ancestors, and thus it is not the differences of effective population size that affect these estimates. However, the SNP used in this study are fewer than in the previous study, about 37,500 SNP in this study compared to the 41,000 SNP were used in the previous study. The cause of this difference is the difference in criteria on minor allele frequencies (MAF) used in the two studies: In the current study, the criteria of MAF was 0.05 in each of the two populations, whereas in Xiang et al. [12] the criteria was 0.01 across LL and YY populations. The additional low MAF SNPs used in Xiang et al. [12] have increased the estimates of the metafounder parameter γ since there are more homozygote genotypes for such low MAF markers. In practice, γ needs to be

estimated depending on the SNP used in the analysis.

Genetic parameters

Before being compared to genetic parameters in SSGBLUP, variance components in MF-SSGBLUP were scaled to be comparable with the results from regular population that assumed base individuals are unrelated [5, 18]. Overall, estimates in MF-SSGBLUP were not far from those in regular SSGBLUP method. In YY, additive genetic variances of ADG and FCR in two metafounder scenarios were slightly higher than estimates in regular SSGBLUP scenarios. For environmental variances, estimates were nearly the same in all the four scenarios. Thus, the heritabilities of ADG and FCR in two metafounder scenarios were also a little higher than results in the regular SSGBLUP scenarios.

For both MF-SSGBLUP and SSGBLUP, although univariate models and bivariate models gave similar estimates of genetics variances, the slight decrease of standard errors in bivariate models indicated that compared with univariate models, bivariate models would further reduce the uncertainty of the estimated genetics parameters. Genetic correlations between ADG and FCR (r_g) were estimated in bivariate models. Although MF-SSGBLUP in LL showed more negative correlation (-0.27) than that in SSGBLUP (-0.19), taking the standard error (0.10) into account, there were no significant differences for the estimated r_g in MF-SSGBLUP and in SSGBLUP.

Predictive abilities

Predictive abilities changed slightly with different weighting factors (ω). We termed

378 the weighting factor ω that resulted in a highest predictive abilities as the optimal ω .
 379 For ADG, optimal ω were almost the same in LL and YY (around 0.2), but for FCR,
 380 optimal ω were dramatically different in LL (around 0.7) and YY (around 0.1). A
 381 possible reason could be that for different traits and populations, proportions of
 382 genetic variances that could be accounted by 50K SNP markers were quite different.
 383 For FCR, genes that largely affected FCR were not consistent in LL and YY [21] and
 384 thus, the linked SNP markers captured different proportion of total genetic variances.
 385 Martini et al. [22] reported that high ω would increase inflation by increasing the
 386 variance of EBVs. Thus, choosing an optimal ω to construct combined pedigree-based
 387 and genomic-based relationship matrix is crucial in genomic evaluation.
 388 Magnitudes of predictive abilities in this study were higher than those in a previously
 389 published study [9]. The main reason for enhanced predictive ability was due to the
 390 increased population size. In addition, based on the published results from the same
 391 populations, accuracies for ADG and FCR in SSGBLUP in this study were higher
 392 than accuracies of total number of piglets born [23]. This could due to a fact that total
 393 number of piglets born had lower heritabilities than those in ADG and FCR. As shown
 394 in Table3, genotyped subgroups had higher predictive abilities than non-genotype
 395 subgroups in all scenarios for ADG and FCR in LL and YY populations. Similar
 396 results were reported in some previous studies [9, 12]. However, Guo et al. [24]
 397 reported that reliabilities of non-genotyped subgroups were higher than those of
 398 genotyped subgroups for total number of piglets born and litter size at Day 5 after

birth in LL population. They interpreted that phenomenon as decreased relationships between phenotypes and genotypes due to pre-selection of genotyped animals. Forni et al. [25] also reported that marker information only increased accuracies of genotyped individuals in SSGBLUP method. In this study, although genotyped animals were pre-selected, genomic information from large number of genotyped animals still provided enough information to improve the performance of genomic prediction. Nevertheless, one consequence of pre-selection was that genotyped subgroups showed more biasedness in genomic prediction than non-genotyped subgroups, whereas biasedness in non-genotyped subgroup was similar to that in the whole population.

