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Investigating the causal inference of vaccine on COVID-19 disease propagation based on Bayesian approach

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ABSTRACT

The causal impact of COVID-19 vaccine coverage on effective reproduction number $R(t)$ under the disease control measures in the real-world scenario is understudied, making the optimal reopening strategy (e.g., when and which control measures are supposed to be conducted) during the recovery phase difficult to design. In this study, we examine the demographic heterogeneity and time variation of the vaccine effect on disease propagation based on the Bayesian structural time series analysis. Furthermore, we explore the role of non-pharmaceutical interventions (NPIs) and the entrance of the Delta variant of COVID-19 in the vaccine effect for U.S. counties. The analysis highlights several important findings: First, vaccine effects vary among the age-specific population and population densities. The vaccine effect for areas with high population density or core airport hubs is 2 times higher than for areas with low population density. Besides, areas with more older people need a high vaccine coverage to help them against the more contagious variants (e.g., the Delta variant). Second, the business restriction policy and mask requirement are more effective in preventing COVID-19 infections than other NPI measures (e.g., bar closure, gather ban, and restaurant restrictions) for areas with high population density and core airport hubs. Furthermore, the mask requirement consistently amplifies the vaccine effects against disease propagation after the presence of contagious variants. Third, areas with a high percentage of older people are suggested to postpone relaxing the restaurant restriction or gather ban since they amplify the vaccine effect against disease infections. Such empirical insights assist recovery phases of the pandemic in designing more efficient reopening strategies, vaccine prioritization, and allocation policies.

Introduction

The COVID-19 pandemic has been reported to cause 6 million deaths worldwide since its initial outbreak in 2019 and has deeply disrupted all aspects of daily life¹. In the absence of vaccines against COVID-19 infection, mitigation of disease propagation was mostly achieved by implementing a wide range of non-pharmaceutical interventions (NPIs) and actions by restricting movement¹ throughout the world, ranging from the emergency declaration, lockdowns, closure of non-essential businesses, social distancing mandates, to the increased testing and tracing. The trade-off between disease prevention and movement restrictions sacrifices the economy and social needs. Indeed, the speed and extent of COVID-19 propagation have challenged the economic system and public health care system of many counties across the world¹,². Fortunately, lab experiments proved vaccines efficacy in against COVID-19 infection³,⁴, such as Pfizer-BioNTech, Moderna, or Janssen COVID-19 vaccines. An opportunity for a gradual reintroduction of active business events and mobile population by lifting the NPIs can be achieved based on the availability of vaccines. However, vaccine efficacy varies on the age-specific population³,⁴ and is proved to be decay over time³. That makes the causal impact of vaccine coverage on disease spread rate in the real-world scenario, measured as the decreased quantity of effective reproduction number $R(t)$ caused by vaccine coverage, vary in a temporal-spatial granularity. This fact could make the economic recovery process in the U.S. confront numerous obstacles while reestablishing a productive and socially acceptable environment. Indeed, CDC⁵,⁶ indicated that NPIs are still needed to prevent disease propagation and mortality during the process of increasing vaccine coverage. Besides, Wang et al. (2021)⁷ pointed out that prematurely reopening social contacts could initiate a new pandemic in the U.S. if vaccine coverage is low. Hence, quantifying the causal impact of vaccine coverage on $R(t)$, defined as the vaccine effect in our study, is essential to assist optimal reopening strategies, which is critical to relieving the socio-economic burden in the COVID-19 emergency phase⁸.

Previous studies⁵,⁶ have analyzed the causal impact of the vaccine on disease infections through lab experiments and a small-scale of targeted people. Although such studies provide a general understanding of the vaccine effect in a controllable environment, they retain two critical drawbacks. First, observations are limited to an ideal setting by ignoring the multiple
influencing factors, which introduces biases when adopting it to real-world scenarios. Second, the applied methods fail to model the causal effect of the vaccine in a quantifiable, continuous, and longitudinal manner, which requires a statistical framework that predicts the performances of $R(t)$ if the vaccine coverage is below the designed value. In real-world scenarios, the difficulty of investigating the causal impact of vaccine coverage is the confounding issue caused by influencing factors of $R(t)$. Indeed, the larger airport hubs is an important indicator that produces a high influx of imported infections and boosts the local transmission of the virus. Besides, the local disease dynamics is greatly influenced by factors such as the demographic characteristics, the presence of disease variants, the protective behavior from imposed policies (e.g., mask requirement), mobility index and social contacts.

