

# Supporting Online Materials

## Does drought show a significant decreasing trend from 1961 to 2017 in northern China?

### S1 Computation of SPEI

According to previous studies (Vicente-Serrano et al. 2010; Wang et al. 2020; Wu et al. 2020; Beguería et al. 2014), the computation of the SPEI is as follows:

Firstly, based on precipitation and potential evaporation, Penman-Monteith equation has been successfully applied in both humid and arid climates around the world. The formula of potential evapotranspiration is:

$$PET = 16K \left( \frac{10T}{I} \right)^m \quad (1)$$

where  $T$  is the monthly mean temperature ( $^{\circ}\text{C}$ );  $I$  is a heat index, which is calculated as the sum of 12 monthly index values;  $m$  is a coefficient depending on  $I$ ,  $m = 6.75 \times 10^{-7} I^3 - 7.71 \times 10^{-5} I^2 + 1.79 \times 10^{-2} I + 0.492$ ; and  $K$  is a correction coefficient computed as a function of the latitude and month.

Secondly, based on climatic water balance, SPEI is determined by standardizing difference between precipitation ( $P$ ) and PET for the month  $i$ :

$$D_i = P_i - PET_i \quad (2)$$

where  $P_i$  and  $PET_i$  denote the aggregated precipitation and PET for the given month  $i$ .

The difference  $X_{i,j}^k$  in month  $j$  and year  $i$  depends on the different time scale  $k$ . For instance, the accumulated difference for 1 month in a particular year  $i$  with a 12-month

23 time scale is calculated as follows:

$$\begin{aligned} 24 \quad X_{i,j}^k &= \sum_{l=13-k+j}^{12} D_{i-1,l} + \sum_{l=1}^i D_{i,l}, \text{ if } j < k, \\ 25 \quad X_{i,j}^k &= \sum_{l=j-k+1}^j D_{i,l}, \text{ if } j \geq k \end{aligned} \quad (3)$$

26 where  $D_{i,l}$  is the difference between P and PET in the first month of year  $i$ .

27 Thirdly, after standardized  $X_{i,j}^k$  data sequence, the log-logistic probability  
28 distribution is selected to obtain the SPEI series. The cumulative function of this  
29 distribution is expressed as:

$$30 \quad f(x) = \left[ 1 + \left( \frac{\alpha}{x - \gamma} \right)^\beta \right]^{-1} \quad (4)$$

31 where  $\alpha$ ,  $\beta$ , and  $\gamma$  are scale, shape, and origin parameters, respectively.

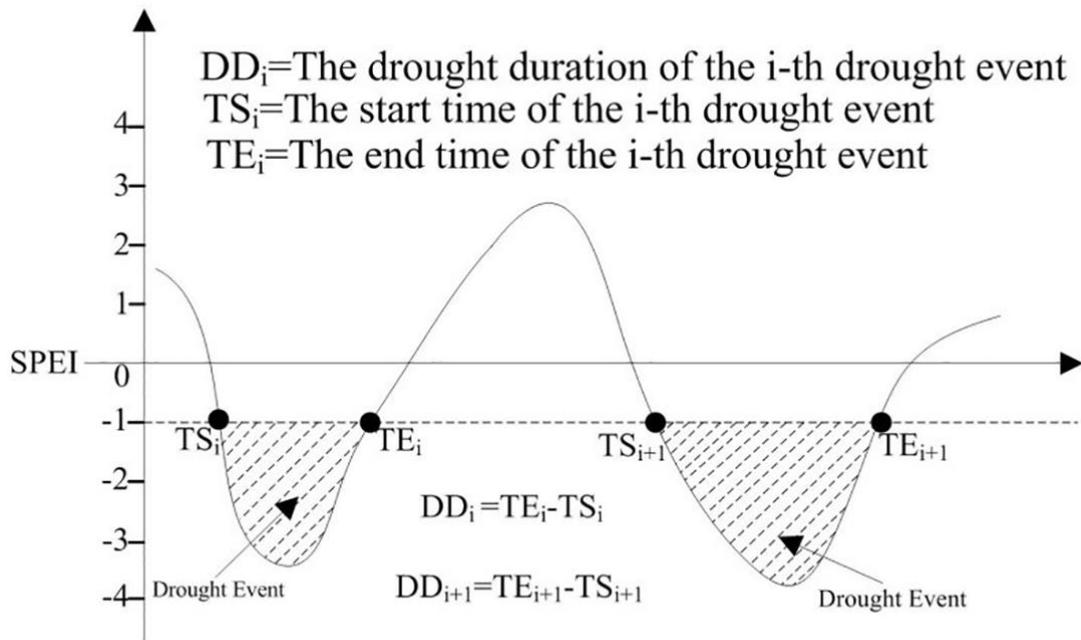
32 Thus, SPEI is given by the standardized values of  $f(x)$ :

$$33 \quad SPEI = W - \frac{C_0 + C_1 W + C_2 W^2}{1 + d_1 W + d_2 W^2 + d_3 W^3} \quad (5)$$

34 where  $W = \sqrt{-2 \ln(P)}$  for  $P \leq 0.5$ ,  $P$  is the probability of a defined  $X_{i,j}^k$  value and  
35  $P = 1 - f(x)$ . If  $P > 0.5$ , then  $P$  is replaced by  $1 - P$  and the sign of SPEI is reversed. Other  
36 constants are  $C_0 = 2.515517$ ,  $C_1 = 0.802853$ ,  $C_2 = 0.010328$ ,  $d_1 = 1.432788$ ,  $d_2 =$   
37  $0.189269$ , and  $d_3 = 0.001308$ .

## 38 **S2 Definition of drought duration**

39 According to Wu et al. (2020), the drought duration of the  $i$ -th drought event (DD $_i$ ) was  
40 calculated as the difference between the end time of the  $i$ -th drought event (TE $_i$ ) and  
41 the start time of the  $i$ -th drought time (TS $_i$ ). In this study, the total drought duration  
42 (DD) is defined as the sum of all DD $_i$  over different period (Fig. S1).



43

44

Fig. S1 Definition of the drought duration for i-th drought event

45

## 46 References

47 Beguería S, Vicente-Serrano SM, Reig F, Latorre B (2014) Standardized precipitation

48 evapotranspiration index (SPEI) revisited: parameter fitting, evapotranspiration

49 models, tools, datasets, and drought monitoring. *Int J Climatol* 34(10):3001-

50 3023

51 Vicente-Serrano, Sergio M, Beguería, Santiago, López-Moreno, Juan I (2010) A

52 multiscale drought index sensitive to global warming: the Standardized

53 Precipitation Evapotranspiration Index. *J Climate* 23 (7)

54 Wang XY, Zhuo L, Li C, Engel BA, Sun SK, Wang YB (2020) Temporal and spatial

55 evolution trends of drought in northern Shaanxi of China: 1960–2100. *Theor Appl*

56 *Climatol* 139(3-4):965-979

57 Wu ZT, Yu L, Du ZQ, Zhang H, Fan XH, Lei TJ (2020) Recent changes in the drought

58 of China from 1960 to 2014. *Int J Climatol* 40:3281–3296

59

60