Compared with SSGBLUP, there was a trend that MF-SSGBLUP method performed slightly better in genomic predictions for ADG and FCR, although the differences were not always statistically significant. This finding was in agreement with the theory that MF-SSGBLUP should perform at least as good as SSGBLUP method [5]. All in all, MF-SSGBLUP was recommended to be used for pig genomic evaluation.

Conclusion

MF-SSGBLUP method was successfully implemented in genomic prediction for ADG and FCR in Danish Landrace and Yorkshire populations. The method of single-step genomic evaluation with a metafounder performed at least as good as regular single-step method in genomic evaluation for ADG and FCR in Danish Landrace and

Yorkshire populations. Bivariate models were recommended instead of univariate models for the metafounder approach for the correlated productive traits. The optimal weighting factors (ω) in SSGBLUP and MF-SSGBLUP methods were not completely identical.

Availability of data and materials

The datasets in the current study are not publicly available since they are owned by SEGES, but are available from the corresponding author on reasonable request and if agreed by SEGES.

Abbreviations

SSGBLUP: Single-step genomic best linear unbiased prediction

MF-SSGBLUP: a single-step genomic method with a metafounder

FCR: feed conversion ratio

ADG: average daily gain

LL: DanBred Landrace

YY: DanBred Yorkshire

GEBVs: genomic estimated breeding values

GS: genomic selection

GLS: generalized least squares

MAF: minor allele frequencies

441

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532 **Contributions**

533 CF and TX performed data analysis and wrote the manuscript. OFC, TX and TO

534 conceived the study, made substantial contributions to the interpretation of results and

535 revised the manuscript. TO provided with the data and improved the manuscript and

536 added valuable comments during the study. All authors read and approved the final

537 manuscript.

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541

542 **Ethics declarations**

543 **Ethics approval and consent to participate**

544 Data recording and sample collection were conducted following Danish laws of

545 management and welfare procedures for pig production.

546

547 **Competing interests**

548 The authors declare that they have no competing interests.

549

Table and figure

Table1 numbers of animals with records of ADG and FCR in the training and in the validation dataset, respectively, as well as the numbers of genotyped animals in the two datasets

LL	Training	Validation
ADG	654,908	31,512
FCR	17,901	988
Genotyped	29,825	7,700
Genotyped and FCR	2,660	902

YY	Training	Validation
ADG	541,301	29,192
FCR	18,478	909
Genotyped	30,144	7,645
Genotyped and FCR	2,802	870

ADG = average daily gain; FCR = feed conversion ratio.

Note: all genotyped animals have ADG record, but only some have FCR record.

558 Table2. Variance components,¹ heritabilities,² and genetic correlations between ADG and FCR with SE in LL and YY populations, respectively

Model	scenario	Breed	$\sigma_{a_ADG}^2$	σ_{a_ADG,a_FCR}	$\sigma_{a_FCR}^2$	σ_{pen}^2	σ_{litter}^2	$\sigma_{e_ADG}^2$	$\sigma_{e_FCR}^2$	$h_{a_ADG}^2$	$h_{a_FCR}^2$	r_g
BLUP	all	LL	1916.33	-0.56 (0.44)	4.12*10-3	633.35	455.57	4544.12	2.82*10-2	0.25	0.13	-0.20
			(98.71)		(2.55*10-3)	(69.57)	(77.25)	(96.21)	(2.49*10-3)	(0.05)	(0.06)	(0.11)
		YY	2039.74	-1.19 (0.22)	3.60*10-3	577.24	445.98	5144.01	1.55*10-2	0.25	0.19	-0.44
			(117.88)		(6.4710-4)	(57.33)	(62.07)	(94.21)	(6.19*10-3)	(0.05)	(0.05)	(0.15)
	UNI_SSGBLUP	LL	1899.91	-	3.44*10-3	669.29	510.24	4787.67	2.87*10-2	0.24	0.11	-
			(99.30)		(2.61*10-3)	(64.02)	(81.99)	(95.34)	(2.53*10-3)	(0.04)	(0.06)	
		YY	2168.95	-	3.75*10-3	571.73	422.21	5092.61	1.54*10-2	0.26	0.19	--
			(116.30)		(5.95*10-4)	(56.91)	(61.32)	(93.86)	(5.69*10-3)	(0.04)	(0.04)	
SSGBLUP(w=0.25)	BI_SSGBLUP	LL	1882.02	-0.48 (0.42)	3.35*10-3	691.50	527.58	4885.49	2.88*10-2	0.24	0.10	-0.19
			(96.75)		(2.42*10-3)	(50.15)	(63.81)	(90.25)	(2.47*10-3)	(0.04)	(0.06)	(0.09)
		YY	2174.28	-1.28 (0.31)	3.58*10-3	568.85	418.41	5080.37	1.56*10-2	0.26	0.19	-0.46