In this study, to overcome the aforementioned issues, we first classify the U.S. counties into four groups based on county-level demographic information (e.g., population density, hospital bed capacity, median household income, and the percentage of the older people) and core airport hubs. This procedure specifies the experiment by testing the causal impact of vaccine coverage within each county group. Then, we cut the study period from January to July 2021 into six continued experiments corresponding to vaccine coverage of 0%, 10%, 20%, 30%, 40%, and 50%. That makes the influencing policies much more controllable within a shorter period. Besides, we consider a set of covariates in the model to avoid the confounding issue, such as the NPI measures (e.g., business reopening policy, restaurant restriction, bar closure, gather ban, and mask requirement), the presence of Delta variant, mobility index, and the hospital bed utilization rate. Last but not least, we apply the Bayesian structural time series (BSTS) model to capture the causal impact over a longitudinal time horizon rather than 2 static points, which is much more flexible than the conventional difference in difference models and Rubin causal model. The overview of the study is presented in Figure 1, which contains objective, input data, model framework, and results. This study aims to shed light on: first, demographic heterogeneity and longitudinal time variation of the causal impact of vaccine coverage on disease propagation; second, the role of NPI measures on the vaccine effect and disease propagation. We propose four corresponding hypotheses to investigate these research questions: (H1) Vaccine coverage has a higher impact on preventing the disease spread in counties without core airport hubs than in counties with core airport hubs. (H2) Mask requirement has a higher effect on decreasing disease spread for counties with low population density than counties with high population density. (H3) The vaccine effect for counties relaxing NPIs in the early time is significantly higher than for counties relaxing NPIs later. (H4) Mask requirement amplifies the vaccine effect under the presence of the Delta variant. The exploration of these hypotheses helps to gain knowledge about the effect of the COVID-19 vaccine and the NPIs in a real-world scenario. Furthermore, it assists in the economic recovery process in designing vaccine prioritization and reopening strategy for COVID-19 as well as further pandemics.

Figure 1. Study overview
Results

The causal impact of vaccine coverage on effective reproduction number $R(t)$ for counties with different demographics

To investigate the first hypothesis, we aggregate the causal impact of vaccine coverage on $R(t)$ over the time horizon by county category and coverage level. The mean and standard deviation in Figure 2 A-D characterize the temporal variation of vaccine effect for 30 consecutive days, and the causal impact in Figure 2 E designates the demographic heterogeneity of cumulative vaccine effect for each county class.

Figure 2. Causal effect of vaccine coverage for counties with different demographics. The demographic characteristics of each county is presented in Table 1.

Figure 2 E presents the average cumulative causal impact ($\Theta = \sum_t \theta_t$, $t = 1, 2, ..., 30$) of vaccine coverage at 0%, 10%, 20%, 30%, 40%, and 50%. The cumulative causal impacts are aggregated by county class for each vaccine coverage. The numbers of $\Theta_i (i = 1, 2, 3, 4)$ should be interpreted as `the number of effective reproduction number $R(t)$-as-usual days worth of impact'. For example, counties with core airport hubs experienced a cumulative median vaccine effect of $\Theta = -2.6$ after 30 consecutive days when vaccine coverage was 10% on March 10, 2021. This suggests that the $R(t)$ was decreased by 2.6 on 30 consecutive days for counties with core airport hubs compared with the $R(t)$ if the vaccine coverage was above 10% on March 10, 2021. Most counties experienced a positive impact at vaccine coverage of 0%, except for counties (`class 1') with high median income, low population density, low percentage of older people, and low hospital bed capacity. The vaccine does not immediately reduce $R(t)$. That might be because that imposed controls measures were gradually relaxed after January 2021, and people’s less cautious about maintaining protective behaviors as soon as they have the injection leading to a surge in infection risk. We also clearly observe the demographic disparity in the negative causal impact of vaccine coverage across county classes from vaccine coverage of 10% to 30%. In particular, the significantly higher vaccine effect for counties with core airport hubs (-3.8) than counties without core airport hubs on average with a t statistic of 73 at 0.05 significance level leads to the rejection of H1. However, the cumulative negative effects gradually shift to positive as vaccine coverage reaches 40% and 50% for all county classes after May 25, 2021, which seems a counter-intuitive observation. The presence of the Delta variant at the end of April 2021 (when vaccine coverage reaches 40%) might account for that observation since it leads to the surge of infection risk and decreases the vaccine effect when it initially spreads, which parallels the previous study.