			(110.43)		(5.26*10-4)	(54.42)	(70.61)	(100.25)	(4.22*10-3)	(0.03)	(0.04)	(0.13)
	<i>UNI_MF-SSGBLUP</i>	LL	1885.58	-	3.46*10-3	721.22	529.21	4894.98	2.88*10-2	0.23	0.11	-
			(102.48)		(2.59*10-3)	(59.25)	(65.23)	(95.54)	(2.61*10-4)	(0.04)	(0.07)	
		YY	2305.03	-	3.79*10-3	570.11	415.72	5077.82	1.56*10-2	0.27	0.20	-
			(122.34)		(6.31*10-4)	(56.87)	(61.25)	(93.91)	(5.72*10-4)	(0.03)	(0.03)	
MF-SSGBLUP(w=0.25)	<i>BI_MF-SSGBLUP</i>	LL	1887.71	-0.68 (0.43)	3.48*10-3	727.64	532.84	4916.36	2.87*10-2	0.23	0.11	-0.27
			(97.14)		(2.41*10-3)	(53.62)	(63.94)	(91.40)	(2.50*10-3)	(0.05)	(0.05)	(0.10)
		YY	2311.95	-1.37 (0.22)	3.86*10-3	567.00	411.53	5065.37	1.55*10-2	0.28	0.20	-0.46
			(118.92)		(5.91*10-4)	(60.40)	(57.75)	(88.41)	(5.01*10-4)	(0.03)	(0.03)	(0.12)

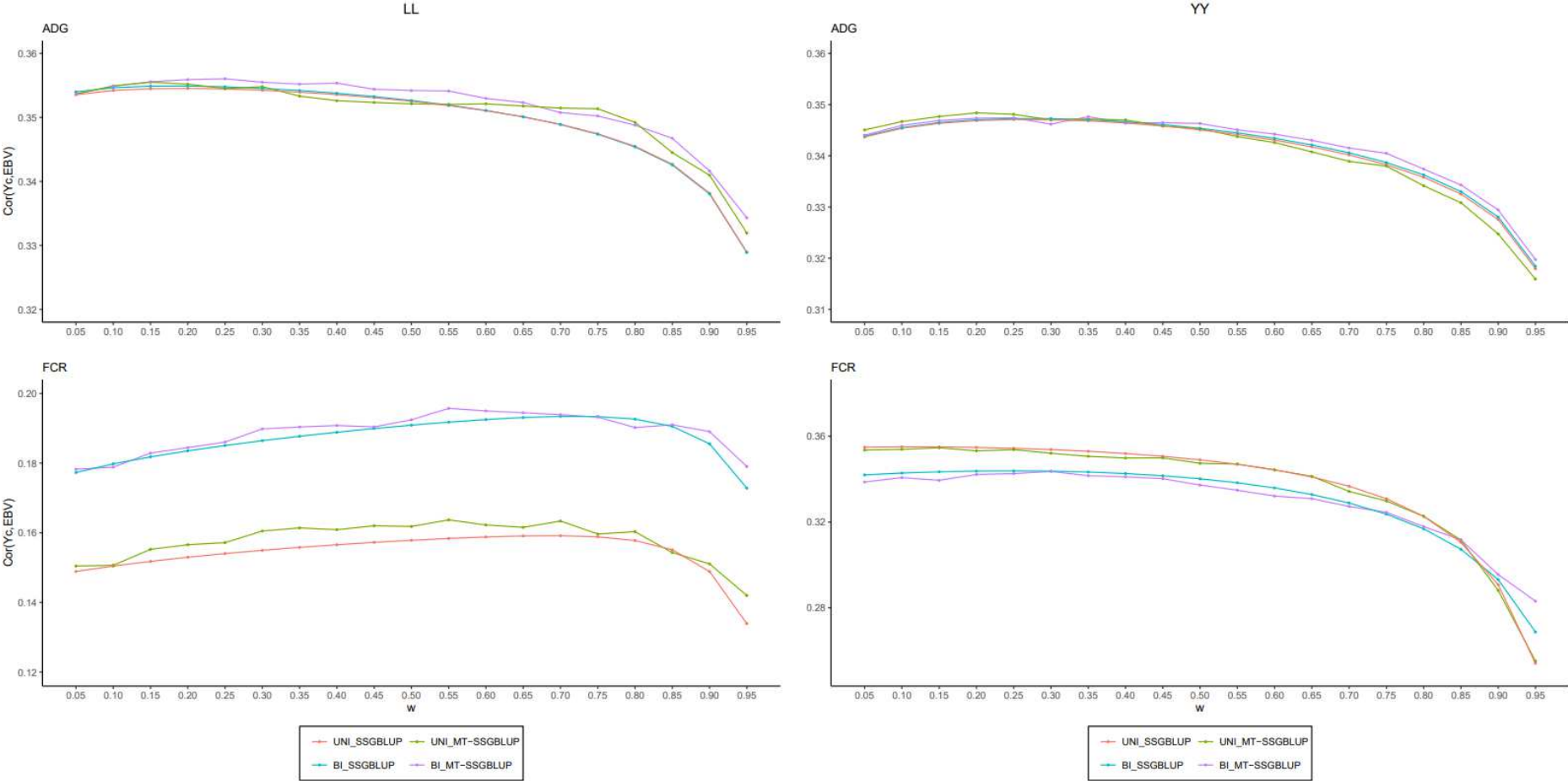
559 ¹Variance components for genetic parameters correspond to the usual genetic variance, which is the variance among unrelated individuals in base
560 population:

561 In SSGBLUP, $\sigma_{a_{ADG}}^2$ is the additive genetic variance for ADG, and in MF-SSGBLUP = $\sigma_{a_{ADG}}^2 * (1 - \gamma_L/2)$ for LL and $\sigma_{a_{ADG}}^2 * (1 -$
562 $\gamma_Y/2)$ for YY; in SSGBLUP, $\sigma_{a_{FCR}}^2$ is the additive genetic variance for FCR, and in MF-SSGBLUP = $\sigma_{a_{FCR}}^2 * (1 - \gamma_L/2)$ for LL and

563 $\sigma_{a_{FCR}}^2 * (1 - \gamma_Y/2)$ for YY; in SSGBLUP $\sigma_{a_{ADG,a_{FCR}}}$ is genetic covariance between ADG and FCR, and in MF-SSGBLUP $= \sigma_{a_{ADG,a_{FCR}}} * (1 - \gamma_L/2)$ for LL and $\sigma_{a_{ADG,a_{FCR}}} * (1 - \gamma_Y/2)$ for YY; σ_{pen}^2 is the variance of pen effect for ADG; σ_{litter}^2 is the variance of litter effect for ADG; $\sigma_{e_{ADG}}^2$ is the residual variance for ADG; $\sigma_{e_{FCR}}^2$ is the residual variance for FCR. Numbers between brackets are the SE of the corresponding parameters.