To further understand the impact of vaccine coverage over a longitudinal time horizon, we summarize the mean and standard
deviation of the point-wise causal impact of vaccine coverage in Figure 2 A-D. Each dot in Figure 2 A-D corresponds to the difference between the actual and the predicted $R(t)$ across time ($\theta_t = R(t) - \hat{R}(t)$) in vaccine coverage of 0%, 10%, 20%, and 30%. The vertical error bars show the standard deviation of the estimated causal effect. The negative value of $\theta_t$ means that the vaccine had a negative impact on $R(t)$, resulting in the decrease of $R(t)$ and otherwise. Several interesting observations can be made from these visualizations. First, we notice that the impact of vaccine coverage on $R(t)$ is not linear. The age-structured vaccine allocation strategy (e.g., the first got vaccinated age group) might be a potential reason for that observation as indicated by Matrajt et al. (2021)21. Second, we see the negative vaccine effect decreases earlier for counties (‘class2’) with a high percentage of older people, low population density, low median household income, and low hospital bed capacity (start at vaccine coverage of 20%) than it for other county classes (start at vaccine coverage of 30%). The surge of infection risk introduced by the Delta variant at the end of April 2021 accounts for the decreased negative vaccine effect4. It also indicates that older people are more vulnerable to being infected by the new variant than others. This finding is consistent with Powels et al. (2021)3. Third, from the cross-comparison of vaccine effects for county classes, the average point-wise vaccine effect for counties with core airport hubs is higher than other counties. A potential reason could be that the people who plan for long travel are more cautious about mask-wearing, which might amplify the vaccine effect by interfering with the virus transmission process13,22.

Role of NPI measures on effective reproduction number $R(t)$ To examine the second hypothesis, we regress NPI measures (e.g., business reopening, restaurant restriction, gather ban, bar closure, and mask requirement) as covariates in a dynamic approach when investigating the vaccine effect. We measure the mean effect of NPIs by calculating the mean of marginal effects in each county and aggregating them based on the county class. Figure 3 summarizes the continuous and longitudinal effect of the NPIs and the presence of the Delta variant on disease infections for each county class at each vaccine coverage.

Figure 3. Average marginal effect of policies on disease infections. The demographic characteristics of each county class is presented in Table 1.

The interpretation of the positive marginal effect of NPI measures should be ‘the increased number of $R(t)$ by relaxing one step of the NPI measure’. And the steps within each NPI measure are presented in Table 2. For example, Figure 3 A shows that relaxing one step of the business reopening policy (e.g., from ‘restrictions’ to ‘easing restriction’) increases 0.0022 of $R(t)$ for counties (‘class3’) with high population density, high median income, high hospital bed capacity, and low percentage of older people at vaccine coverage of 50%. For the impact of NPI measures on $R(t)$, we gain three observations from Figure 3 A-D. First, we see that the marginal effect of relaxing the business reopening policy for high population density counties (‘class3’) is about 3.5 times that of counties with low population density (‘class1’ and ‘class2’). That indicates high population density counties have a higher infection risk by relaxing business reopening policy due to their active commercial activities. Second, we observe a lower marginal effect of relaxing restaurant restriction, gather ban, and bar closure policies on average compared with the marginal effect of relaxing business reopening policy for all counties classes in Figure 3 B, C, and D. Third, We observe that the effects of relaxing mask requirement in Figure 3 E increase along with augmenting vaccine coverage overtime for all counties. In particular, a significantly higher marginal effect (t statistic of 93 at 0.05 significance level) for counties with core
airport hubs (‘airport’) or high population densities (‘class3’) than for counties with relatively low population density (‘class1’ and ‘class2’) leads to the rejection of H2. It indicates that mask requirement is more effective in decreasing disease infection for counties with core airport hubs or high population density. Indeed, Barasheid et al. (2016) suggested that wearing masks in crowded places could reduce the risk of respiratory infections by 20%. More importantly, although the presence of the Delta variant significantly increases the infection risk as described in Figure 3 F, our results indicate that the mask requirement is the more effective than other NPIs in preventing the disease spread after 50% people got vaccinated, which parallels the finding suggested by Brüssow and Zuber (2022).