567 ²Heritability, in SSGBLUP, $h_{ADG}^2 = \frac{\sigma_{a_{ADG}}^2}{\sigma_{a_{ADG}}^2 + \sigma_{litter}^2 + \sigma_{pen}^2 + \sigma_{e_{ADG}}^2}$ for ADG, and in MF-SSGBLUP, $= \frac{\sigma_{a_{ADG}}^2 * (1 - \gamma_L/2)}{\sigma_{a_{ADG}}^2 * (1 - \gamma_L/2) + \sigma_{litter}^2 + \sigma_{pen}^2 + \sigma_{e_{ADG}}^2}$ for LL and
568 $\frac{\sigma_{a_{ADG}}^2 * (1 - \gamma_Y/2)}{\sigma_{a_{ADG}}^2 * (1 - \gamma_Y/2) + \sigma_{litter}^2 + \sigma_{pen}^2 + \sigma_{e_{ADG}}^2}$ for YY; in SSGBLUP, $h_{FCR}^2 = \frac{\sigma_{a_{FCR}}^2}{\sigma_{a_{FCR}}^2 + \sigma_{e_{FCR}}^2}$ for FCR, and in MF-SSGBLUP, $= \frac{\sigma_{a_{FCR}}^2 * (1 - \gamma_L/2)}{\sigma_{a_{FCR}}^2 * (1 - \gamma_L/2) + \sigma_{e_{FCR}}^2}$ for LL
569 and $\frac{\sigma_{a_{FCR}}^2 * (1 - \gamma_Y/2)}{\sigma_{a_{FCR}}^2 * (1 - \gamma_Y/2) + \sigma_{e_{FCR}}^2}$ for YY.
570 ³Genetic correlation $r_g = \frac{\sigma_{a_{ADG,a_{FCR}}}}{\sqrt{\sigma_{a_{ADG}}^2 * \sigma_{a_{FCR}}^2}}$

571 Figure 1



572

573

574 Table3. Accuracies of the optimal weighting factors (ω) in four scenarios from different validation groups for ADG and FCR

Population	Trait	Validation group	<i>UNI_SSGBLUP</i>	<i>UNI_MF-SSGBLUP</i>	<i>BI_SSGBLUP</i>	<i>BI_MF-SSGBLUP</i>
LL	ADG	All	0.3545 ^a	0.3555 ^a	0.3549 ^a	0.3560 ^a
		Genotyped	0.4096 ^a	0.4098 ^a	0.4101 ^a	0.4102 ^a
		Non-genotyped	0.3269 ^a	0.3268 ^a	0.3264 ^a	0.3269 ^a
	FCR	All	0.1921 ^a	0.1933 ^a	0.1934 ^a	0.1957 ^b
		Genotyped	0.2001 ^a	0.2060 ^b	0.2013 ^a	0.2064 ^b
		Non-genotyped	0.1672 ^a	0.1703 ^a	0.1786 ^b	0.1795 ^b
YY	ADG	All	0.3471 ^a	0.3472 ^a	0.3473 ^a	0.3474 ^a
		Genotyped	0.3946 ^a	0.3945 ^a	0.3942 ^a	0.3941 ^a
		Non-genotyped	0.3086 ^a	0.3088 ^a	0.3092 ^a	0.3081 ^a
	FCR	All	0.3550 ^a	0.3547 ^a	0.3438 ^b	0.3435 ^b