Role of postponing relaxing NPI measures on vaccine effects To exam the third hypothesis, we selected two groups of counties A and B within the same county class, with group A applying the NPIs 15 days earlier than group B during the study period. Then, we measure the role of NPIs on vaccine effects using the cumulative vaccine effect of the group A to subtract it from group B ($\phi = \sum \Theta_A - \sum \Theta_B$). Figure 4 shows the improved cumulative vaccine effect $\phi$ for each policy. The negative values of $\phi$ mean that vaccine could decrease more number of $R(t)$ by postponing relaxing the control policy for 15 days, otherwise. For example, Figure 4 A indicates that the vaccine could reduce the $R(t)$ by 2 more if counties (with high median household income, relatively low population density, low percentage of older people, and low hospital bed capacity) postponed relaxing the business reopening policy by 15 days ($\phi = -2$ for postponing relaxing business reopening policy).

From Figure 4 A-D, we observe the disparity of the role of NPI measures in the vaccine effect across county classes. Several interesting observations can be made from these visualizations. First, we notice that postponing relaxing the restaurant restriction amplifies the vaccine effect of reducing $R(t)$ for all counties, while postponing relaxing the bar closure barely affects the vaccine effect. This observation leads to the rejection of H3. Second, postponing relaxing mask requirement amplifies the vaccine effect by 2 more times for counties with core airport hubs (‘airport’) and counties (‘class3’) with high population density, high median household income, high hospital bed capacity, and low percentage of older people than counties with low population densities (‘class1’ and ‘class2’). Third, in addition to restaurant restriction, postponing relaxing gather ban can also significantly amplify the vaccine effect of reducing $R(t)$ for counties (‘class2’) with a relatively high percentage of older people, low population density, low median household income, and low hospital bed capacity. Last but not least, we observe that the presence of the Delta variant significantly decreases the vaccine effect of reducing $R(t)$ for all counties, especially the impact of the presence of the Delta variant for counties with core airport hubs (‘airport’) is significantly higher than its effect for counties without core airport hubs (‘class1’, ‘class2’, and ‘class3’). That finding is consistent with our previous statement that the causal impact of vaccine coverage is lower for counties with core airport hubs than counties without core airport hubs after the presence of the Delta variant. That might be because core airport hubs connecting cross-border mobility and gathering it into a high spatial density movement results in high infection risk among people.

The Role of mask requirement on the vaccine effect with the presence of Delta variant Mask wearing has been highly
recommended by CDC\textsuperscript{12} due to being less costly to apply than other NPI measures, which are associated with high social costs\textsuperscript{13}. However, the role of mask requirement on vaccine effect after the Delta variant remains to be quantified. The fourth hypothesis aims to gain insight into whether the mask requirement is needed when the vaccine coverage for the general public reaches 50\%, which corresponds with the presence of the Delta variant. To construct the experiment, we selected two groups of counties $C$ and $D$ within the same county class, with group $C$ keeping applying the mask requirement and the group $D$ relaxing the mask requirement after the vaccine coverage reaches 50\%. We quantify improved effects by taking the difference of vaccine effects (both daily and cumulative) for two counties groups ($\sigma_t = \theta_{C,t} - \theta_{D,t}$ and $\Sigma = \sum_{t=1}^{30} \sigma_t$, $t = 1, 2, ..., 30$). Figure 5 A summarizes the average improved daily effect, and Figure 5 B introduces the cumulative effect for each county class. Negative values of $\sigma_t$ and $\Sigma$ would mean that vaccine would reduce more number of $R_t$ by applying the mask requirement policy after the presence of the Delta variant. For example, the vaccine would reduce $0.5 (\sigma_{30} = -0.5)$ more of the $R_t$ at the day of 30 if counties with core airport hubs apply the mask requirement than those without the mask requirement after the presence of the Delta variant.