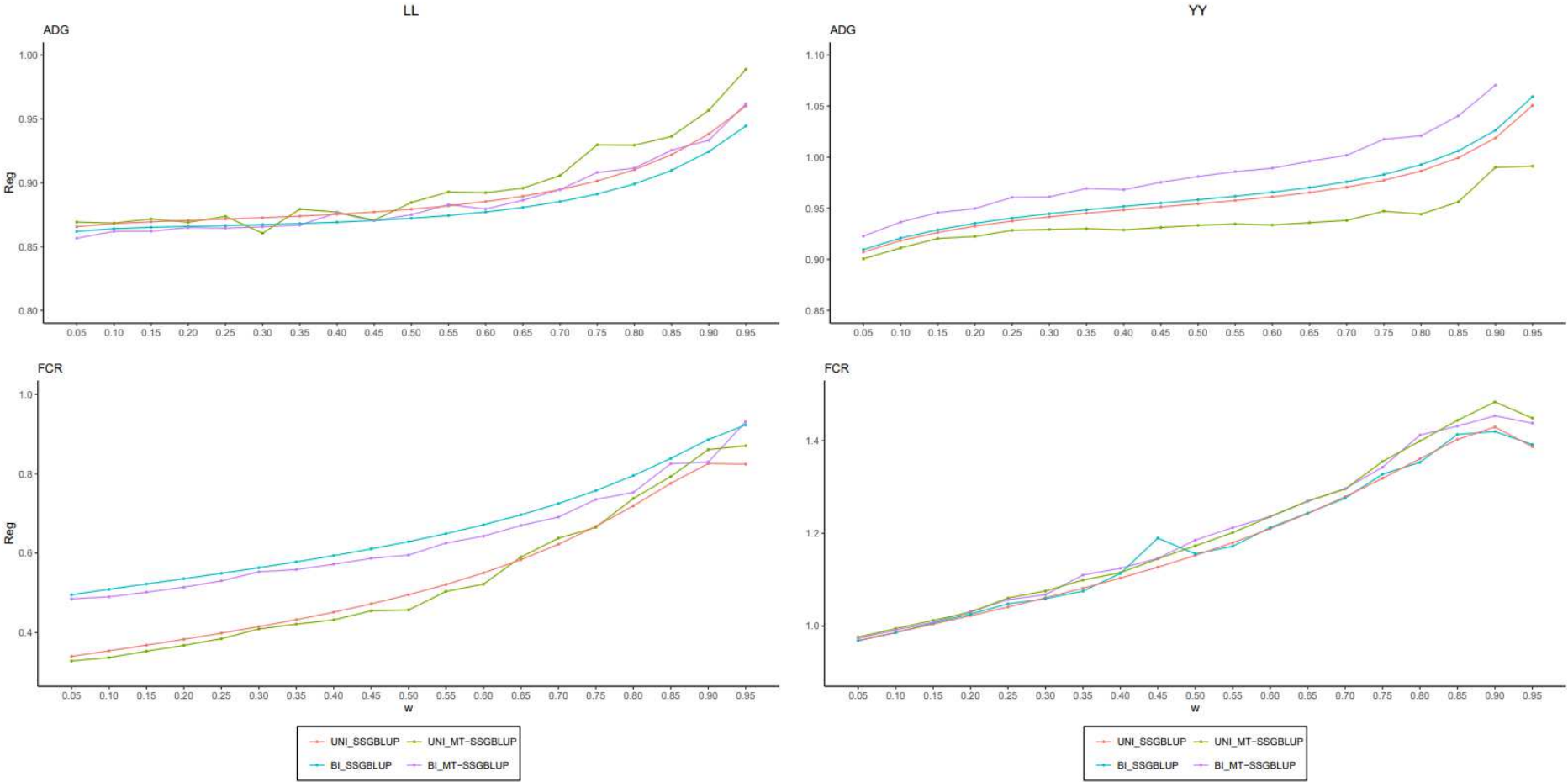
	(ω=0.10)	Genotyped	0.3699 ^a	0.3671 ^a	0.3574 ^b	0.3561 ^b
		Non-genotyped	0.1179 ^a	0.1214 ^a	0.1167 ^a	0.1139 ^a

575 Four scenarios are *UNI_SSGBLUP*, *UNI_MF-SSGBLUP*, *BI_SSGBLUP* and *BI_MF-SSGBLUP*.

576 Validation groups include a validation population of all young pigs born between 1 May 2016 and 1 February 2017, and a genotyped and a
577 non-genotyped subgroup which were separated by the validation population.

578 Different superscripts of small letters among scenarios indicate significant differences ($p < 0.05$) by Hotelling-Williams t-test

579 Figure 2



580

Table4. Biases of the optimal weighting factors (ω) in four scenarios from different validation groups for ADG and FCR

Population	Trait	Validation group	<i>UNI_SSGBLUP</i>	<i>UNI_MF-SSGBLUP</i>	<i>BI_SSGBLUP</i>	<i>BI_MF-SSGBLUP</i>
LL	ADG ($\omega=0.20$)	All	0.9600	0.9888	0.9445	0.9618
		Genotyped	0.7334	0.7386	0.7324	0.7375
		Non-genotyped	0.8379	0.8394	0.8289	0.8281
	FCR ($\omega=0.70$)	All	0.8241	0.8705	0.9230	0.9310
		Genotyped	0.5419	0.4789	0.5650	0.5241
		Non-genotyped	1.0776	1.2833	0.7638	0.8809
YY	ADG ($\omega=0.25$)	All	0.9994	0.9912	1.0060	1.0019
		Genotyped	0.7425	0.7418	0.7498	0.7595
		Non-genotyped	0.8668	0.8655	0.8704	0.8856