![Figure 5](https://via.placeholder.com/150.png)

**Figure 5.** Improved effect of the vaccine on disease propagation under the presence of Delta variant (with vs. without mask requirement). The daily vaccine effect is calculated by using the point-wise vaccine effect under the presence of the Delta variant for counties with mask requirement to subtract the point-wise causal effect of vaccine for counties without mask requirement. The demographic characteristics of each county class are presented in Table 1.

Figure 5 presents a demographic heterogeneity in the role of mask requirement on vaccine effect across counties. We observe that there is a significantly improved daily negative vaccine effect by applying mask requirement after the presence of Delta variant for almost all counties (t statistic being 65 and 109) except the counties (‘class1’) with a high median household income, low percentage of older people, low population density, and low hospital bed capacity. That observation leads to the rejection of H4. Besides, we observe that the improved negative vaccine effect is about 2 times higher after applying the mask requirement for counties with core airport hubs than counties without core airport hubs. In particular, we see that counties with high population density, high median household income, high hospital bed capacity, and low percentage of older people obtain the highest improved negative vaccine effect among counties without core airport hubs. It indicates that the mask requirement amplifies the vaccine effect of reducing disease propagation for counties with high mobility and activities needs. In conclusion, the estimated results suggest that although the mask requirement does not amplify the vaccine effect for all areas, it greatly amplifies the vaccine effect in reducing the viral burden against the disease infection for areas with core airport hubs, high population density, and vulnerable people even with the presence of the Delta variant. Palcu et al. (2022)\textsuperscript{14} also suggested that facial masks should be encouraged even after the vaccine is available.

**Discussion**

Although increasing the vaccine coverage is the most effective approach against COVID-19 infections, the optimal reopening strategy is still needed to balance the trade-off between disease prevention and economic recovery in the short term. However, the lack of understanding of the causal impact of dynamic vaccine coverage and the joint effects of NPIs in real-world scenarios limits us in designing the optimal vaccine prioritization and the corresponding reopening strategies. This study examines the vaccine effect’s temporal variations and demographic heterogeneity for U.S. counties based on the causal time series analysis. Furthermore, we examine the role of NPI measures and the presence of the Delta variant on the vaccine effect and disease spread, which allows us to monitor and understand the impact of relaxing imposed policies in the COVID-19 period with
unprecedented spatiotemporal granularity and scale. The analysis concludes that (1) The vaccine allocation strategy (e.g., age-specific allocation) would greatly affect the causal impact of vaccine coverage on disease infections. Although vaccine effect in reducing the disease infections for areas with high population density and fewer older people or core airport hubs is 2 times higher than areas with less population density. Areas with more older people need a high vaccine coverage to help them against the more contagious variants (e.g., the Delta variant) due to their physical weakness. Therefore, the age & population density specific vaccine prioritization is needed, especially when facing vaccine supply constraints. (2) Although business restriction policy and mask requirement are proved to be the more effective measures to prevent COVID-19 infections than other NPIs for areas with high population density and core airport hubs after the vaccine is available. The mask requirement is more applicable to assist disease prevention during the economic recovery process for two reasons. First, the mask requirement policy is less costly. Second, the mask requirement is more effective than other NPI measures in amplifying the vaccine effects against disease infections for areas with high population density or core airport hubs. In particular, the vaccine would reduce 8 more of the $R(t)$ in 30 consecutive days by applying the mask requirement for counties with airport hubs after more contagious variants show up. (3) Areas with a high percentage of older people are suggested to postpone relaxing the restaurant restriction or gather ban since these two measures significantly amplify the vaccine effect against disease infections. However, the bar closure policy barely affects the disease infections as well as the vaccine effect. The analysis specifies vaccine effects for counties with different demographics and explores how the NPI measures affect the vaccine effects and disease propagation in the COVID-19 period. The implication assists the economic recovery process design a more efficient reopening strategy, vaccine prioritization, and relocation policies.