	FCR	All	1.0040	1.0122	1.0064	1.0080
	(ω=0.10)	Genotyped	0.4721	0.4876	0.4832	0.5019
		Non-genotyped	1.0064	0.9962	1.0054	0.9991

Four scenarios are *UNI_SSGBLUP*, *UNI_MF-SSGBLUP*, *BI_SSGBLUP* and *BI_MF-SSGBLUP*.

Validation groups include a validation population of all young pigs born between 1 May 2016 and 1 February 2017, and a genotyped and a non-genotyped subgroup which were separated by the validation population.

Figures

Figure 1

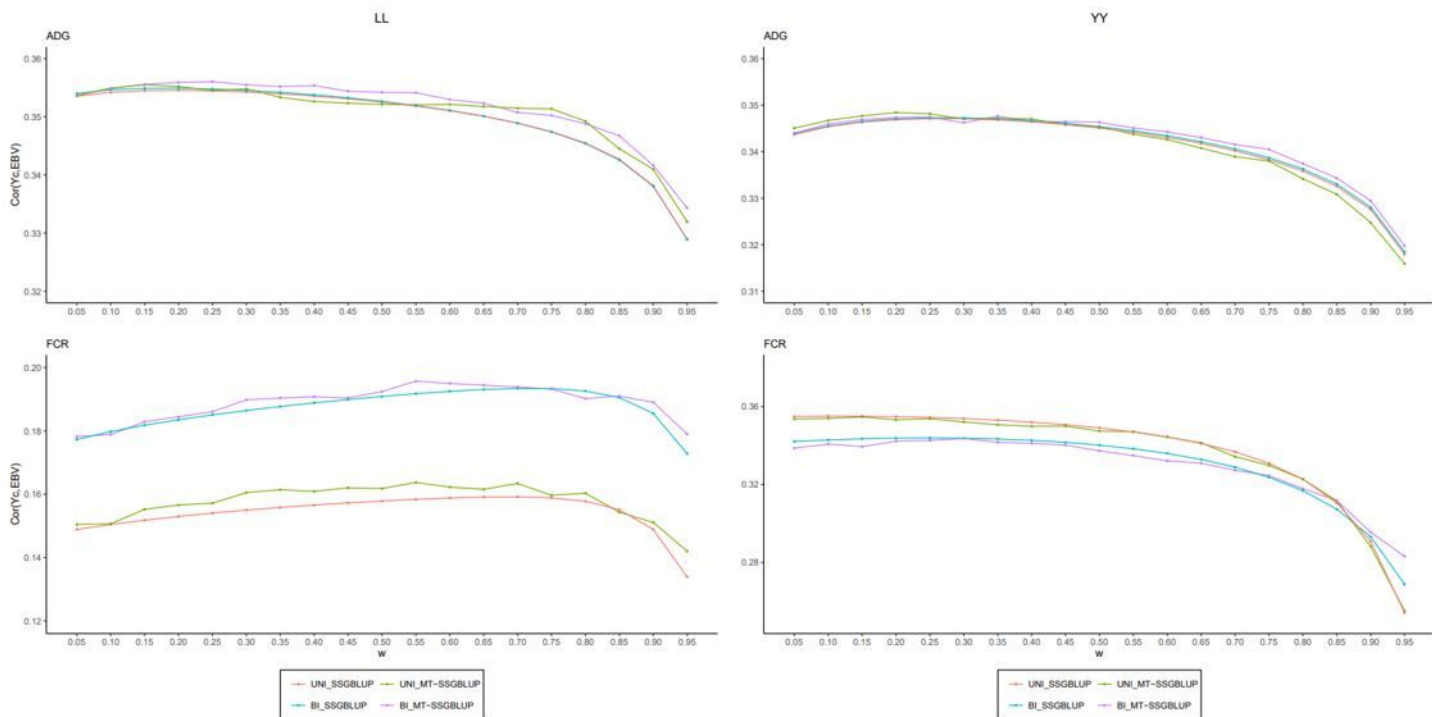


Figure 1

The diagrams of correlation coefficients between corrected phenotypes (Y_c) of ADG and FCR, and genomic estimated breeding values (\hat{a}) in different scenarios ($\text{cor}(Y_c, \hat{a})$) with a dynamic ω are shown in Figure 1.

Figure 2

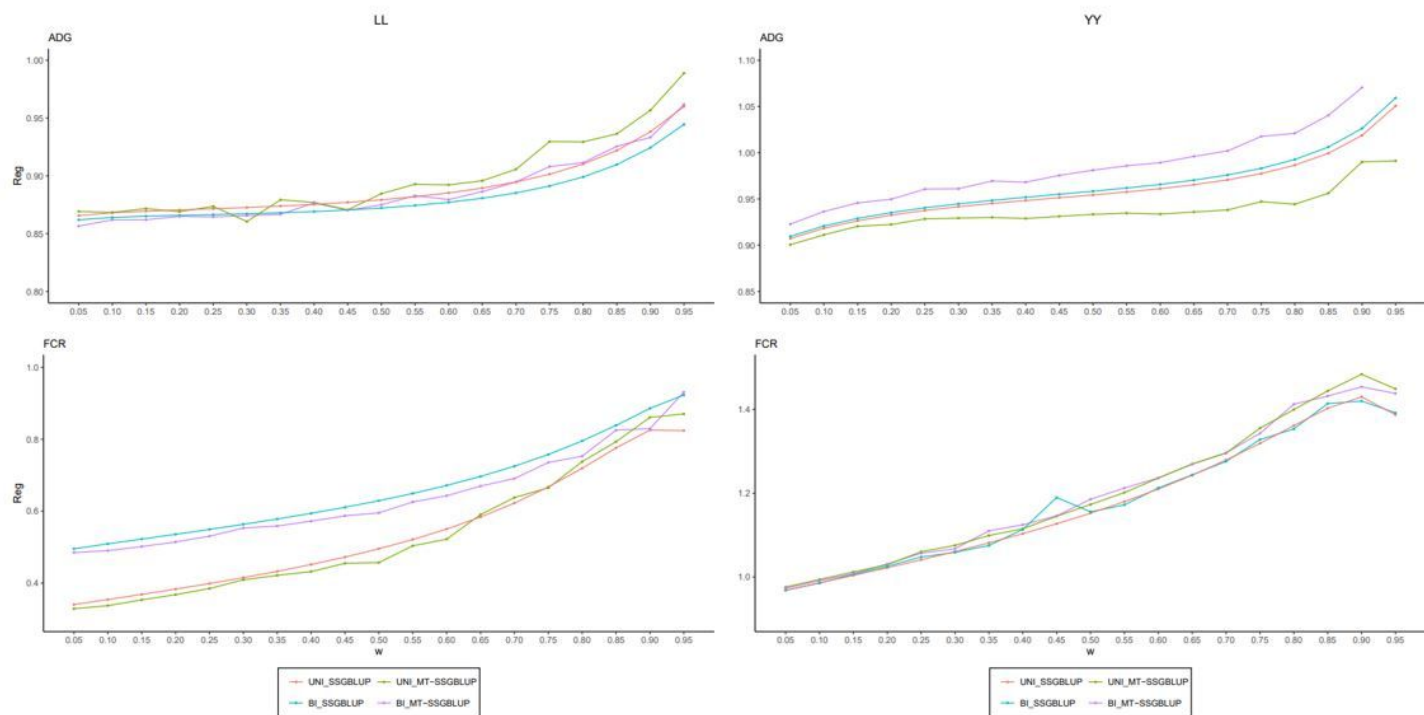


Figure 2

The changes of biasedness for both ADG and FCR in different scenarios in both LL and YY with ω ranging from 0.05 to 0.95 with a gap of 0.05 are shown in Figure 2.