This study investigates the causal impact of vaccine coverage on $R(t)$ from a Bayesian time series approach. It has certain limitations related to the causal experiment for the observational study. First, to avoid potential confounding issues in this study, we specify the experiment to a more controllable setting by separating the study period into six continued periods. Besides, we consider NPI measures, the presence of the Delta variant, daily mobility index, and dynamic hospital bed utilization rate as covariates to eliminate the confounding issue in examining the vaccine effects on disease spread. Although the influencing factors of disease infection might not be fully captured in the real-world scenarios, we address this issue by matching the most similar control county, which provides a best prior for the unknown factors. Second, additional disease variant shocks (e.g., the Delta variant), present later in the study period, significantly affect the $R(t)$ value and directly introduce biases in estimating vaccine effects under the lack of the measure of these new variants. We address the interference of the Delta variant by coding it as a binary indicator after it was detected at the end of April 2021. However, it might not be sufficient to capture the full effect later due to its rapid growth. Last but not least, the lack of disaggregated individual-level behavior analysis leaves the underlying reason for our insight to remain to be explored.

Although this study used aggregated measures to quantify the county-level demographic heterogeneity and temporal variation of vaccine effects and the corresponding NPIs at the COVID-19 phase, more microscopic analysis is worth to be explored with additional data. Further research focuses on extending the causal effects of vaccines to a more disaggregated level, where different patterns of vaccine effects on disease propagation can be obtained, and individuals’ activities can be explored to provide a detailed explanation for the vaccine effect. Besides, comparative analysis containing multiple communities could yield novel and more generalizable insights on vaccine effects and the corresponding control measures for developing better disease surveillance and economic recovery strategy. Furthermore, examining vaccine effects on disease spread after the entrance of new disease variants could strengthen the understanding of the reliability of vaccine effects in adjusting to diverse variants under real-world scenarios.

Materials and methods

Experiment design

To explore the causal impact of vaccine coverage on $R(t)$, the experiment is composed of four steps and described in Figure 6: (1) We characterize the demographic heterogeneity of disease dynamics by grouping counties into four classes. Within each county class, we cut the time from January to July 2021 into six continued periods and match each period with a vaccine coverage level. Figure 6A presents the matching mechanism for each coverage level. That procedure specifies the experiment for exploring the temporal variation of the causal time series analysis. (2) As shown in Figure 6B, counties whose vaccine coverage reaches the coverage level before the specified date are labeled as ‘treatment counties’, and the rest are labeled as ‘control counties’. To measure the causal impact of vaccine coverage for the treatment county $f$ at the vaccine coverage $i$, we select the best matching control county $g$. (3) In Figure 6C, we predict the counterfactual disease propagation $R(t)$ (what if the vaccine coverage does not reach the designed coverage?) after the county $f$ reaches the designed vaccine coverage using the observed data from $g$. (4) Figure 6D describe the calculation of causal impact. We compute the causal impact of the vaccine at the designed coverage rate $i$ by taking the difference between the predicted and observed $R(t)$ for county $f$.

As indicated by previous studies, population density, the percentage of older people, hospital resources, income, and core airport hubs are important indicators of disease infections and vary significantly over counties. In the first step, we classify
Figure 6. Model procedure. The date for each designed vaccine coverage are: 0% — 01/10/2021, 10% — 03/10/2021, 20% — 04/10/2021, 30% — 05/05/2021, 40% — 05/25/2021, 50% — 06/15/2021.

counties into four classes. The first county class is composed of the counties having core airport hubs in the U.S. The rest of the counties are obtained using K-mean clustering based on population density, median household income, percentage of older people, and the average daily number of beds in the hospital. They are grouped into three classes by comparing the Akaike Information Criterion based on the elbow method. The performance of each county group is presented in Table 1. In the second step, we define the study period as 70 consecutive days for each treatment county at specified vaccine coverage. As indicated in Figure 6B, we select the best matching control county based on the similarity of $R(t)$ before the date of reaching the designed vaccine coverage. We calibrate the model parameter via a cross-validation method in the third step to ensure the model’s reliability. As indicated in Figure 6C, the hyper-parameters are selected based on the model performance in the training and testing periods. The well-trained model is then used to predict the $R(t)$ in 30 consecutive days after reaching the designed vaccine coverage. In the fourth step, we define the point-wise causal effect of vaccine at its designed coverage $i$ in time $t$ for treatment county $f$ as $\theta_{i,t,f}$, and the cumulative causal effect of vaccine from time $t=0$ to time $t=T$ for treatment county $f$ as $\Theta_{i,T,f} = \sum_{t=0}^{T} \theta_{i,t,f}$. $R(t)$ is the observed value. Then, the key question is how to estimate $\theta_{i,t,f}$.

There are many methods to estimate the causal effect of diverse interventions on the outcome of interest. We used the Bayesian structure time series (BSTS) model to predict $R(t)$ for selected treatment counties. BSTS model captures time-varying local trends and seasonality variations for the time-correlated disease spread rate. It enables us to analyze the dynamic effects of vaccines on disease propagation for 30 consecutive days after reaching each designed coverage. The BSTS model for the treatment county $f$ is defined as the following:

$$
\begin{align*}
    y_t &= Z_t^\top \alpha_t + \epsilon_t \\
    \mu_{t+1} &= \mu_t + \eta_{\mu,t} \\
    \gamma_{t+1} &= -\sum_{s=0}^{t-1} \gamma_{s} + \eta_{\gamma,t} \\
    x_t^\top \beta_t &= \sum_{j=1}^{J} x_{j,t} \beta_{j,t}
\end{align*}
$$

(1)

$y_t$ is the observed $R(t)$ for the treatment county $f$ on day $t$ and $\alpha_t$ denoting the unobserved latent states. The evolution of unobserved latent states is defined as $\alpha_{t+1} = T_t \alpha_t + R_t \eta_t$. Matrices $Z_t$, $T_t$, and $R_t$ contain unknown parameters. The vector $\alpha_t$ is formed by concatenating individual state components, such as the local trend $\mu_t$, seasonality $\gamma_t$, and regression $x_t^\top \beta_t$ components. $\mu_t$ represents local variations of the time series data and $\gamma_t$ captures the seasonal variation (e.g., holidays) with $S$. 

8/12
Table 1. The performance of mean scores for each county class after the normalization. ‘class 1’ refers to counties with high median household income, relatively low population density, low percentage of older people, and low hospital bed capacity; ‘class 2’ refers to counties with relatively high percentage of older people, low population density, low median household income, and low hospital bed capacity; ‘class 3’ refers to counties with high population density, high median income, high hospital capacity, and low percentage of older people. Note: 1, ‘airport’ refers to counties having core airport hubs in U.S.23, 2, older people mean people who are at least 65 years old.

<table>
<thead>
<tr>
<th>Name</th>
<th>Population density</th>
<th>Median household income</th>
<th>Percentage of the older people</th>
<th>Hospital bed capacity</th>
<th>Core airport hubs</th>
<th>Number</th>
</tr>
</thead>
<tbody>
<tr>
<td>Class 1</td>
<td>0.12</td>
<td>0.56</td>
<td>0.12</td>
<td>0.12</td>
<td>NO</td>
<td>97</td>
</tr>
<tr>
<td>Class 2</td>
<td>0.02</td>
<td>0.21</td>
<td>0.30</td>
<td>0.08</td>
<td>NO</td>
<td>160</td>
</tr>
<tr>
<td>Class 3</td>
<td>0.42</td>
<td>0.42</td>
<td>0.13</td>
<td>0.43</td>
<td>NO</td>
<td>68</td>
</tr>
<tr>
<td>Airport</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>YES</td>
<td>16</td>
</tr>
</tbody>
</table>

\[
\eta_j(t) = \beta_j(t) + \epsilon_j(t)
\]

\[
\beta_j(t) = \beta_j(t-1) + \eta_{\beta_j}(t)
\]

\[
\epsilon_j(t) \sim \text{Cauchy}(0, 2.5)
\]

\[
R(t) = \frac{\text{Vaccine coverage} \times \text{Core airport hubs} \times \text{Population density}}{\text{Median household income}}
\]

\[
\text{Effective reproduction number } R(t)
\]

\[
\text{Vaccine coverage}
\]

\[
\text{Population -- 0.12 NO 0.02 160 0.08 0.42 33 16 YES Core airport}
\]

Supplementary Figure 3A shows the variation of average daily 24\(R(t)\) values from 1 to 5, the presence of the Delta variant obtained from local news, daily bed utilization rate obtained from the Health and Human Service Protect Public Data Hub, and the number of trips per person obtained from the U.S. Department of Transportation. To ensure that the disease dynamics are statistically meaningful, we remove counties with incomplete data, which results in 341 counties in the study. We use selected data to explore the causal impact of the vaccine coverage and the joint effects of covariates on COVID-19 propagation in the U.S.

\[
\text{Effective reproduction number } R(t)
\]

\[
\text{Vaccine coverage}
\]

\[
\text{Population -- 0.12 NO 0.02 160 0.08 0.42 33 16 YES Core airport}
\]

Supplementary Figure 3B shows the variation of average daily vaccine coverage within each county class. We report that the vaccine coverage ranges from 0% to 69.7% during the study period, with a mean value of 14.7%.
**NPI measures and the Delta variant**
The NPI measures in our study are obtained from Kaiser Family Foundation\textsuperscript{12} including business reopening policy, restaurant restriction, gather ban, bar closure, and mask requirement. Each measure contains multiple steps to match the recovery stages and is presented in Table 2. To capture the effect of the presence of the Delta variant, we collect the earliest state-level detected date of the Delta variant from Web news by hand and apply a two-weeks delay for an incubation time. Besides, we code the presence of the Delta variant as a binary variable. We visualize the mask requirement, business reopening policy, and the Delta detection in Supplementary Figure 4.

<table>
<thead>
<tr>
<th>Policy</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Business reopening</td>
<td>Reopened: 0; Easing restrictions: 1; Restrictions: 2</td>
</tr>
<tr>
<td>Mask requirement</td>
<td>No: 0; Unvaccinated people only: 1; Yes: 2</td>
</tr>
<tr>
<td>Bar closure</td>
<td>Open: 0; Open with service limit: 1 ; Closed: 2</td>
</tr>
<tr>
<td>Gather ban</td>
<td>No limit: 0; Limit on large gatherings: 1; All gatherings prohibited: 2</td>
</tr>
<tr>
<td>Restaurant restriction</td>
<td>Open: 0; Open with limited number of people to indoor service: 1 ; Closed to indoor service: 2</td>
</tr>
</tbody>
</table>

**Table 2.** Status for NPI measures in the COVID-19 period

**Bed utilization rate and mobility index**
Daily bed utilization rate and individual mobility directly reflect local disease dynamics. In this study, the hospital resource data are obtained from the Health and Human Service Protect Public Data Hub\textsuperscript{31}. We calculate the bed utilization rate as the total number of staffed inpatient and outpatient beds divided by the total number of staffed inpatient beds occupied in the hospital during the 7 days. We report that the mean and standard deviation of the county-level bed utilization rate is 60.23% and 16.91%. Previous studies\textsuperscript{37,38} have asserted a close association between mobility and social distancing policies and disease propagation before the vaccine is available. However, this relationship might be changed since people might loosen their protective action based on their vaccinated statuses\textsuperscript{20}. In this study, we use the county-level daily trips generated by each person to capture the temporal variation of the mobility index. The data are obtained from the U.S. Department of Transportation\textsuperscript{33}. The mobility index and bed utilization rate is visualized in Supplementary Figure 5. We report the mean and standard deviation of county-level daily trips per person to be 3.49 and 0.88.

**Data availability statement**
Publicly available datasets were analyzed in this study. This data can be found here: all data are cited.

**Author contributions statement**
Lu Ling and Satish V. Ukkusuri conceived and conducted the experiment(s), Lu Ling and Satish V. Ukkusuri analyzed the results. All authors reviewed the manuscript.

**Competing interests**
The authors declare no competing interests.

**References**


Supplementary Files

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